

1-1-2003

Evaluation of bridge rating methods

Espen Mellingen
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Evaluation of bridge rating methods

by

Espen Mellingen

A thesis submitted to the graduate faculty

in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

Major: Civil Engineering (Structural Engineering)

Program of Study Committee:
Terry J. Wipf, Major Professor
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Ames, Iowa

2003

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has met the requirements of Iowa State University

Signatures have been redacted for privacy




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1. INTRODUCTION

1.1. BACKGROUND

The 2001 Iowa National Bridge Inventory (NBI) Report (11) indicated that of the 25,138 bridges in Iowa, 7,102 (29%) are either structurally deficient or functionally obsolete. While many of these bridges may be strengthened or rehabilitated, some simply need to be replaced. Another option, however, for managing these structures is to perform diagnostic load testing on bridges that are structurally deficient. Frequently, diagnostic load tests reveal strength and serviceability characteristics that exceed the predicted codified parameters. Usually, the codified parameters are conservative when predicting the load distribution characteristics and the influence of other structural attributes; hence the predicted rating factors are often conservative. In cases where calculations show a structural deficiency, it may be very beneficial to apply a tool that utilizes a more accurate model that incorporates field-test data; at a minimum, this approach would result in more accurate load ratings but will more frequently result in increased rating factors. Bridge Diagnostics, Inc. (BDI) developed hardware and software that is specially designed for performing bridge-ratings based on data from physical testing. The hardware consists of pre-wired strain gages, a data acquisition system, and other components. The software consists of three separate programs for visually evaluating test data, developing an analytical model, analyzing and calibrating the model, and performing load-rating calculations with the calibrated model. Figure 1.1 illustrates the bridges in Iowa from the 2001 NBI Report (12).

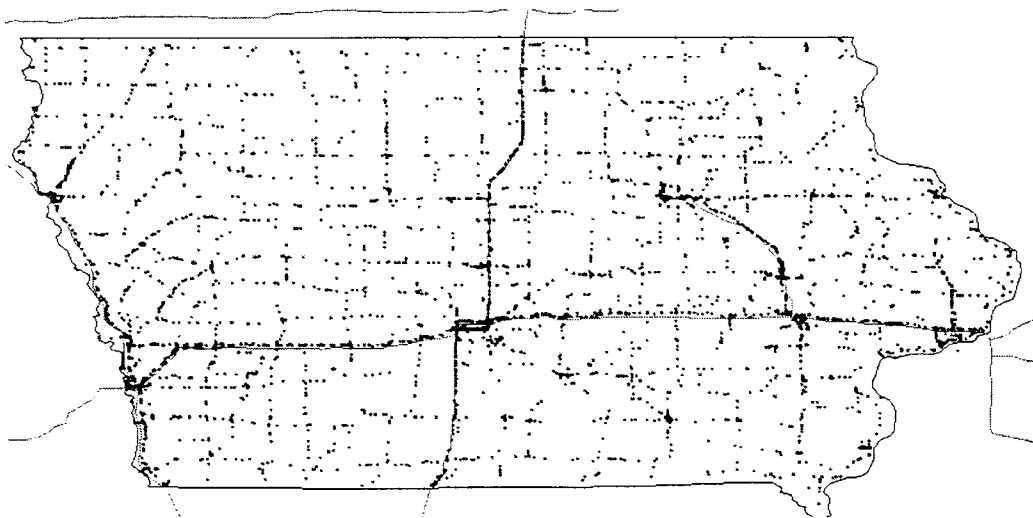


Figure 1.1. Bridges in Iowa: from 2001 NBI Report (11).

1.2. OBJECTIVE AND SCOPE

The objective of the work presented herein was to investigate the useability of the BDI structural testing system for bridge load rating based on physical testing. The project includes examination of all aspects of the system including:

- Instrumentation installation.
- Data collection.
- Data interpretation.
- Analytical model verification, generation, calibration, and load rating.
- Comparison with codified load rating using the Load Factor Design (LFD) Method.

Seven different “typical” bridge structures were selected and investigated to reach the objective. The bridges included three steel-girder bridges with concrete decks, two concrete slab bridges, and two steel-girder bridges with timber decks. In addition, a steel-girder bridge with a concrete deck previously tested and modeled by BDI was investigated for model verification purposes. This report will focus primarily on bridge descriptions, equipment installation, describing the analytical process, including analytical model verification, generation, calibration, analytical load rating, and codified load rating.

1.3. METHODOLOGY

The methods used in this report include a complete investigative process, which is described below:

- Model verification includes comparing previously calculated parameters with new model parameters in order to verify that the calibration process is acceptable and accurate.
- Model generation includes creating an analytical bridge model using the BDI Software.
- Model calibration includes using the measured field strains and the analytical model to adjust model parameters such that the difference between field and analytical strain data is minimized.
- Analytical load rating includes applying appropriate design trucks to the calibrated model in order to extract loads and obtain rating factors for the bridge sections of interest.
- Codified load rating includes applying appropriate design truckloads on the bridge as stated in AASHTO Standard Specifications (4).

1.4. REPORT SUMMARY

This report is divided into six chapters, and Chp. 1 provides the background information, objective and scope, methodology, and report summary. The literature review for evaluation of the BDI and other rating methods, and a description of the different design methods available is presented in Chp. 2. A description of the BDI system is given in Chp. 3. Chapter 4 provides descriptions of all seven tested bridges in addition to the bridge used for model verification, and Chp. 5 summarizes the results for all eight bridges. Finally, Chp. 6 provides conclusions and recommendations.

2. LITERATURE REVIEW & SURVEY

A literature search was performed to collect information on rating methods and bridge analysis methods. The Structural Information Service Center in the Iowa State University Bridge Engineering Center was searched first. In addition, several computerized searches were conducted through the Iowa State University Parks Library. A summary of representative literature is presented which focuses on issues relating to this investigation.

2.1. CLASSIFICATION OF BRIDGES

In bridge engineering, it is common practice to classify bridges into three broad groups, which are short-span, medium-span, and long-span bridges. Currently, no established criteria define the span ranges, but a common practice to classify bridges by span length are as follows:

- Short-span bridges: 20-125 ft
- Medium-span bridges: 125-400 ft
- Long-span bridges: Over 400 ft

Bridges with spans less or equal to 20 ft are classified as culverts. Bridges can also be classified according to materials (concrete, steel, or wood), useage (pedestrian, highway, or railroad), or structural form (slab, girder, truss, arch, suspension, or cable-stayed). All bridges investigated in this study are, by applying the first criteria noted, defined as short-span highway bridges.

2.2. METHODS OF BRIDGE ANALYSIS

According to Xanthakos (14), for the purpose of elastic analysis, steel beam bridge systems may be classified into (a) orthotropic plate concepts that consider the bridge system as an elastic continuum to be treated as an equivalent plate; (b) grid systems concepts that idealize the bridge system as an equivalent grillage of interconnected longitudinal and transverse beams, cross-members, and diaphragms; and (c) girder-plate concepts where the interacting forces between the slab and longitudinal girders are treated as the redundants of the system. Examples of inelastic behavior can be found in composite bridge systems, so classical force and displacement methods that are based on elastic behavior need to be supplemented or replaced by finite-difference and finite-element techniques, folded plate methods, finite strip methods, grillage analogy, series or other harmonic methods, and yield line theories.

2.3. DESIGN METHODS

The American Association of State Highway and Transportation Officials (AASHTO) Standard Specifications (4) allows two alternative design procedures: Allowable Stress Design (ASD) and strength design method (or load factor design (LFD)). In addition, bridge engineers also have a choice of using the newly adopted AASHTO Load and Resistance Factor Design (LRFD) Specifications (2) as a new standard.

2.3.1. Allowable Stress Design (ASD) Method

The ASD Method is a service level design method and historically has been the standard design method for most structures. The method proportions structural members using design loads and forces, allowable stresses, and design limitations for the material of interest under service conditions. For example, for structures composed of steel girders with concrete slabs connected by shear connectors, the composite girders and slabs shall be designed and the stresses computed by the composite moment of inertia method and shall be consistent with the predetermined properties of the various materials. The ASD method implies that the ultimate limit state is automatically satisfied if allowable stresses are not exceeded.

2.3.2. Load Factor Design (LFD) Method

LFD Method is an alternative method for the design of simple and continuous beam and girder structures of moderate length. It is a limit states design with emphasis on ultimate limit states, with the serviceability limit states typically checked for compliance. The required strength of a section is the strength necessary to resist the factored loads and forces applied to the structure in the combinations stipulated by the AASHTO Standard Specifications (4). The “design strength” refers to the factored resistance, ϕR_n , whereas “required strength” refers to the load effects computed from factored loads. The resistance factor “ ϕ ” depends on the type of the load effects (e.g., flexure, shear, torsion, etc.) and on the special characteristics of the loaded member (e.g., reinforced concrete, prestressed concrete, precast, cast-in-place, etc.).

2.3.3. Load and Resistance Factor Design (LRFD) Method

The basic LRFD Methodology is that each component and connection must satisfy a modified version of the LFD Methodology. Each component and connection shall satisfy Equation 2-1 for each limit state, unless otherwise specified. For service and extreme event limit

states, resistance factors shall be taken as 1.0. All limit states shall be considered of equal importance. Accordingly, as illustrated in AASHTO LRFD Specifications (2),

$$n \times \sum \mu \times Q_i < \phi \times R_n = R_f \quad (2-1)$$

where:	n	=	$n_D \times n_R \times n_i > 0.95$
	μ	=	load factor (statistically based multiplier applied to force effects)
	ϕ	=	resistance factor (statistically based multiplier applied to nominal resistance)
	n_D	=	factor relating to ductility
	n_R	=	factor relating to redundancy
	n_i	=	factor relating to operational importance
	Q_i	=	force effect (deformation or stress, i.e., thrust, shear, torque, or moment caused by applied loads, imposed deformations, or volumetric changes)
	R_n	=	nominal resistance (based on permissible stresses, deformations, or specified strength of materials)
	R_f	=	factored resistance = $\phi \times R_n$

2.4. BRIDGE RATING USING DESIGN METHODS

This section describes methods currently used for bridge rating, which include the ASD Rating Method, the LFD Rating Method, and the Load and Resistance Factor Rating (LRFR) Method. Although these methods are described in the following sections, only the LFD Method has been utilized in this report since it is most similar to the BDI approach. An important objective of this investigation was to compare the rating values obtained from theoretical methods with those obtained utilizing the software, which uses field load test data. Therefore, it was desired to apply the same methodology so that the rating values can be realistically compared.

2.4.1. ASD Rating

According to AASHTO Standard Specifications (4), since the ASD Rating utilizes stresses, the rating equation is as shown in Equation 2-2:

$$RF = \frac{f_s - f_{DL}}{f_{LL-I}} \quad (2-2)$$

where:	RF	=	Rating Factor
	f_s	=	Allowable stress

$$\begin{aligned}
 f_{DL} &= \text{Stresses due to dead load} \\
 f_{LL_I} &= \text{Stresses due to live load plus impact}
 \end{aligned}$$

2.4.2. LFD Rating

Since the LFD Rating utilizes loads, according to AASHTO Specifications (4), the rating equation is as shown in Equation 2-3:

$$RF = \frac{C - 1.3 \times DL}{2.17 \times LL \times (1 + I)} \quad (2-3)$$

where:

$$\begin{aligned}
 RF &= \text{Rating Factor} \\
 C &= \text{Capacity of section of interest} \\
 DL &= \text{Dead Load} \\
 LL &= \text{Live Load} \\
 I &= \text{Impact coefficient}
 \end{aligned}$$

2.4.3. LRFD Rating (LRFR Method)

The LRFR Method utilizes stresses, but applies more factors in the rating equation. According to AASHTO LRFD Specifications (2), the LRFR Rating equation is as follows:

$$RF = \frac{C - \gamma_{DC} \times DC - \gamma_{DW} \times DW + \gamma_P \times P}{\gamma_L \times L \times (1 + IM)} \quad (2-4)$$

The capacity when utilizing the Strength Limit States is shown in Equation 2-5:

$$C = \phi_C \times \phi_S \times \phi \times R \quad (2-5)$$

And the capacity when utilizing the Service Limit States is shown in Equation 2-6:

$$C = f_R \quad (2-6)$$

where:

$$\begin{aligned}
 RF &= \text{Rating Factor} \\
 \phi_C &= \text{Condition factor} \\
 \phi_S &= \text{System factor} \\
 \phi &= \text{LRFD Resistance factor} \\
 R &= \text{Nominal member resistance} \\
 C &= \text{Capacity} \\
 f_R &= \text{Allowable stress}
 \end{aligned}$$

γ_{DC}	=	LRFD Load factor for structural components and attachments
DC	=	Dead load effect due to structural components and attachments
γ_{DW}	=	LRFD Load factor for wearing surfaces and utilities
DW	=	Dead load effect due to wearing surfaces and utilities
γ_P	=	LRFD Load factor for permanent loads other than dead loads
P	=	Permanent loads other than dead loads
γ_L	=	Evaluation live load factor
L	=	Live load effect
IM	=	Dynamic load allowance

2.5. BDI RATING SYSTEM

Although there are other bridge-rating software packages available, only the BDI Software, which was used throughout this investigation, is described in this section. The BDI Software applies the limit states for rating calculations because it uses the loads applied to the structure. The rating equation used by the BDI Software is of the same general format as the LFD Method; however, the user must specify the load factors as illustrated in Equation 2-7:

$$RF = \frac{C - \gamma_{DL} \times DL}{\gamma_{LL} \times LL \times (1 + I)} \quad (2-7)$$

where:	RF	=	Rating Factor
	C	=	Capacity
	γ_{DL}	=	Dead Load Factor
	γ_{LL}	=	Live Load Factor
	I	=	Impact coefficient

In 1999, the Iowa Department of Transportation (Iowa DOT) contracted the BDI (9) team to test and rate eight highway bridges. The final report of that work was presented to the Iowa DOT in November 1999 as “Load Testing and Load Rating Eight State Highway Bridges in Iowa.” Four of these bridges were three-span reinforced concrete slab bridges, two with a 17-degree skew and two with no skew. Also tested and rated were a single span and a three span steel-girder/reinforced-concrete deck bridge, a three span parabolic reinforced-concrete T-beam bridge, and a single span prestressed-concrete/steel-girder hybrid bridge. Based on the codified approach, all but one of the

eight bridges has an Inventory rating for an HS-20 truck below 1.0, while, based on the BDI approach, only one of the bridges has an Inventory rating for an HS-20 truck below 1.0.

For the HS-20 load vehicle, the BDI approach yielded higher rating factors than the codified approach. The four reinforced concrete slab bridges had Inventory Ratings increases varied from 4 to 103 percent with Inventory Rating factors greater than the codified factors by an average of 70 percent. The two steel bridges tested had Inventory Rating factors that were 146-158 percent greater than the codified factors. The prestressed concrete/steel hybrid bridge and the parabolic reinforced concrete T-beam bridge had ratings that were in excess of 350 percent greater. Much of the rating increases were credited to issues such as increased exterior beam stiffness due to the presence of reinforced concrete parapets and the presence of unintended composite action.

The model accuracy results for all eight bridges are given in Table 2.1. These results illustrate that, in general, the concrete slab bridges (bridges BDI-1, BDI-2, BDI-3, BDI-5 and BDI-8) are more difficult to model than the steel girder bridges (bridges BDI-4, BDI-6 and BDI-7).

Table 2.1. Model accuracies for the eight bridges analyzed by Bridge Diagnostics, Inc.

Bridge	Total error ^a	Percent error ^b	Scale error ^c	Correlation Coefficient ^d
BDI-1	943	13.0	4.1	0.95
BDI-2	1,570	9.5	4.1	0.95
BDI-3	1,028	4.4	3.0	0.98
BDI-4	911	6.0	4.2	0.97
BDI-5	2,366	15.5	5.3	0.93
BDI-6	2,546	2.0	3.2	0.99
BDI-7	1,601	3.4	3.5	0.98
BDI-8	1,258	2.5	1.7	0.99

^a Total strain difference in microstrain.

^b Sum of the strain differences squared divided by the sum of the measured strains squared.

^c Maximum error from each gage divided by the maximum strain from each gage.

^d Represents how well the shapes of the computed response histories match the measured response.

where: BDI-1, BDI-2, BDI-3, BDI-5 are three span reinforced concrete bridges.

BDI-4 is a single span steel girder bridge with a concrete deck.

BDI-6 is a three span steel girder bridge with a concrete deck.

BDI-7 is a single span steel girder and prestressed concrete beams bridge with a concrete deck.

BDI-8 is a three span parabolic reinforced concrete T-beam bridge.

The parameters given in Table 2.1 are defined as follows: the total error (a), the percent error (b), the scale error (c), and the correlation coefficient (d). The correlation coefficient value can vary between -1.0 and 1.0 where 1.0 represents an exact linear relationship and -1.0 represents an exact opposite linear relationship. The equations used to calculate these parameters are described in Chp. 3.

2.6. LOAD RATING THROUGH PHYSICAL TESTING

In 1998, Lichtenstein (10) authored the “Manual for Bridge Rating Through Load Testing” through an National Cooperative Highway Research Program (NCHRP) project as a guide for the nondestructive load testing of bridges for improved rating. This report focused on defining and illustrating nondestructive load testing and its applications to the rating community. There are two types of nondestructive load testing described by Lichtenstein for the purpose of bridge load rating: diagnostic and proof. Diagnostic load testing involves loading the bridge in question with a known truck load at set positions and measuring the bridge response. The results of a diagnostic test would typically be used to facilitate rating calculations. Proof load testing involves setting a limit or goal for the bridge and gradually increasing the vehicle load until the limit or goal is reached. Both types of load tests can yield knowledge of a particular structure’s behavior and can be used to generate more accurate load ratings. Lichtenstein notes that most bridge types can benefit from testing.

2.7. SURVEY OF STATES

To gain a better understanding of how bridge owners are using physical testing as a tool to better manage their bridge inventory, a survey of State DOT’s and Iowa County Engineers was conducted. A copy of the questionnaire sent to State DOT’s, which includes 8 questions is presented in Appendix A. The county survey, which includes 3 questions, is given in Appendix B.

Of the 36 survey respondents, 10 responded to the state questionnaire, and 26 responded to the county questionnaire. Based on the relatively low response rate, only general conclusions drawn from the responses can be made. Most respondents do not perform physical testing for load rating purposes, and responded that, in general, such testing is not conducted due to lack of specific procedures, unfamiliarity with various non-destructive techniques, believed to not be cost effective, or current comfort with the typical AASHTO rating results. Also, when asked how much would be budgeted for a physical load test, analysis, and rating for a given hypothetical bridge, most participants responded “Less than \$5,000”. However, it is interesting to note that most respondents that do perform load testing for rating purposes, indicated “More than \$15,000” when asked the same

question. Based on these results, there is reason to believe that those who do not perform load testing for rating purposes assume that it is not economically feasible, while those who perform load testing have found it to be economically viable for evaluating bridge conditions. It was also found that most respondents that perform load testing for rating purposes consider edge rail stiffening and restraint at the abutments or piers when calculating ratings.

3. COMPONENTS OF BDI LOAD RATING SYSTEM

The system developed by BDI is a systematic approach to the testing, modeling, and rating of bridges. The system, which has three basic phases each with their own tools and individual processes, is described in the following sections. A step-by-step procedure for completing an analysis and rating is given in Appendix C.

3.1. PRELIMINARY INVESTIGATION

The first step is to perform a preliminary investigation of the bridge, which includes a visual inspection of the bridge. It is important to observe anything out of the ordinary that can influence the bridge behavior, such as concrete deterioration, beam deformations, large cracks in the slab, support conditions, etc. In addition, if possible, previous maintenance and inspection reports should also be reviewed.

Based on information collected during the preliminary investigation, an instrumentation plan is developed. This plan, which uses the components described in the following sections, is established to gain a better understanding of the bridge behavior (e.g., end restraint, edge stiffening, composite action, load distribution, etc.).

3.2. BDI STRUCTURAL TESTING SYSTEM (STS)

The Structural Testing System (STS) is the field component of the testing system, and consists of four main elements: the BDI Intelliducers, the BDI STS Units, the BDI Autoclicker, and the BDI Power Unit. The main purpose of using the STS is to collect bridge behavior data. Specifically, collecting strain data as a truck with known dimensions and weights is driven over the bridge. It is common to position the truck in at least three different transverse positions: the outer wheel line placed at two feet from each curb and the truck centered on the bridge. Additional positions may also be included if needed. Typically, the truck will be driven in each lane twice to verify that the recorded strains are consistent. If any strain asymmetry is determined (by comparing data from symmetric load paths), the analytical model must be developed accordingly.

3.2.1. BDI Intelliducer

The BDI Intelliducer, shown in Fig. 3.1, is the strain transducer used with the BDI system for measuring bridge response. Each Intelliducer measures 4.4 in. x 1.2 in. x 0.4 in., with either a 15-ft or 25-ft wire attached and has the ability to identify itself to the rest of the system with a unique number

(i.e. 4696, 4788, etc.) that can be identified and recognized by the STS power unit (described subsequently). From this unique number, the system has the ability to calibrate and zero the gage using a pre-stored gage calibration factor. Intelliducers may be used on many different surfaces, including, but not limited to, steel, concrete (reinforced and pre-stressed), and timber. This wide variety of uses stems from the design and the ease of application of the transducers. Two holes (3 in. on center) in the transducer are for the 'tabs', which are bonded to the testing surface using Lactic adhesive after appropriately preparing the surface of the element being tested.



Figure 3.1. A BDI Intelliducer in use on top of a concrete curb.

For gage placement on reinforced concrete structures, gage extensions should be implemented (see Fig. 3.2) to increase the 3-inch gage length; the longer length enables surface strains to be averaged over a greater distance, thus reducing the effects of cracks in the concrete. BDI has prescribed a set of standards for the use of gage extensions. A gage length of $1.0 \times d$, where d is the member depth, and $L/20$, where L is the span length, are given as lower and upper bounds, respectively, for reinforced concrete slabs and rectangular beams. For T-beams, the lower and upper bounds are given as $1.5 \times d$ and $L/20$, respectively.

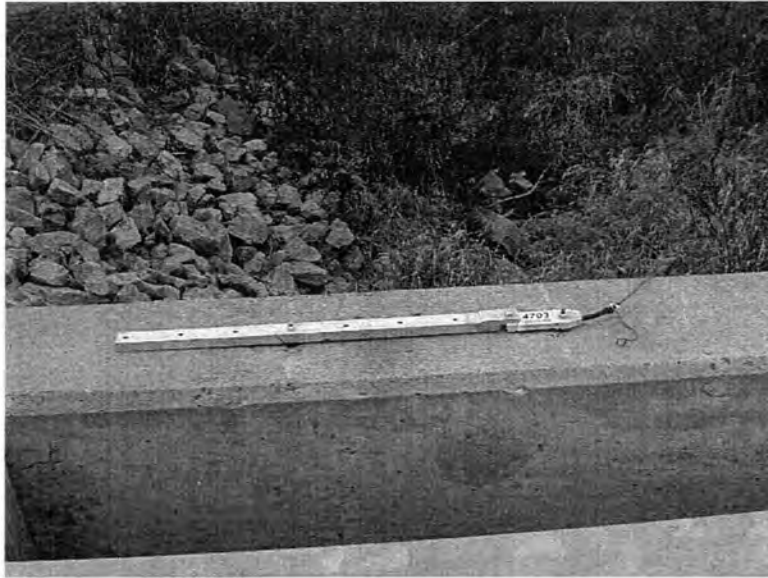


Figure 3.2. An Intelliducer with gage extensions in use.

3.2.2. STS Unit

The BDI STS Unit, shown in Fig. 3.3, transfers the data collected from the Intelliducers to the Power Unit (described in the following section). Each STS Unit is capable of collecting data from four Intelliducers. An STS Unit has the capability of storing 50,000 data points during a single test. At the conclusion of a test, the data are transferred to the Power Unit (described subsequently).

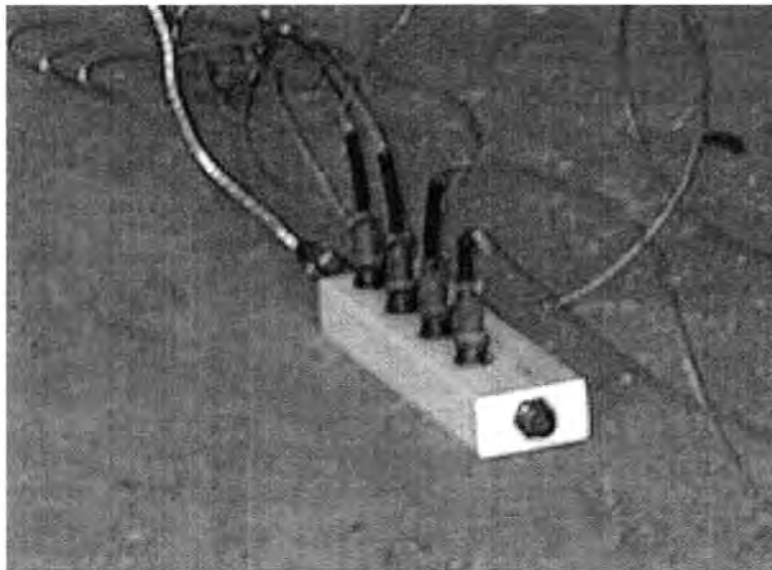


Figure 3.3. BDI STS Units in use during a load test.

Each STS Unit measures 2.3 in. x 3.0 in. x 11.0 in. and weighs 1.8 lbs. The unit is equipped with six connection points, four transducer connections, a “line out”, and a “line in”. All of the connections are quick-lock, military-style. The “line out” or P/C end of the unit transmits data to the Power Unit and P/C. The “line in” connection is designed to attach to other units in series and/or parallel through the use of Y-cables. This wiring configuration is a significant advantage over traditional transducer wiring in that only a single cable is connected to the Power Unit.

3.2.3. Power Unit

The Power Unit, shown in Fig. 3.4, powers the intelligiducers and transmits commands to the system during the test. Each transducer requires a 5-volt excitation voltage that is provided by the Power Unit. The unit has the ability to operate under two different energy sources, DC current from an automobile battery or AC current from a small portable generator or inverter.

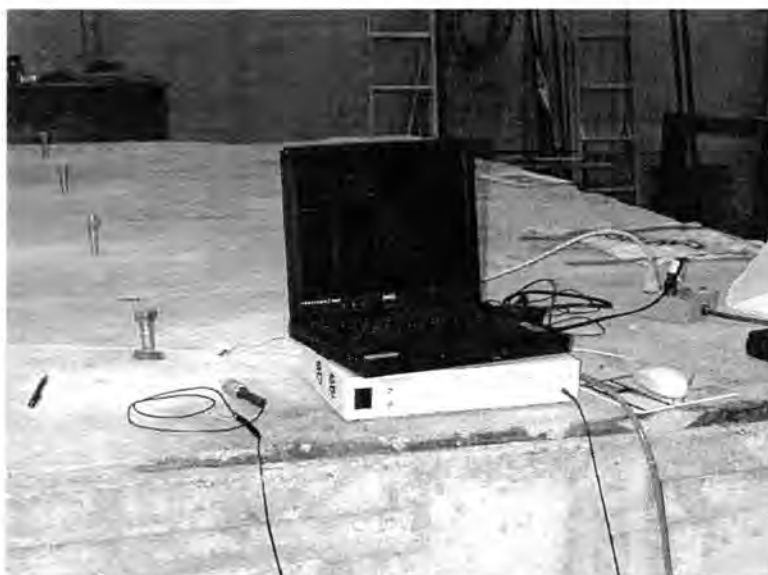


Figure 3.4. BDI Power Unit connected and ready for use.

3.2.4. BDI Autoclicker

The BDI Autoclicker, shown in Fig. 3.5, measures and transmits the load vehicle position to the Power Unit through the use of an electronic eye and hand-held radio transmitters. A reflective strip placed on the load vehicle's tire triggers the electronic eye. Thus, every wheel revolution creates a “click” in the data. These “clicks” are used to correlate data collected in the time domain to the truck position domain. For bridges that have a very short span as compared to a wheel revolution, the clicks

may be recorded by hand by simply removing the Autoclicker radio and tapping the transmit button at regularly spaced intervals.

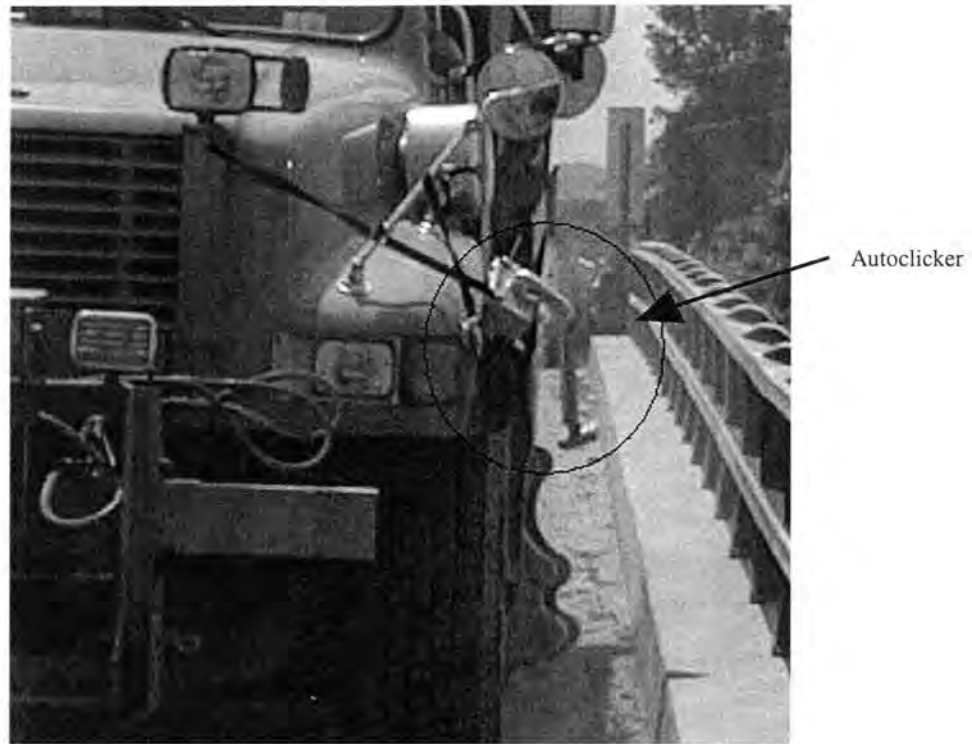


Figure 3.5. BDI Autoclicker in use during a load test.

3.2.5. STS Software and Personal Computer

The control functions of the system are performed by the STS software. The software is run in a Microsoft Windows environment on a laptop computer that is attached, via a parallel port, to the Power Unit. The system is relatively easy to use with pull down menus and large command buttons. The initial setup of the software should only be completed after all connections between Intelliducers, STS Units, and the Power Unit have been completed. The initial setup verifies that all Intelliducers are recognized by the rest of the system and that all connections are tight.

The main software menu window contains most of the information that is critical to the load test. Items such as sample frequency, test length, and file output name are easily accessible in the main window. Other options specifically related to Intelliducers such as channel gain, initial offset, and filtering are located in the advanced options menu. Careful attention should be given to these settings to ensure proper data collection.

3.3. BDI SOFTWARE PACKET

The BDI Software Packet is the analytical modeling part of the testing system, and consists of three main components: WinGRF – data presentation, WinGEN - model generator, and WinSAC - structural analysis and correlation. All elements serve different purposes, but each is essential to the overall process. Each component has been developed such that data can be seamlessly moved from one application to another. These three components are described in detail in the following sections.

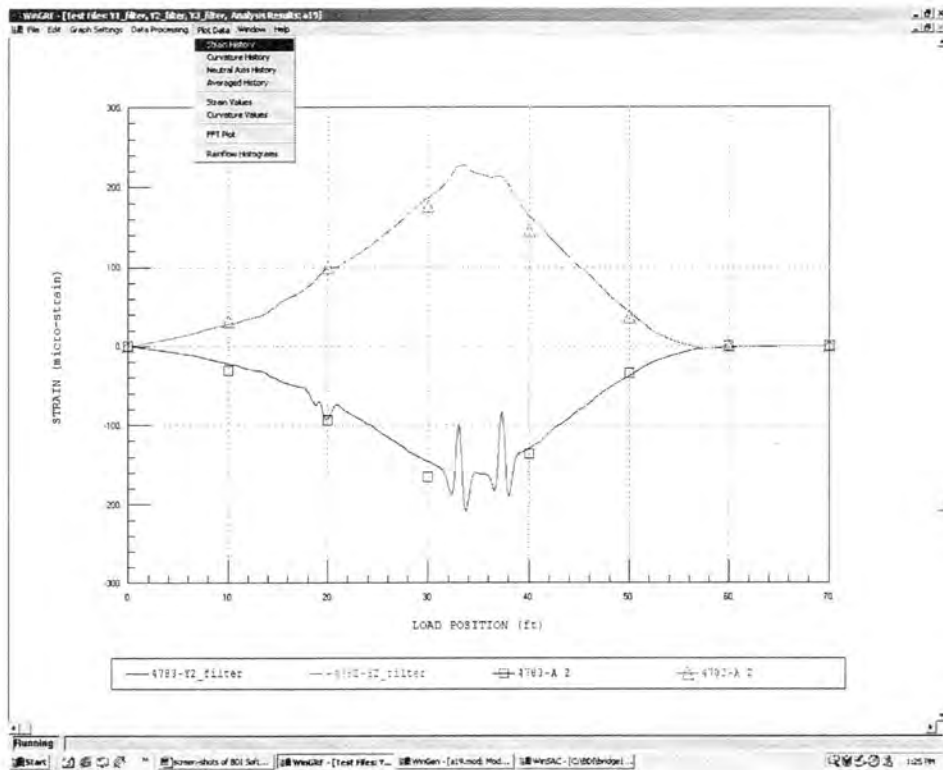
3.3.1. BDI Graph Data Viewer (WinGRF)

WinGRF is used for graphical data presentation, and is the first step in the modeling process. First, the “clicker distance” – the known distance (e.g., wheel circumference) used to convert data from the time domain into the truck position domain – must be input in the field strain files. Plots can then be viewed in terms of truck position to observe bridge behavior information, such as the presence of end restraint conditions, non-symmetric behavior, etc. Plots such as neutral axis location may also be constructed if the distance between the top and bottom gages has been input in the program. Options, such as averaging and filtering of data files and offset correction, may also be completed in WinGRF. Figure 3.6 shows typical screen shots of WinGRF; an example of strain plots is shown in Fig. 3.6a while an example of a neutral axis plot is presented in Fig. 3.6b.

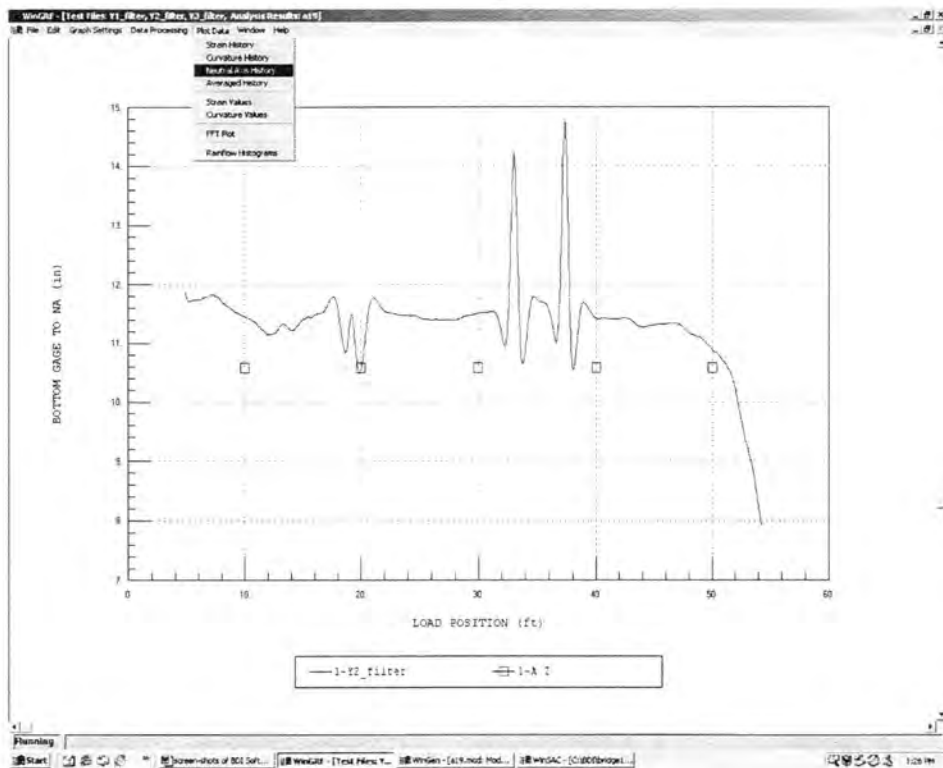
3.3.2. Model Generator (WinGEN)

WinGEN is a finite element model generator. This application allows the user to create models using beam and shell elements. A 2-D model can be created using the WinGEN; however, it is also possible to create a 3-D model using a drafting program, such as AutoCAD, and then import the drawing file to WinGEN. A sketch of a typical model is presented in Fig. 3.7.

Once the overall model is defined and all section and material properties have been entered, the location of intelligucers used in the field test can be established on the sections (both beam and deck). Through this, direct comparisons between the field data and analytical results can be made. A common source of error in bridge modeling is to implement incorrect boundary conditions. WinGEN allows the use to establish constraint conditions at the abutments and at the piers (if any) that represent the actual conditions. To make comparisons between the field strains and the analytical strains, an idealized truck simulating the truck used during the field test can be created. When necessary, model optimization parameters are also established using WinGEN.



a. Strain plots.



b. Neutral axis plot.

Figure 3.6. Typical screen-shots of WinGRF.

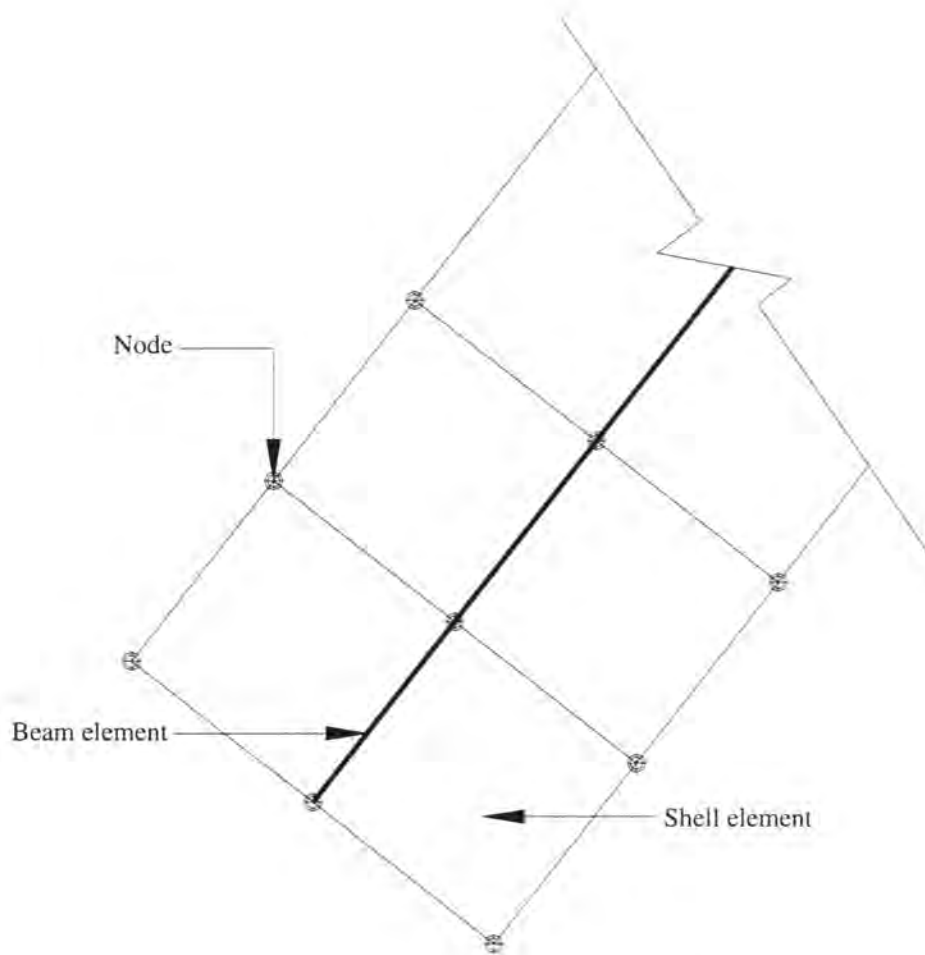
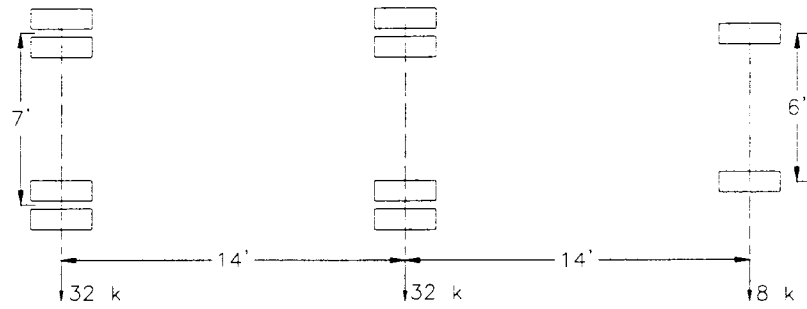
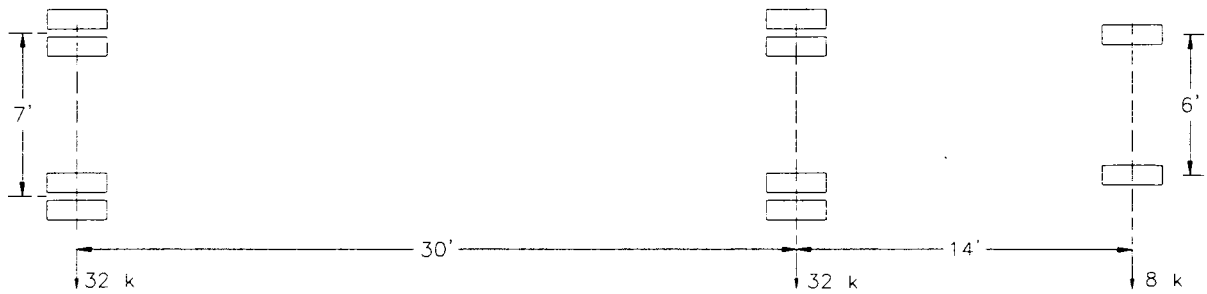


Figure 3.7. Schematic of typical mesh generated with WinGEN.

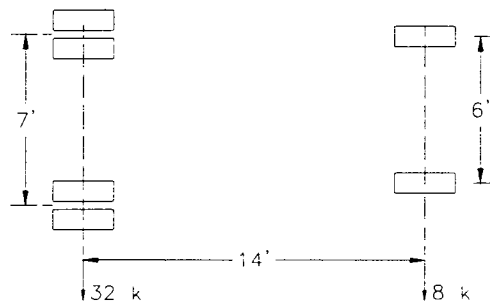
After an accurate model has been created (through appropriate optimization), rating trucks, such as HS-20, HS-20 (30), H-20 or Type-3 (shown in Fig. 3.8), are idealized with appropriate critical load paths to induce maximum live load. Capacities, typically calculated according to AASHTO Standard Specifications (4), are input into WinGEN. Next one needs only to compute the loads on the desired sections by applying dead load and live load from the rating trucks and associated paths, on the structure. Typical screen shots from WinGEN are shown in Fig. 3.9.



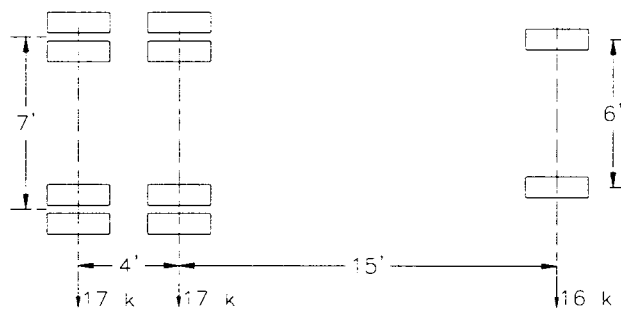
a. Design truck HS-20



b. Design truck HS-20 (30)

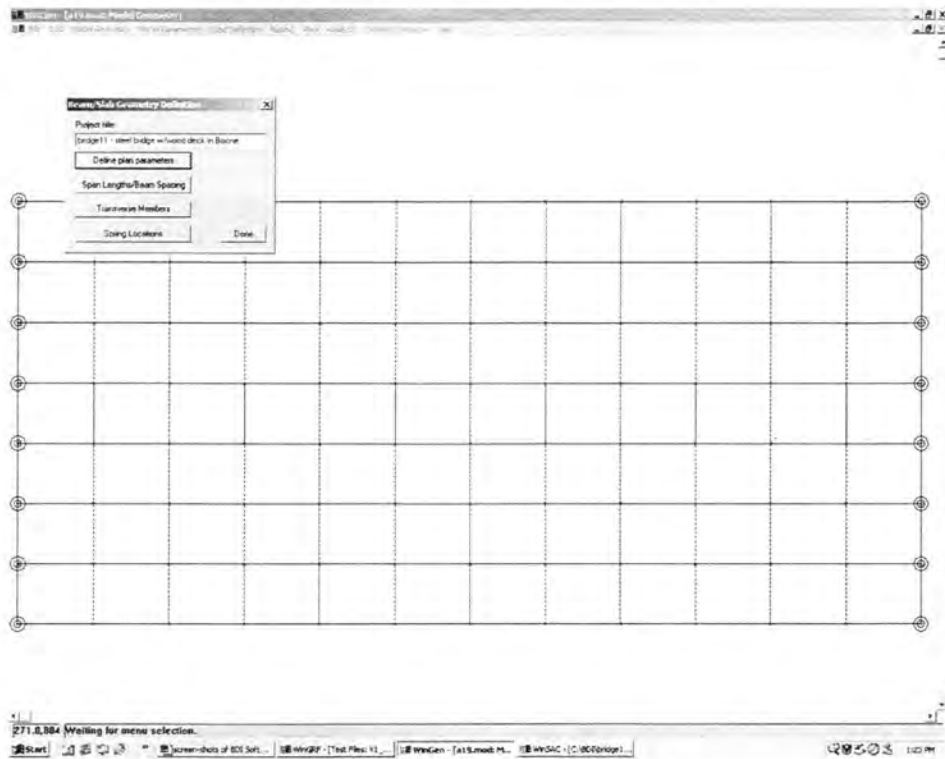


c. Design truck H-20

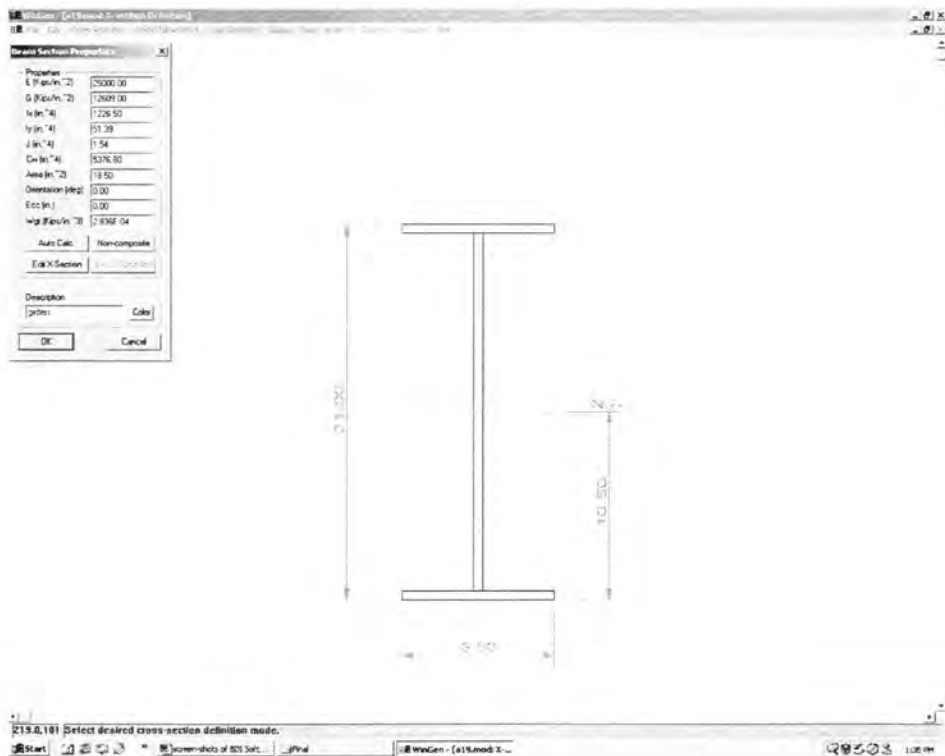


d. Design truck Type-3

Figure 3.8. Typical Rating Truck Details.



a. Plan view of analytical model.



b. "Construction" of a cross-section parameter.

Figure 3.9. Typical screen-shots of WinGEN.

3.3.3. Structural Analysis and Correlation (WinSAC)

After a model has been created in WinGEN, the WinGEN output file will be used in WinSAC. WinSAC performs analytical calculations and also constructs iterative analytical solutions by changing user defined optimization parameters within user defined boundaries. The resulting model, in the best way possible, represents the actual bridge behavior given user entered constraints. Typical variables chosen as optimization parameters are beam moments of inertia, modulus of elasticity of slabs, and rotational restraint at the abutments. The user sets the appropriate boundaries, so that the final optimized variables are within reasonable values. Usually, the lower limit for moment of inertias are set to 80 % of the non-composite value of the sections, and the upper limit set to 120 % of the composite values. Typically, there is no lower limit for the moment of elasticity for the slabs, but the upper limit may vary depending on the type of slab. The rotational restraints do not need explicit boundaries since zero represents a simply supported condition and infinity represents a fixed condition. Analytical accuracy is reported in terms of total error, percent error, percent scale error, and correlation coefficient, where the definitions of these variables have been discussed in Chp. 2. Equations for calculating the error functions where m represents measured strains, c represents calculated strains, and n represents the total number of strain computations are given in Table 3.1. In WinSAC, the percent error is considered to be the optimization objective function.

As mentioned previously, WinSAC performs multiple iterations, which includes a statistical analysis of the model where analytical strains are compared to the measured strains. Each iteration consists of N sub-iterations where N is the number of user-defined optimization parameters. Basically, WinSAC changes one optimization parameter per sub-iteration within the user-defined boundaries to establish the model accuracy sensitivity for that particular parameter. After all sub-iterations are completed and the model accuracies for all parameters have been established, WinSAC optimizes all parameters accordingly, and a new iteration begins, with updated section parameters. These iteration-loops (i.e., iterations and sub-iterations) continue until the percent error cannot be improved, and the optimization process is terminated with the percent error from the final iteration as the “lowest” error. The section parameters from the last iteration represent the optimized model. A “good” model will generally have a correlation coefficient greater than 0.90 and a percent error less than 10%. WinSAC results may be plotted with experimental results using WinGRF for a visual illustration of the model accuracy. Typical screen shots of WinSAC that illustrate the run time options and the iterations are shown in Fig. 3.10.

Table 3.1. Error functions and their corresponding equations.

Error Function	Equation
Absolute Error	$\sum_n \epsilon_m - \epsilon_c $
Percent Error	$\frac{\sum_n (\epsilon_m - \epsilon_c)^2}{\sum_n (\epsilon_m)^2}$
Scale Error	$\frac{\max_n \sum \epsilon_m - \epsilon_c }{\max_n \sum \epsilon_m }$
Correlation Coefficient	$\frac{\sum_n (\epsilon_m - \text{average}(\epsilon_m)) \cdot (\epsilon_c - \text{average}(\epsilon_c))}{\sum_n \sqrt{(\epsilon_m - \text{average}(\epsilon_m))^2 \cdot (\epsilon_c - \text{average}(\epsilon_c))^2}}$

* See Manual (*)

4. BRIDGE DESCRIPTION AND EXPERIMENTAL PROGRAM

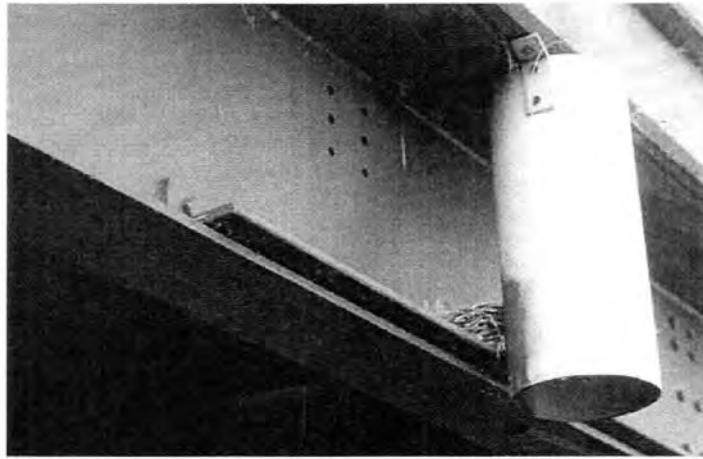
To complete the requirements of this project, seven bridges were tested, analyzed, and rated for purposes of evaluating the applicability and use of the BDI system. In addition, a bridge that had been previously tested and analyzed, was modeled to verify the procedures used herein. The following sections describe the bridges and the experimental program followed.

4.1. CEDAR CREEK BRIDGE: MODEL VERIFICATION

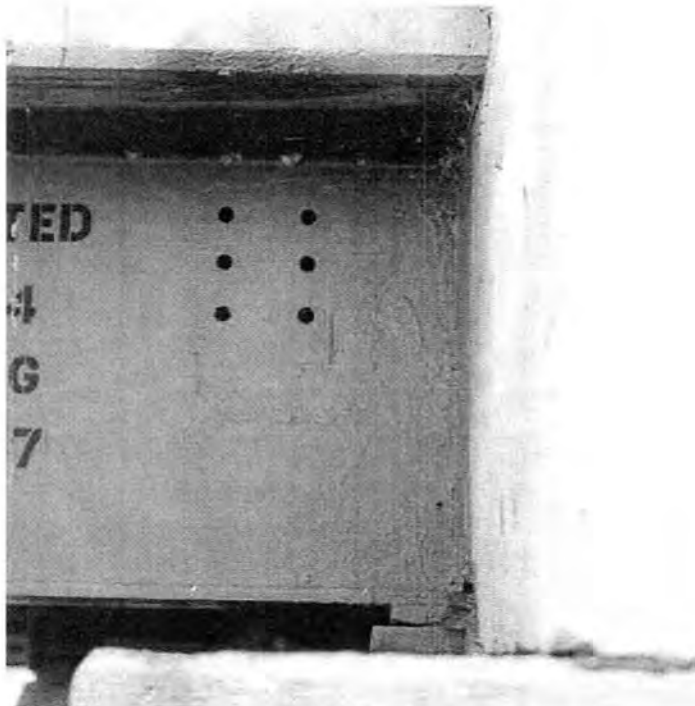
In an attempt to verify that the modeling process used herein was correct, data files and geometric information from a bridge previously investigated by BDI were used to generate analysis results. These results were then compared with results generated by BDI. The bridge used in this verification was Bridge 7601.2S003, a simple-span, composite steel-girder bridge with no skew carrying IA3 over Cedar Creek in Pocahontas County, IA. Based on photographic documentation provided by BDI (see Fig. 4.1) all elements of this bridge appear to be in good condition. As can be seen in Fig. 4.1b, it was anticipated that the bridge would exhibit significant end restraint as the beams appear to be integral with the abutments. This bridge, shown in plan view in Fig. 4.2 and in cross-section in Fig. 4.3, has a span length of 41 ft – 3 in. from centerline to centerline of bearings with a roadway width of 30 ft and an overall width of 32 ft (two 12 ft traffic lanes and two 3 ft shoulders). For reference, BDI submitted the results for this bridge in a report entitled “Load Testing and Load Rating Eight State Highway Bridges in Iowa” to the Iowa Department of Transportation in November 1999 (9).

The deck consists of a Portland Cement (P.C.) overlay and a reinforced concrete-slab deck slightly arched in a parabolic curve with an average thickness of 8.29 in. The superstructure is comprised of two exterior and two interior girders (primary members) and two diaphragm lines (secondary members). The substructure is a reinforced concrete abutment with fixed steel bearings and a reinforced-concrete backwall (shown in Fig. 4.1b). The exterior girders (shown in Figs. 4.4a and 4.4b) consist of two different sections. Over the center 26 ft – 11 in. there is an angle bolted to the outside of the web and a cover-plate welded to the bottom flange. The interior girders (shown in Figs. 4.4c and 4.4d) also consist of two different sections; the section at midspan includes a 26 ft – 11 in. long cover-plate. All girders were instrumented at sections 2 ft from the abutment centerline and at midspan as shown in Fig. 4.2. Each instrumented section had a gage installed on the bottom surface of the top and bottom flanges as shown in Fig. 4.4 (six gages were installed on each girder for a total of 24 gages on the bridge).

A loaded tandem-axle dump truck with a total weight of 50.72 k was used in the tests. Details for the load truck are given in Fig. 4.5. Data were collected for the two truck paths shown in Fig. 4.2 with two runs conducted for each path. Path Y1 was oriented such that the driver's side wheel line was 11 ft – 5 in. from the South girder, while path Y2 had the driver's side wheel line 25 ft – 3 in. from the South girder.

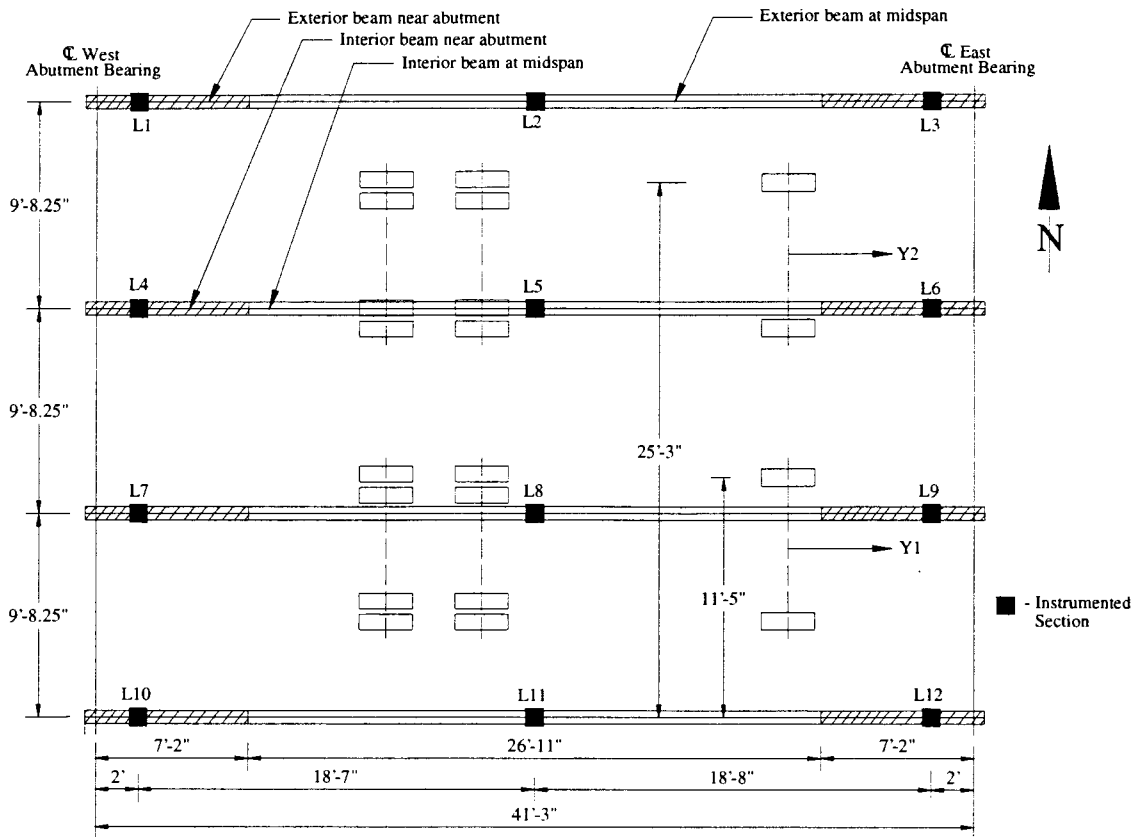


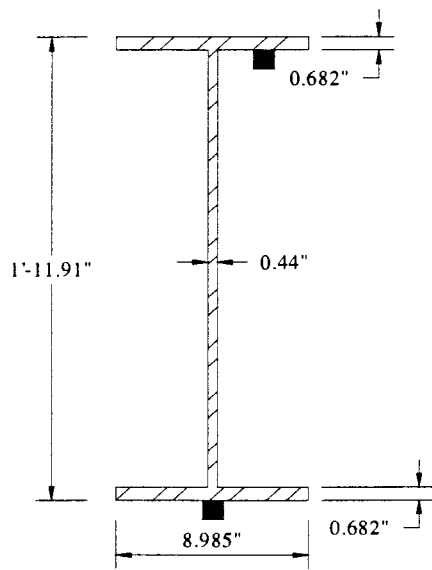
a. Exterior beam at midspan.



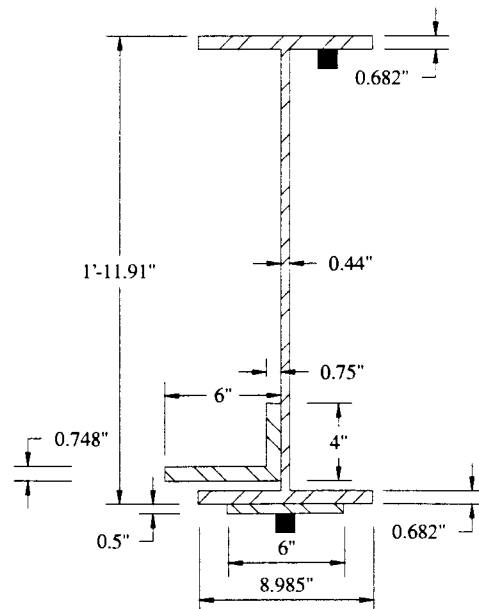
b. Abutment.

Figure 4.1. Cedar Creek Bridge: Photographs provided by BDI .

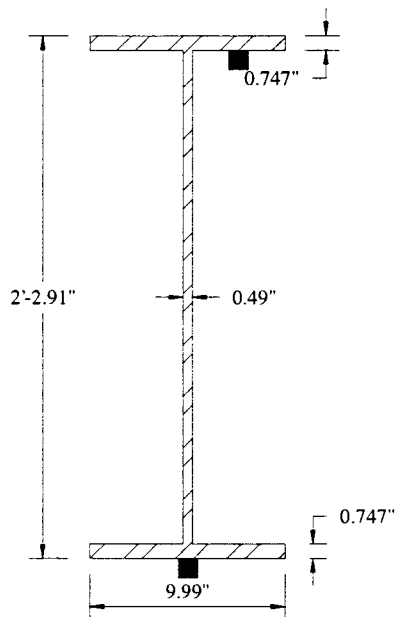




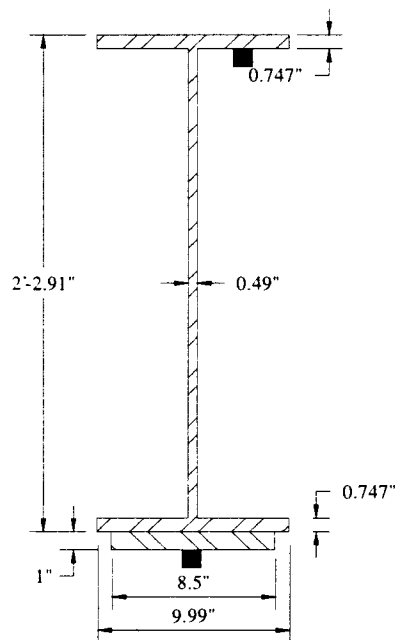
a. Exterior girder near abutment.



b. Exterior girder at midspan.



c. Interior girder near abutment.



d. Interior girder at midspan.

Figure 4.4. Cedar Creek Bridge: Girder cross-sections.

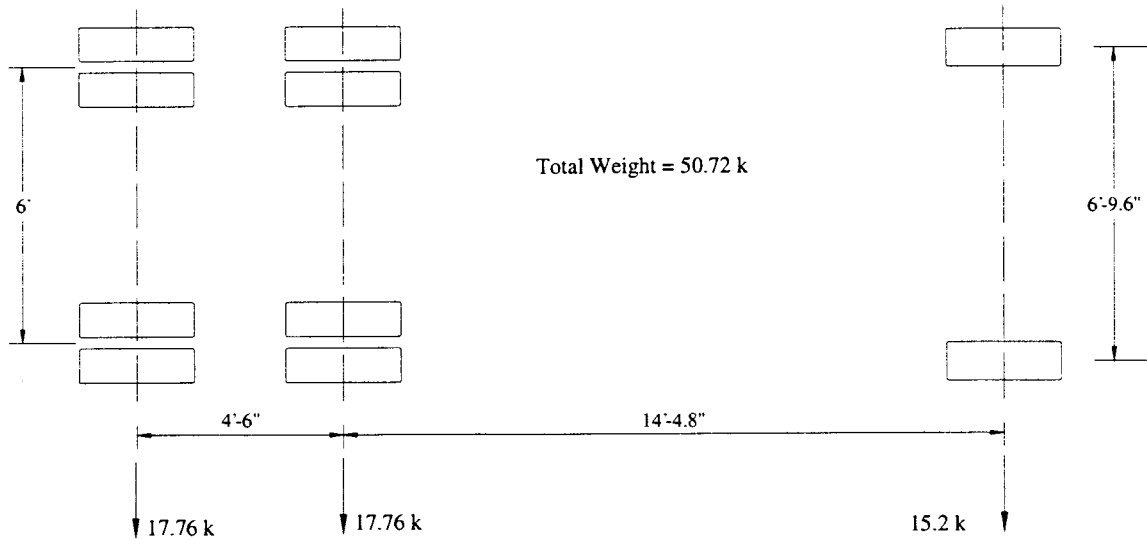


Figure 4.5. Cedar Creek Bridge: Load Truck Details.

4.2. BRIDGE #1

Bridge #1, Boone County Bridge #99, located in western Boone County, IA, is a non-composite, simple-span, steel-girder bridge with a timber deck and no skew carrying 230th Street over a small stream (half a mile East of D. Ave.). Based on a cursory visual inspection and photographic documentation (shown in Fig. 4.6), all steel-girders and the timber deck appear to be in good condition. As can be seen in Fig. 4.6a, it was anticipated that the bridge would not exhibit significant end restraint as the beams are not integral with the abutments. This bridge, shown in plan view in Fig. 4.7 and in cross-section in Fig. 4.8, has a span length of 44 ft – 8 in. from centerline to centerline of abutment bearings with a roadway width of 19 ft and an overall width of 19 ft – 8 in. (one 12 ft traffic lane and two 3 ft – 6 in. shoulders).

The timber deck consists of a 4-in. thick wood plank system with a 1-in. asphalt overlay without structural connection to the girders. In addition, there is a 3-in. gravel overlay on top of the asphalt. The superstructure is comprised of eight girders and four lines of diaphragms bolted to the girders. The substructure consists of expansion bearings and timber backwalls. The exterior beams and the six interior beams are the same size and are spaced on 2 ft – 6.25 in. centers. Six of the eight girders were instrumented near the East abutment and at midspan as shown in Fig. 4.7b. Each instrumented section had a gage installed on the bottom surface at the top and bottom flanges as previously described for Cedar Creek Bridge shown in Fig. 4.4, so that a total of 24 gages were installed at 12 locations.

A loaded tandem-axle dump truck with a total weight of 49.58 k was used in the tests. Details of the truck are given in Fig. 4.9. Data were collected for three truck paths with two runs conducted for each path. Path Y1 was oriented such that the driver's side wheel line was 8 ft – 10 in. from the South girder (with the outer wheel line placed 2 ft from the centerline of the South girder), and path Y2 positioned the truck approximately over the center of the bridge with the driver's side wheel line 12 ft – 8 in. from the South girder. Finally, path Y3 was oriented with the driver's side wheel line 15 ft – 6 in. from the South girder (the outer wheel line was placed 2 ft from the North girder). Truck path information and gage locations are presented in Fig. 4.7.



a. Abutment.

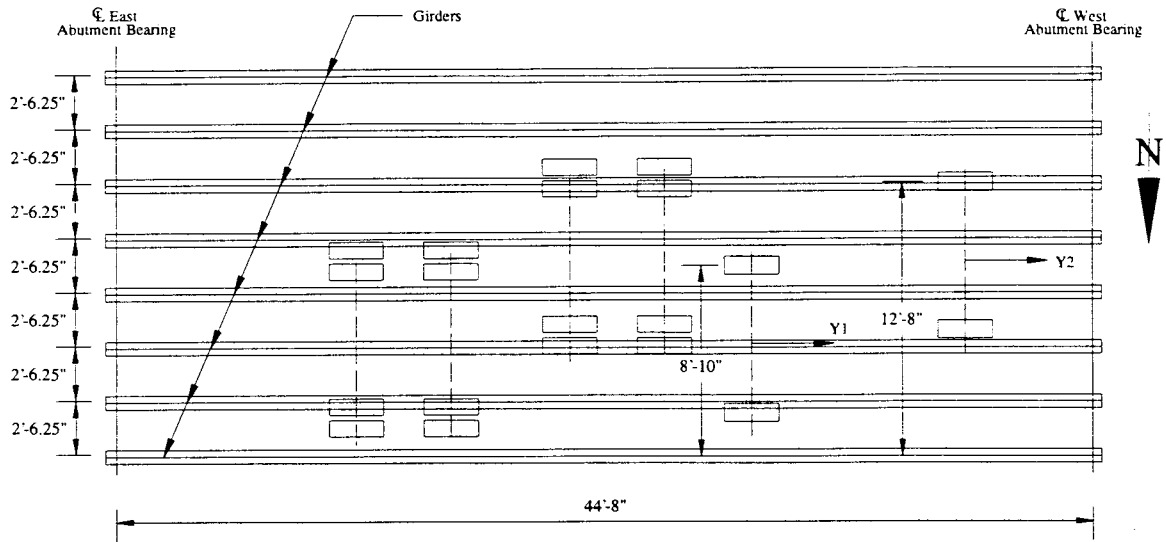


b. Girders and the West side of abutment.

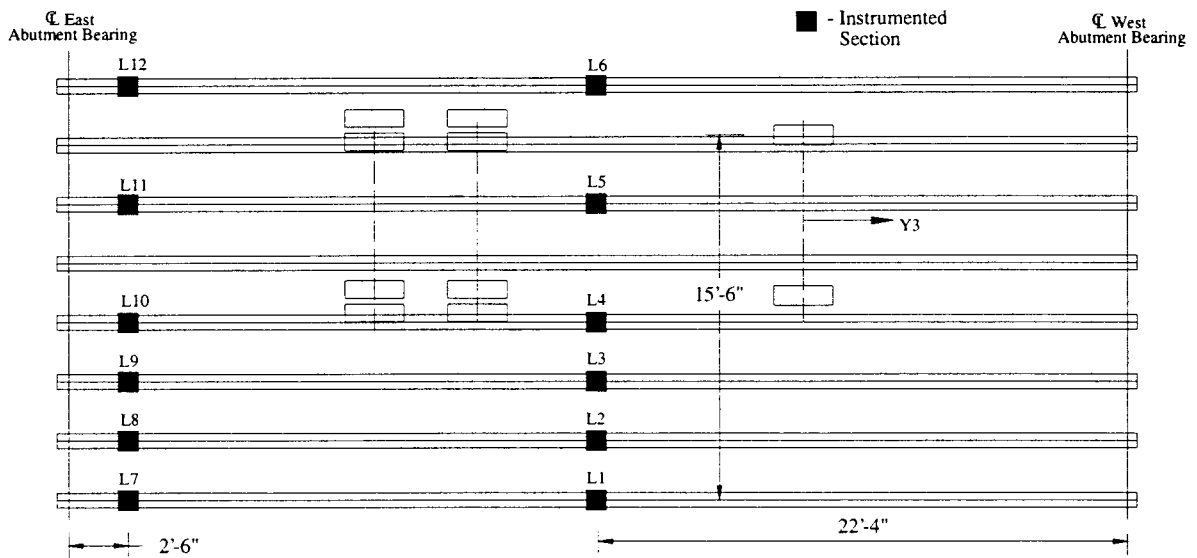


c. End view of bridge.

Figure 4.6. Photographs of Bridge #1.

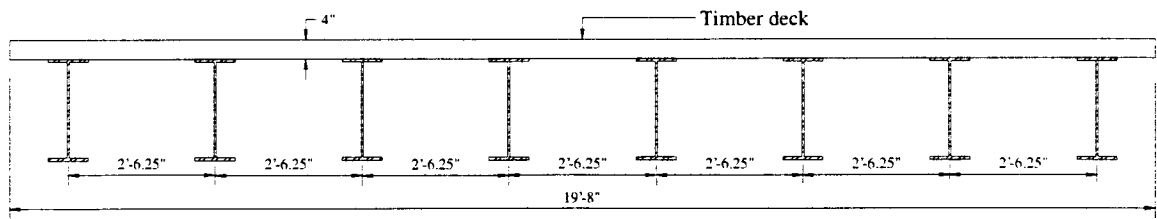


a. Overall dimensions and truck paths Y2 and Y3.

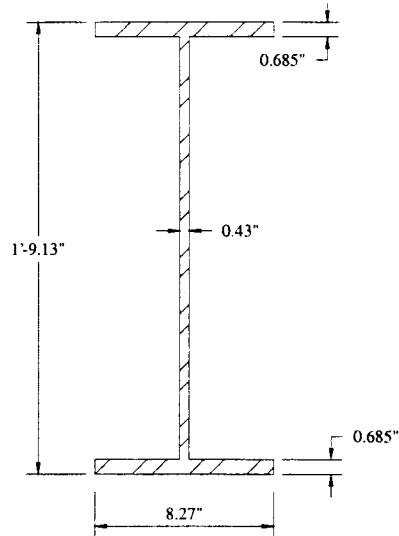


b. Truck path Y3 and gage locations.

Figure 4.7. Bridge #1: Overall bridge dimensions, gage locations, and truck paths.



a. Cross-section of the bridge.



b. Cross-section of a girder.

Figure 4.8. Bridge #1: Cross-sections of the bridge and individual girder.

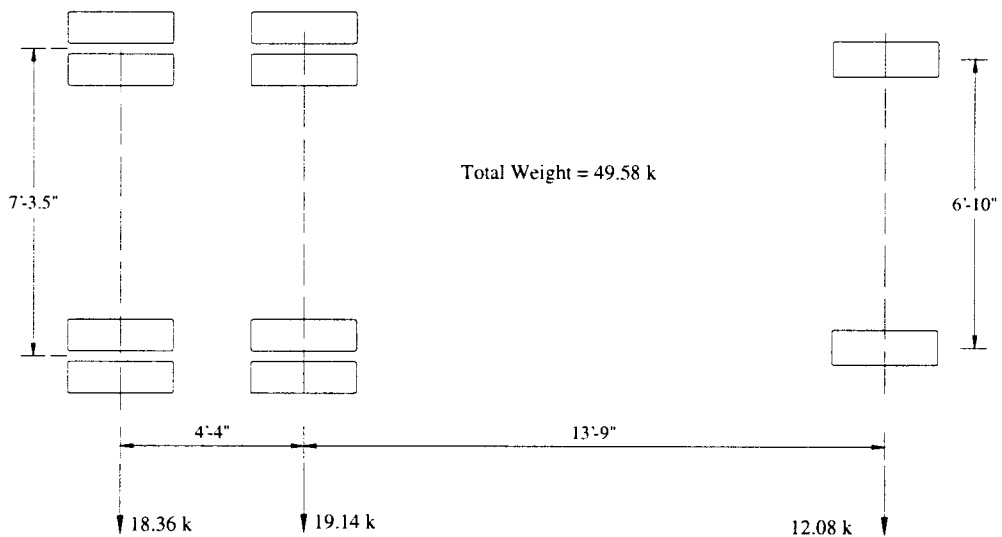


Figure 4.9. Bridge #1: Load Truck Details.

4.3. BRIDGE #2

Bridge #2, Boone County Bridge #11, located in northern Boone County, IA, is a non-composite, simple-span, steel-girder bridge with a timber deck and no skew carrying L Rd. over a small stream one mile North of 130th Street. Based on a cursory visual inspection and photographic documentation, all steel-girders except one appeared to be, with the exception of some light rust, in good condition. The girder on the far West side was bent at midspan (possibly hit by a large object during a flood). The timber deck is in good condition. Photographs of the bridge including the damaged girder are illustrated in Fig. 4.10, where Fig. 4.10a shows the damaged girder section at midspan, Fig. 4.10b illustrates the superstructure system at midspan, and Fig. 4.10c shows the end view of the bridge. It was anticipated that the bridge would not exhibit significant end restraint as the beams are not integral with the abutments (the same conditions at the abutments as for Bridge #1 as shown previously in Fig. 4.6a). This bridge, shown in plan view in Fig. 4.11 and in cross-section in Fig. 4.12, has a span length of 38 ft – 10 in from centerline to centerline of bearings with a roadway width of 17 ft and an overall width of 19 ft – 9 in. (one 12 ft traffic lane and two 2 ft – 6 in. shoulders).

The timber deck consists of a 4-in. thick wood plank system with a 6-in. gravel overlay without structural connection to the girders. The superstructure is comprised of eight girders and four lines of diaphragms bolted to the girders. The substructure consists of expansion bearings and timber backwalls. The exterior beams and the six interior beams are the same size and are spaced on 2 ft – 6 3/8 in. centers. Four of the eight girders were instrumented near the abutments, at midspan, and at quarterspan near the North abutment as shown in Fig. 4.11b. Two of the remaining four girders were instrumented near the North abutment and at midspan also shown in Fig. 4.11b. Each instrumented sections had a gage installed on the bottom surface of the top and bottom flanges as previously described such that a total of 40 gages were installed at 20 locations.

A loaded tandem-axle dump truck with a total weight of 49.58 k was used in the tests. Details for the truck are given in Fig. 4.13. Data were collected for three truck paths with two runs conducted for each path. Path Y1 was oriented such that the driver's side wheel line was 8 ft – 11 in. from the far East girder (with the outer wheel line placed 2 ft from the centerline of the East girder), and path Y2 positioned the truck approximately over the center of the bridge with the driver's side wheel line 11 ft – 11 in. from the East girder. Finally, path Y3 was oriented with the driver's side wheel line 15 ft – 8 in. from the East girder (the outer wheel line was placed 2 ft from the West girder). Truck path information and gage locations are summarized in Fig. 4.11.



a. Bent girder on far West side at midspan.

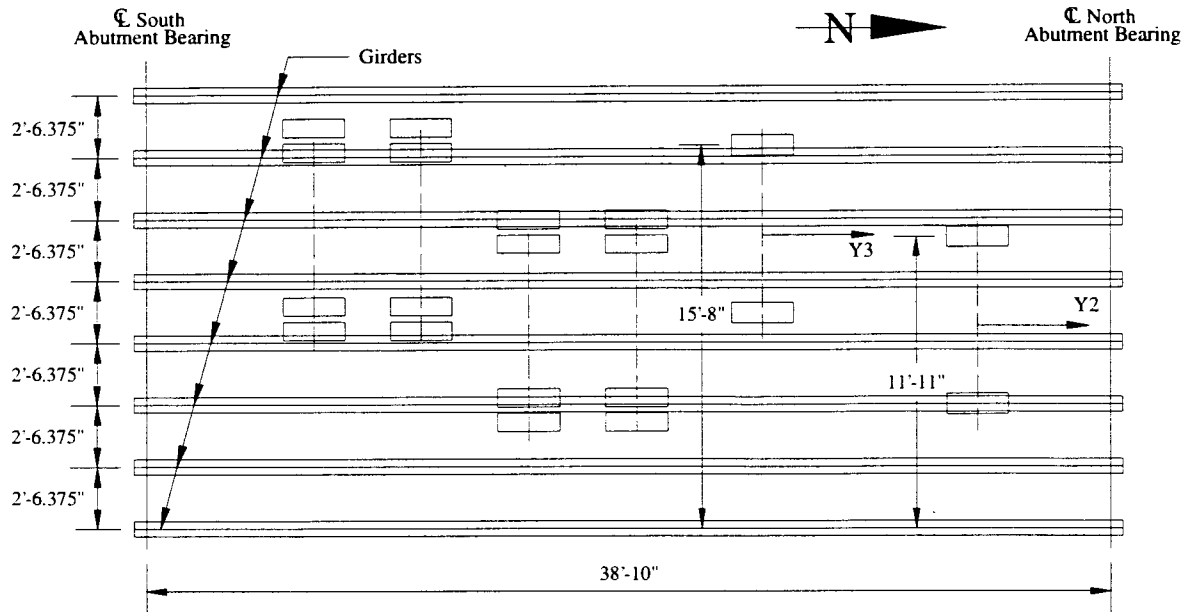


b. Girders on East side at midspan.

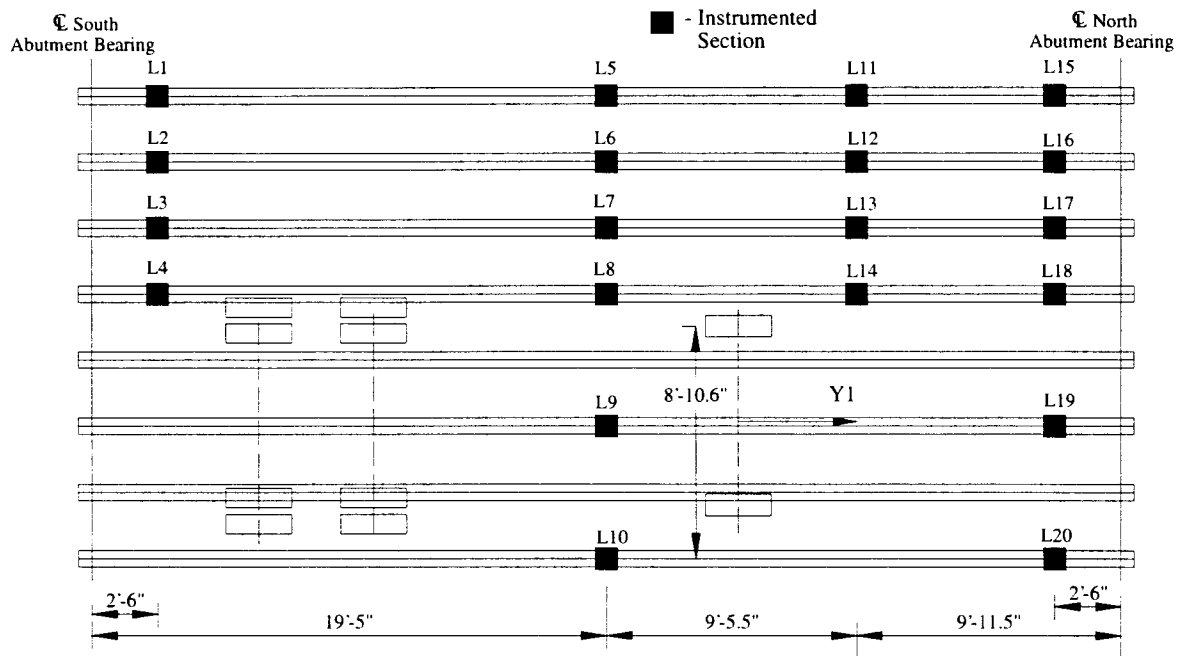


c. End view of the bridge.

Figure 4.10. Bridge #2: Photographs of the bridge.

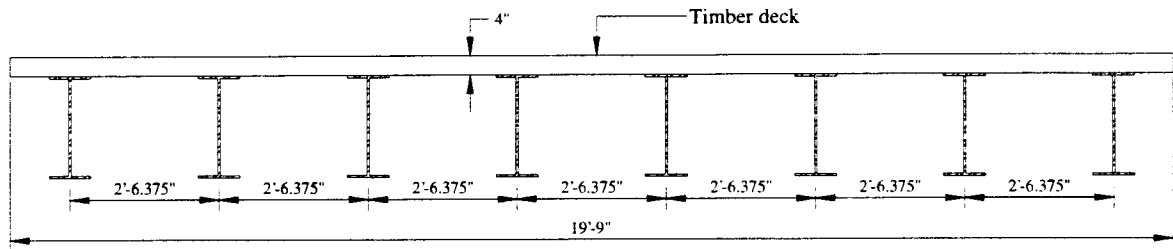


a. Overall bridge dimensions and truck paths Y2 and Y3.

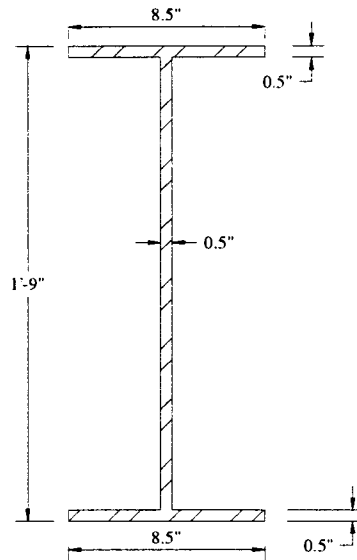


b. Truck path Y1 and gage locations.

Figure 4.11. Bridge 2: Overall dimensions, gage locations, and truck paths.



a. Cross-section of the bridge.



b. Cross-section of the girder.

Figure 4.12. Bridge #2: Cross-sections of the bridge and individual girder.

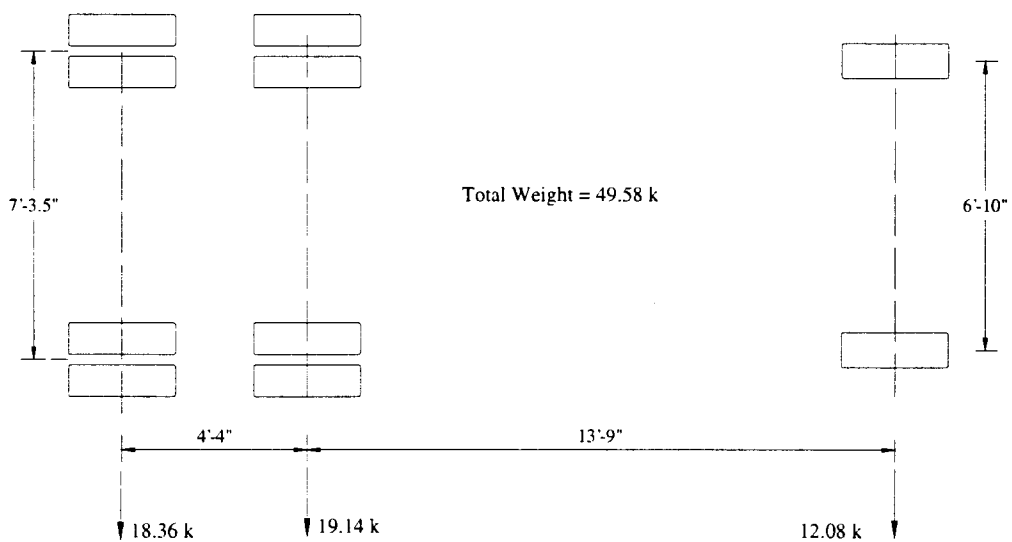


Figure 4.13. Bridge #2: Load Truck Details.

4.4. BRIDGE #3

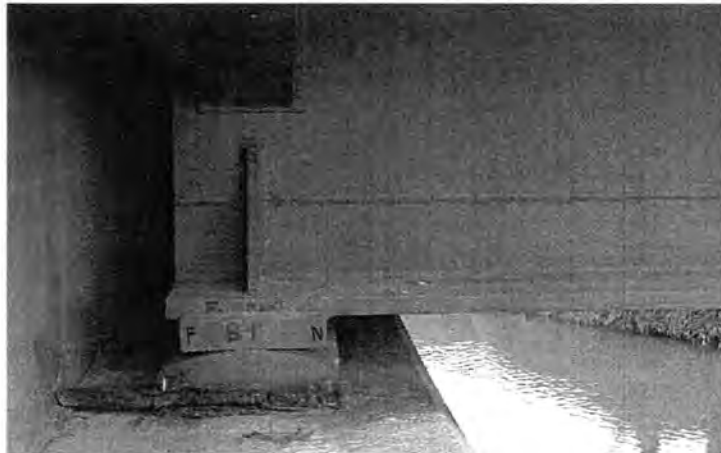
Bridge #3, Iowa DOT Bridge Number 4824.1S 006 located in Iowa County, IA and built in 1929, is a composite, simple-span, steel-girder bridge with a concrete deck and no skew carrying US Highway 6 over a small natural stream. Based on a cursory visual inspection and photographic documentation, all steel sections appear to be in good condition with the exception of some light rust. As can be seen in Fig. 4.14b, it was anticipated that the bridge would not exhibit significant end restraint as the beams are not integral with the abutments. This bridge, shown in plan view in Fig. 4.15 and in cross-section in Fig. 4.16, has a span length of 70 ft from centerline to centerline of abutment bearings with a roadway width of 29 ft – 6 in. (two 12 ft lanes and two 2 ft – 9 in. shoulders).

The deck consists of a reinforced concrete-slab deck with a variable thickness (7 in. at the curb and 9 in. at the centerline), cast-in-place reinforced concrete-slab with a 3-in wearing surface. The superstructure is comprised of two exterior beams (on 31 ft centers), two main girders (on 21 ft – 9 in. centers), four interior stringers (on 4 ft centers), and six floor beams (see Fig. 4.15a for the spacing). As shown in Fig. 4.14c, a non-uniform steel section connects to the exterior beams to the main girders. The substructure is a reinforced-concrete abutment with expansion steel bearings and a reinforced-concrete wingwall. The four interior stringers consist of two different sections: the first section is bolted to the floor beams that are spaced 8 ft – 9 in., and the second section is bolted to the floor beams that are spaced 17 ft – 6 in. The exterior beams also consist of two different sections (shown in Fig. 4.14c): the first section is bolted to the non-uniform members that are spaced 8 ft – 9 in., and the second section is bolted to the non-uniform members that are spaced 17 ft – 6 in. The main girders are 41.38 in. deep and have various cover plates and 2 angles 8 in. x 3 in. x 1 in. attached. The angles are bolted in place (see Fig. 4.14c) over the middle 60 ft. The longest cover plate (welded to the bottom flange) is 14 in. x 1 in. x 45 ft long centered on the bridge. The second cover plate is 12 in. x 5/8 in. x 27 ft long centered on the bridge. A cross-section of the main girder near midspan is presented in Fig. 4.16b. Gages were installed at various critical locations: ten gage pairs were placed on the main girders, three gage pairs were placed on one of the stringers, and three gage pairs were placed on one of the floor beams. At all instrumented sections, gages were positioned on the bottom surface of the top and bottom flanges as previously described. In addition, one extra gage was installed on the top surface (bottom flange) of the angle (shown in Fig. 4.16a) at locations L3, L5 and L7 to determine the effectiveness of the angle. Gage locations are illustrated in Fig. 4.15; there are a total of 16 instrumented sections and 35 gages.

A loaded tandem-axle dump truck with a total weight of 49.4 k was used in the tests. Details of the load truck are given in Fig. 4.17. Data were collected for the five truck paths shown in Fig. 4.15 with two runs conducted for each path. All truck paths were oriented with respect to the driver's side wheel line measured from the North girder: Path Y1 was located at 10 ft – 11 in. (with the passenger side wheel line approximately on the North girder), Path Y2 was located at 8 ft – 8 in. (with the passenger side wheel line 2 ft from the North curb), Path Y3 was located at 16 ft – 2 in. (with the passenger side wheel line approximately on one of the interior stringers), Path Y4 was located at 18 ft – 10 in. (with the truck approximately on the center of the bridge), and Path Y5 was located at 25 ft – 8 in (with the driver's side wheel line approximately on the South girder).

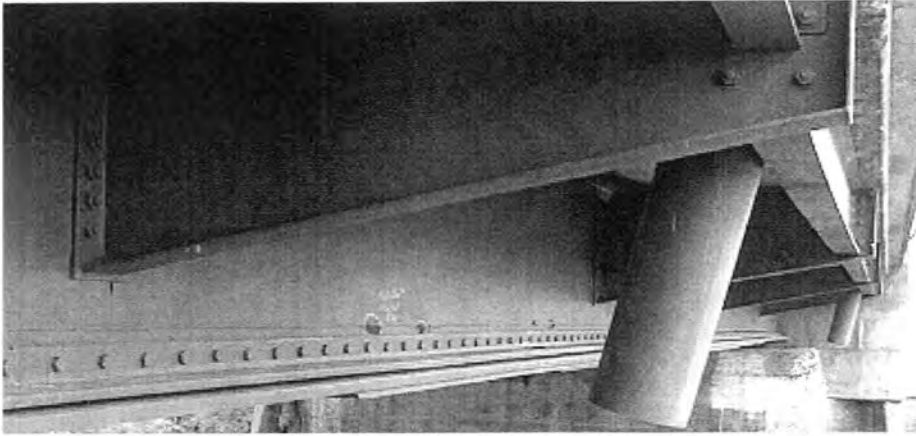


a. End view of bridge

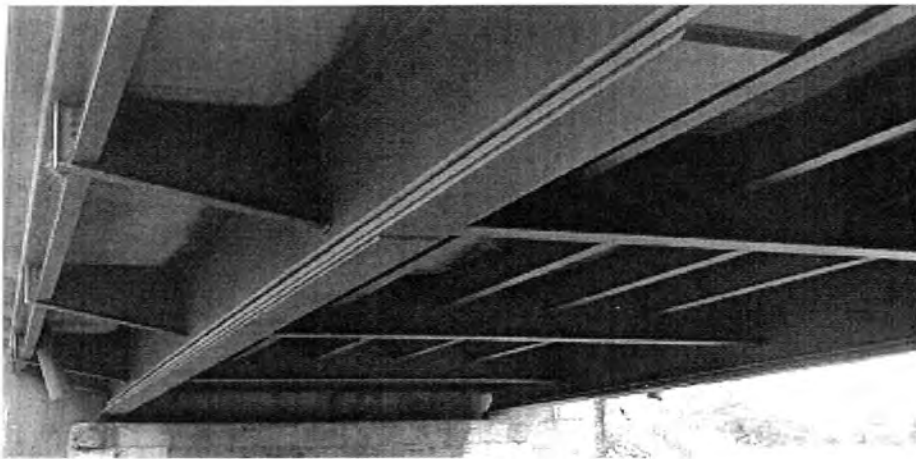


b. Abutment.

Figure 4.14. Bridge #3: Photographs of the bridge.



c. The non-uniform section bolted to the main girder.

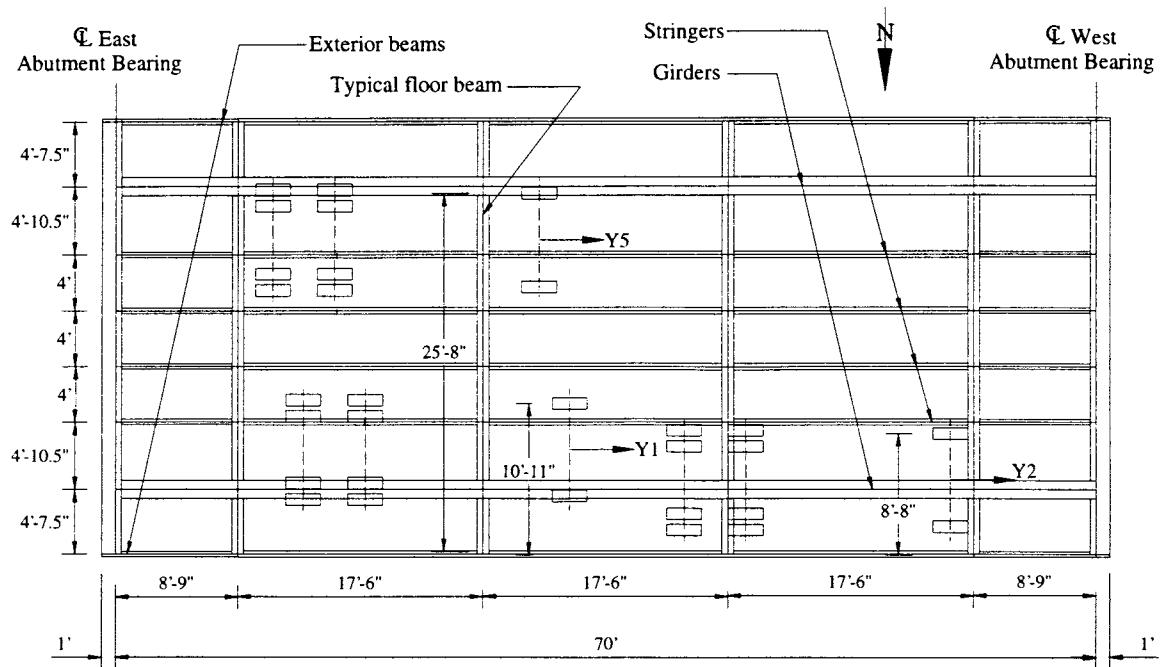


c. Superstructure system.

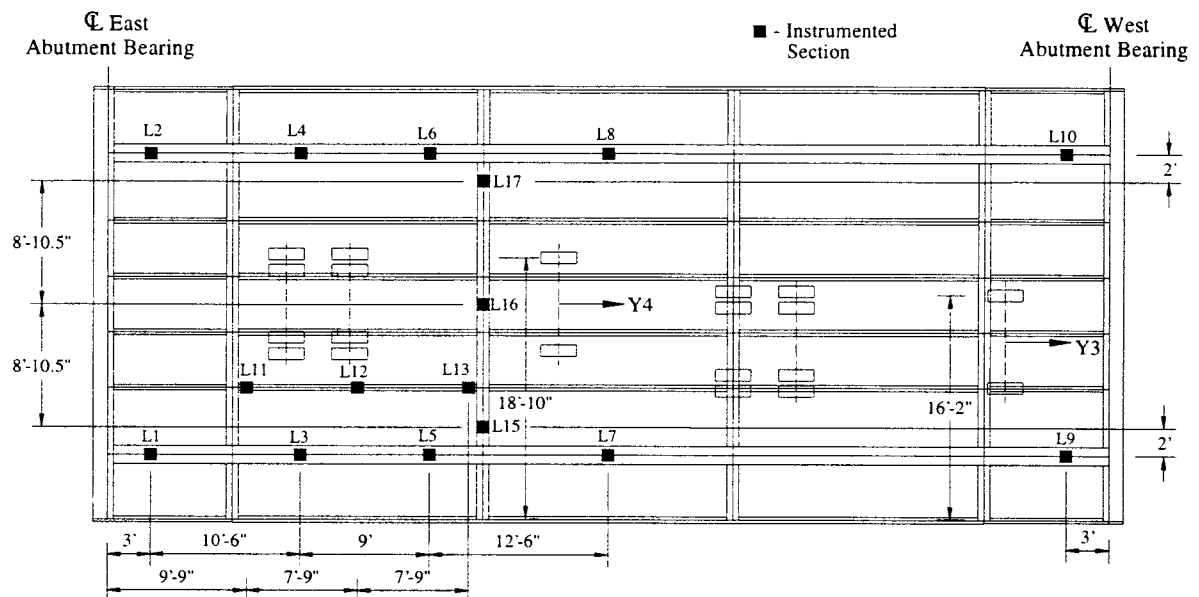


d. Side view of bridge.

Figure 4.14. Continued.

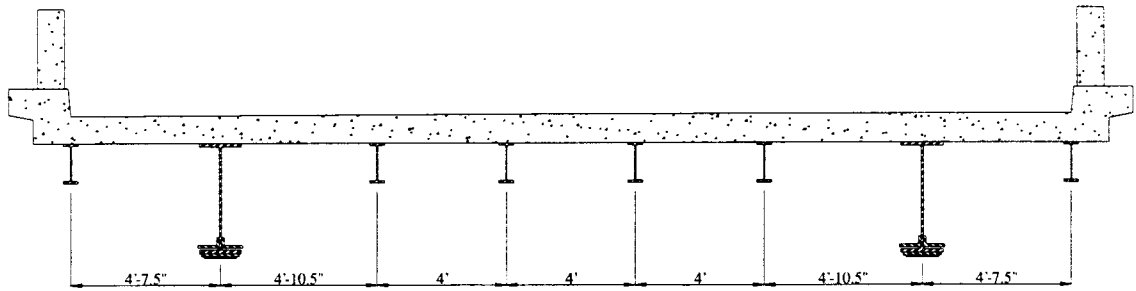


a. Overall dimensions and truck paths Y1, Y2 and Y5.

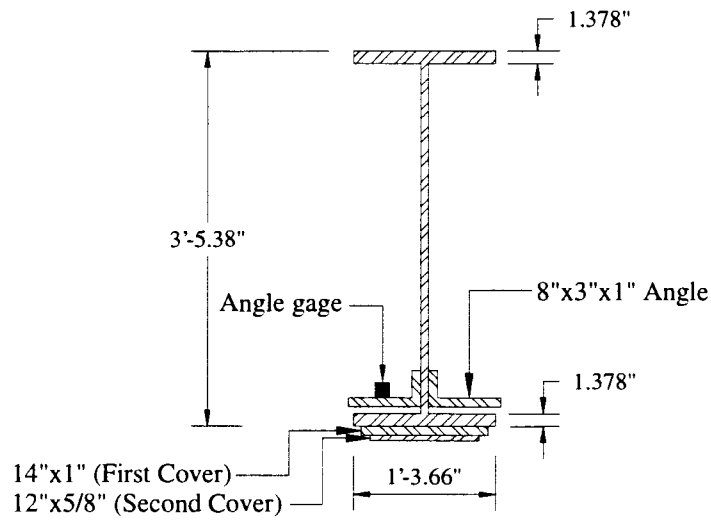


b. Gage Locations and truck paths Y3 and Y4.

Figure 4.15. Bridge #3: Overall dimensions, gage locations, and truck paths.



a. Cross-section of the bridge at midspan.



b. Cross-section of the main girder at midspan.

Figure 4.16. Bridge #3: Typical cross-sections of the bridge and the main girder at midspan.

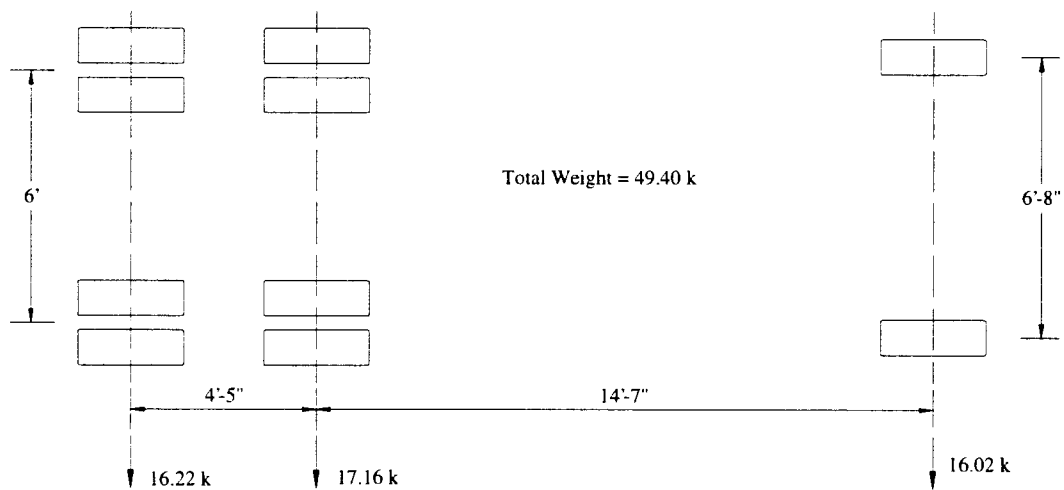


Figure 4.17. Bridge #3: Load Truck Details.

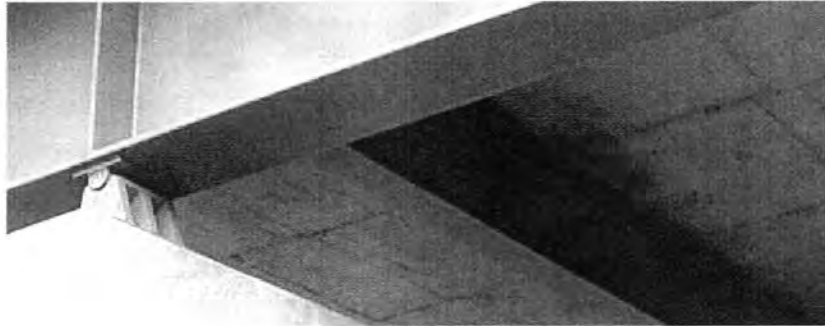
4.5. BRIDGE #4

Bridge #4, Iowa DOT Bridge Number 4821.90 080, located in Iowa County, IA, carries FM W-16 (2.1 miles East of Jct. 149) over Interstate 80. This bridge, which was built in 1963, is a no skew, composite, four-span, steel-girder bridge with a concrete deck. Based in visual inspection and photographic documentation, all structural elements appear to be in good condition (shown in Fig. 4.18). It was anticipated that the bridge would not exhibit significant end restraint as the beams are not integral with the abutments. Since this bridge is symmetric about the centerline, only half of this bridge is shown in plan view in Fig 4.19; a cross-section of the bridge is presented in Fig. 4.20. The total length of this bridge is 216 ft: Span 1 and Span 4 are 46 ft – 6 in. while Span 2 and Span 3 are 61 ft – 6 in. measured from centerline to centerline of bearings. This bridge has a roadway width of 24 ft and an overall width of 26 ft – 4 in. (two 12 ft traffic lanes and two 1 ft – 2 in. shoulders).

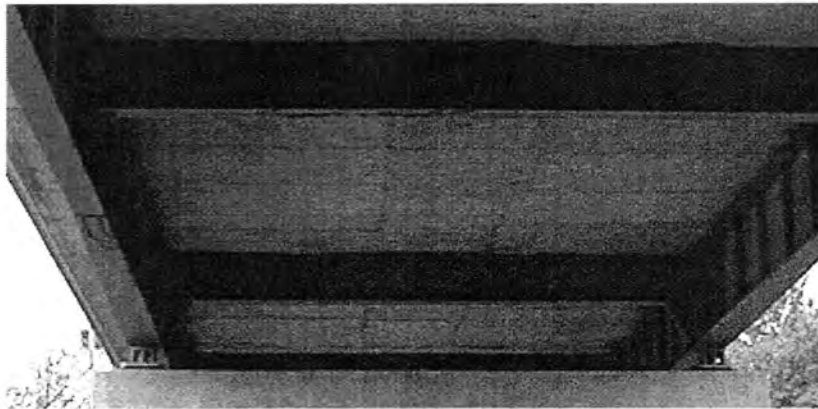
The deck consists of a variable thickness (i.e., 6 in. at the curb and 9 in. at the centerline) cast-in-place reinforced concrete-slab with a 1/2-in. wearing surface. The superstructure is comprised of two exterior girders (spaced 20 ft – 2 in. centers) and thirteen floor beams (spaced as illustrated in Fig. 4.19). The substructure is a reinforced-concrete abutment with steel expansion bearings at the abutments and at the piers, and a reinforced-concrete backwall. The girders consist of three different sections: one section near the abutments and in the vicinity of midspan (shown in Fig. 4.20d), one section at Pier 1 extending 9 ft to the South and 8 ft – 6 in. to the North of the pier (shown in Fig. 4.20e), and the third section at Pier 2 and extending 9 ft on both sides of the pier (shown in Fig. 4.20c). The floor beams consist of two different sections: one section aligned at centerline of the abutment bearings (18 WF 45 as shown in the Steel Manual (5)), and one section for all other floor beams (21 WF 55 as shown in Steel Manual (5)) and illustrated in Fig. 4.20b. All floor beams are bolted to the main girders. The girders were instrumented near the South abutment (4 gages), at midspan of Span 1 (4 gages), near Pier 1 (8 gages), at the midspan of Span 2 (4 gages) and on the South side of Pier 2 (4 gages). In addition, one of the floor beams was instrumented at 4 locations with 2 gages at each location. Top and bottom flanges were instrumented for all fifteen instrumented sections as previously described, thus, as shown in Fig. 4.19, there were a total of 32 gages on the bridge instrumented at 16 locations.

A loaded tandem-axle dump truck with a total weight of 47.72 k was used in the tests. Details for the load truck are given in Fig. 4.21. Data were collected for four truck paths as shown in Fig. 4.19. Path Y1 was oriented with the passenger's side wheel line side approximately over the East girder, Path Y2 was oriented with the passenger's side wheel line side approximately over the center of the bridge, Path Y3 was oriented with the truck positioned approximately over the center of the

bridge, and Path Y4 was oriented with the driver's side wheel line approximately over the West girder.



a. First pier.



b. Superstructure system.



c. Side view of bridge.



d. End view of bridge.

Figure 4.18. Bridge #4: Photographs of the bridge.

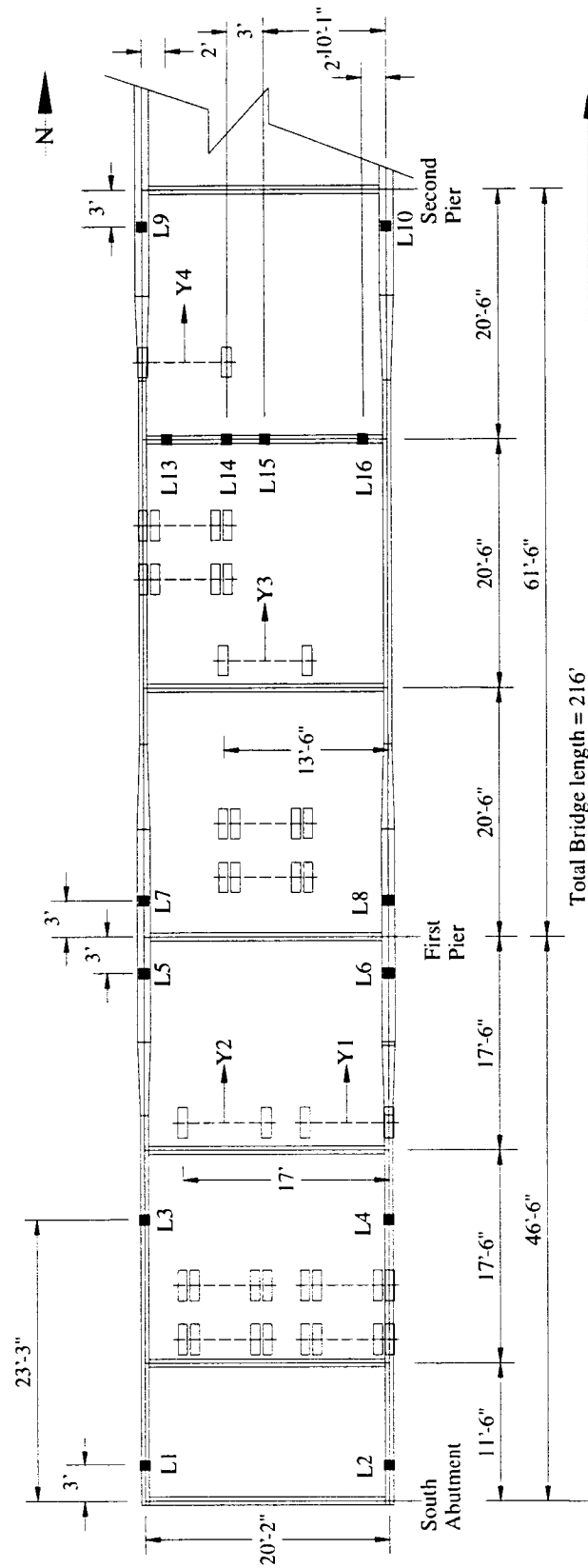
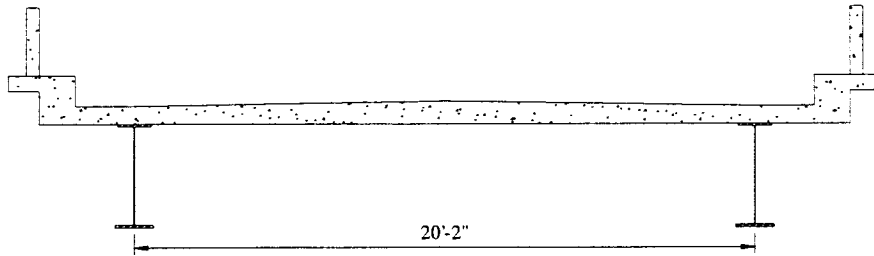
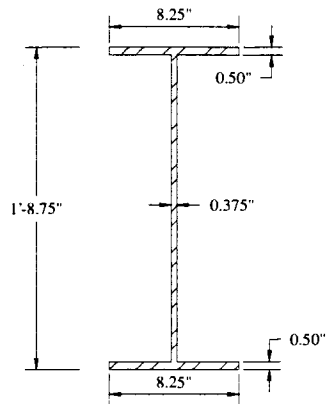


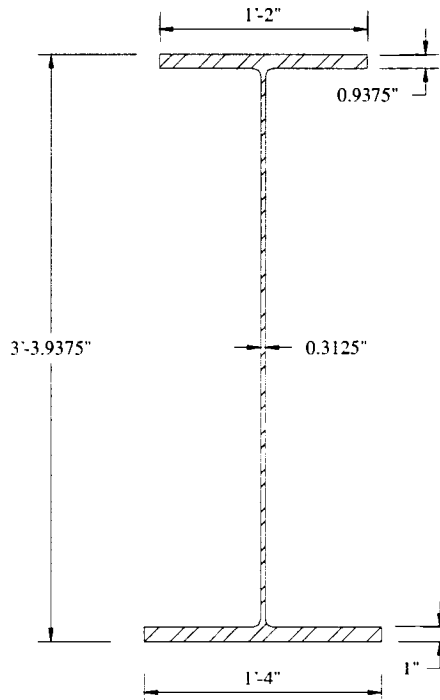
Figure 4.19. Bridge #4: Overall dimensions, gage locations, and truck paths.



a. Cross-section of the bridge at midspan.

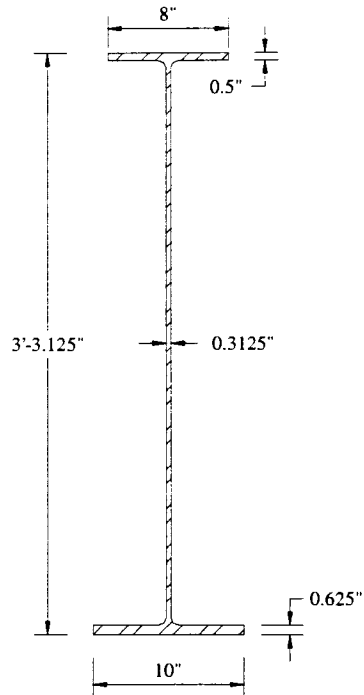


b. Cross-section of the floor beam: 21WF 55.

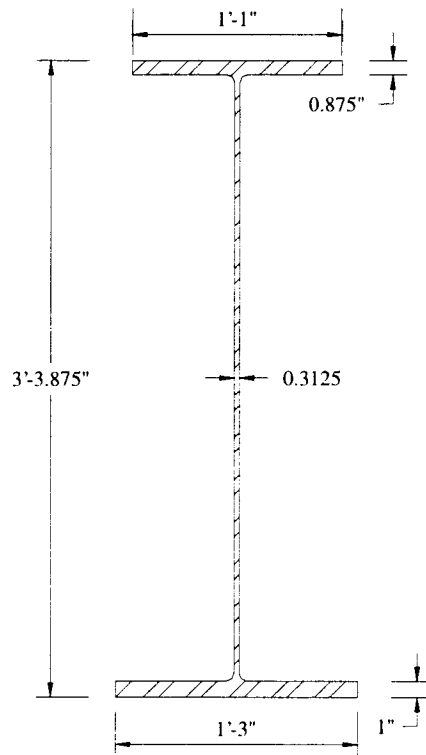


c. Cross-section of the girder at second pier.

Figure 4.20. Bridge #4: Typical cross-sections of the steel beams and the bridge.



d. Girder near the abutments and in the vicinity of midspan.



e. Girder at first pier.

Figure 4.20. Continued.

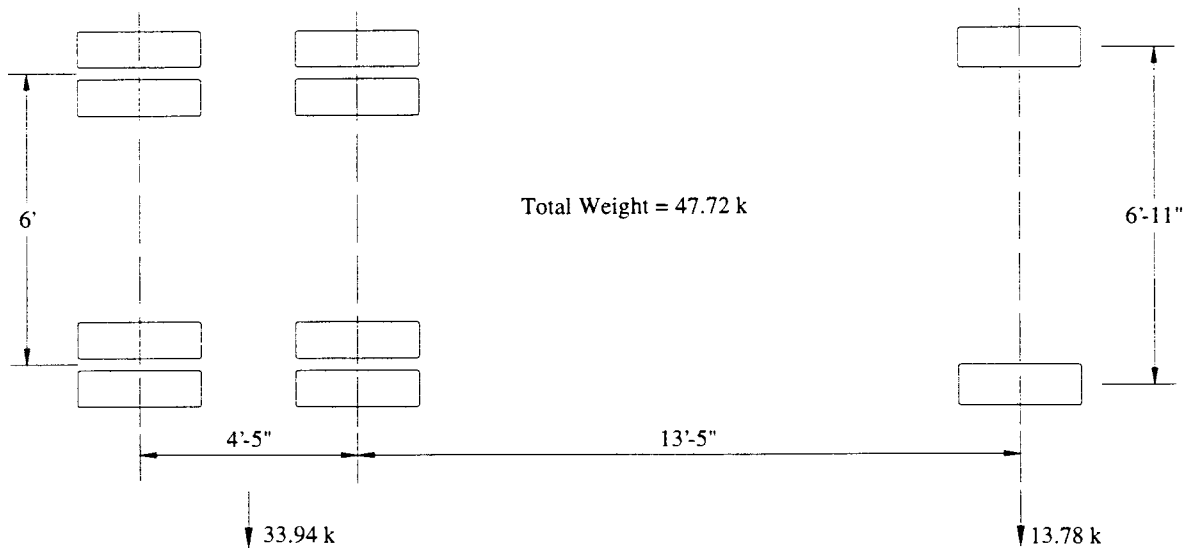


Figure 4.21. Bridge #4: Load Truck Details.

4.6. BRIDGE #5

Bridge #5, Iowa DOT Bridge Number 3150.7A 052, located in Dubuque County, IA is a non-composite, simple-span, steel-girder bridge with a concrete deck and no skew. This bridge, which was built in 1965, carries IA #386 (0.2 miles North of South Jct. US #52) over a drainage ditch. Based on a cursory visual inspection and photographic documentation, all steel sections appear to be in good condition with the exception of some small areas of corrosion on the girders (shown in Fig. 4.22d). The deck appears to be in good condition with the exception of some minor cracking (shown in Fig. 4.22e) and small spalled areas (shown in Fig. 4.22f). As can be seen in Fig. 4.22d, it was anticipated that the bridge would exhibit significant end restraint as the beams are integral with the abutments. This bridge, shown in plan view in Fig. 4.23 and in cross-section in Fig. 4.24, has a span length of 25 ft (clear span) between the abutments with a roadway width of 18 ft and an overall width of 19 ft – 8 in. (one 12 ft traffic lane and two 3 ft shoulders).

The deck consists of an 8-in. thick reinforced cast-in-place concrete-slab with an original 0.25-in. P.C. overlay and an additional 1.5-in. P.C. overlay that was placed in 1994 (see Fig. 4.24a). The superstructure is comprised of five girders and three diaphragm lines. The substructure is a reinforced-concrete abutment with fixed steel bearings and a reinforced-concrete backwall. Originally, the bridge only had four girders. However, it was widened in 1984 with a new girder added to the East side of the bridge. The new girder (shown in Fig. 4.24a) was tied in on the East side of the bridge with the construction joint shown in Fig. 4.24a. The cross-sections of the girders are

illustrated in Figs. 4.24b and 4.24c. All girders were instrumented 2 ft from the abutments and at midspan as shown in Fig. 4.23. Each instrumented section had a gage installed on the bottom surface of the top and bottom flanges.

A loaded tandem-axle dump truck with a total weight of 45.3 k was used in the tests. Details for the load truck are given in Fig. 4.25. Data were collected for the two truck paths shown in Fig. 4.23 with two runs conducted for each path. Path Y1 was oriented such that the driver's side wheel line was approximately over the center girder, while Path Y2 had the passenger's side wheel line over the center girder.

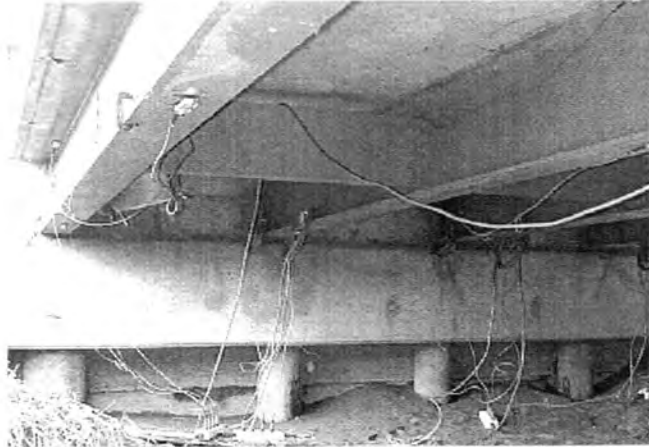


a. End view of bridge.

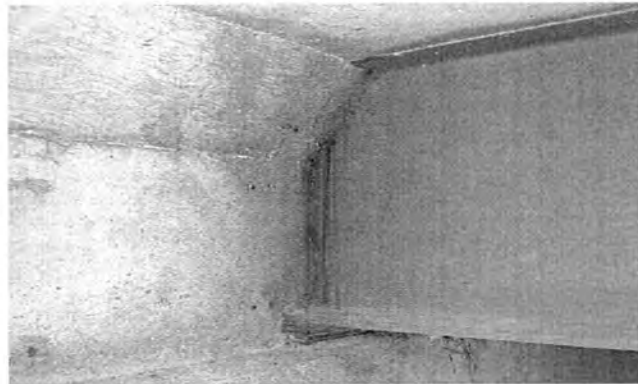


b. Side view of bridge

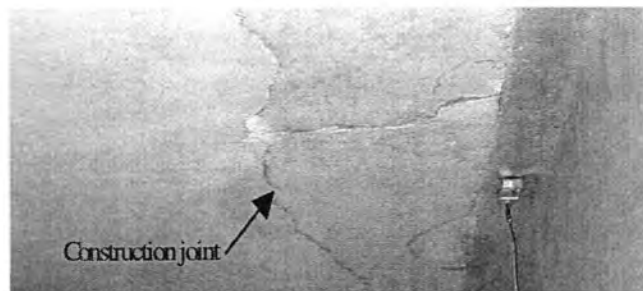
Figure 4.22. Bridge #5: Photographs of the bridge.



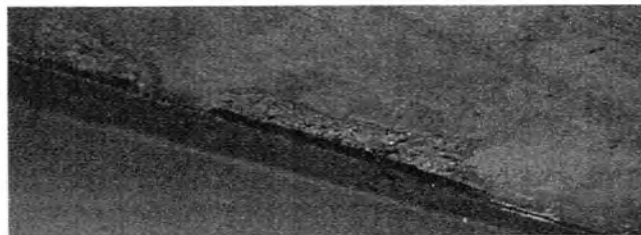
c. Abutment, superstructure system, and gage installation.



d. Abutment.



e. Concrete cracks.



f. Concrete deterioration.

Figure 4.22. Continued.

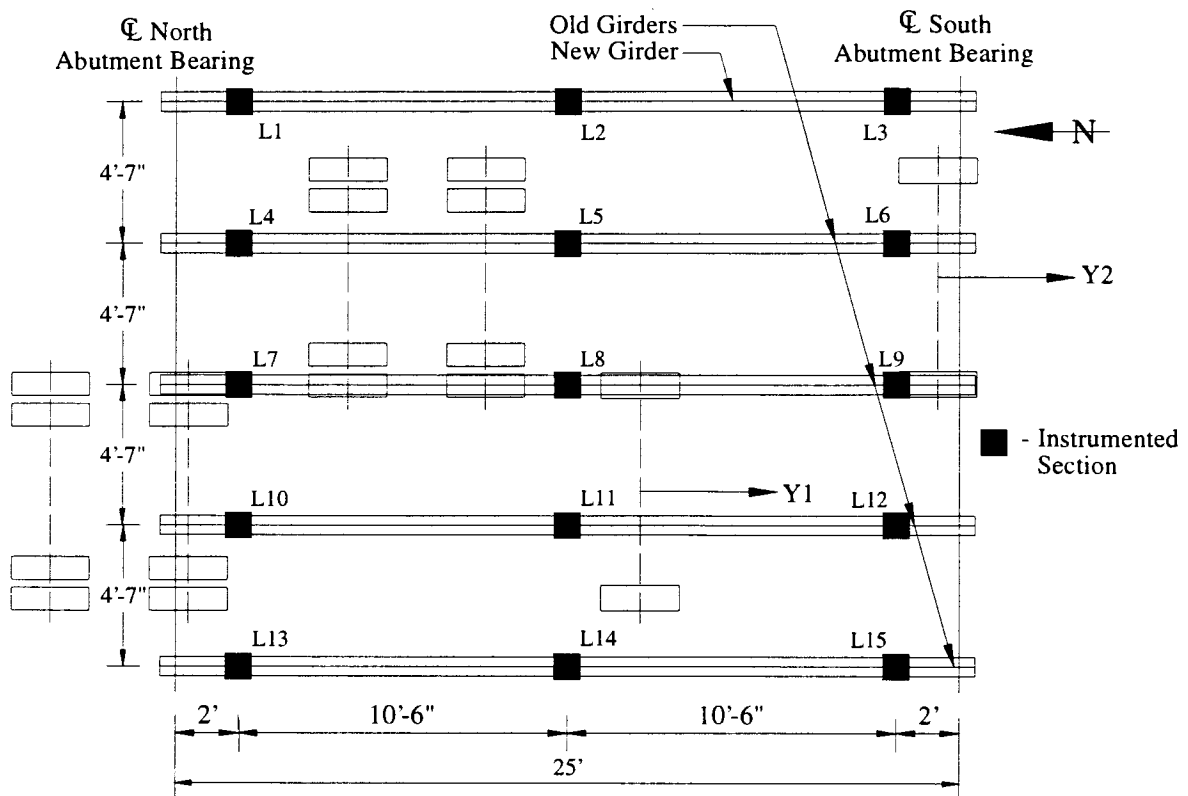
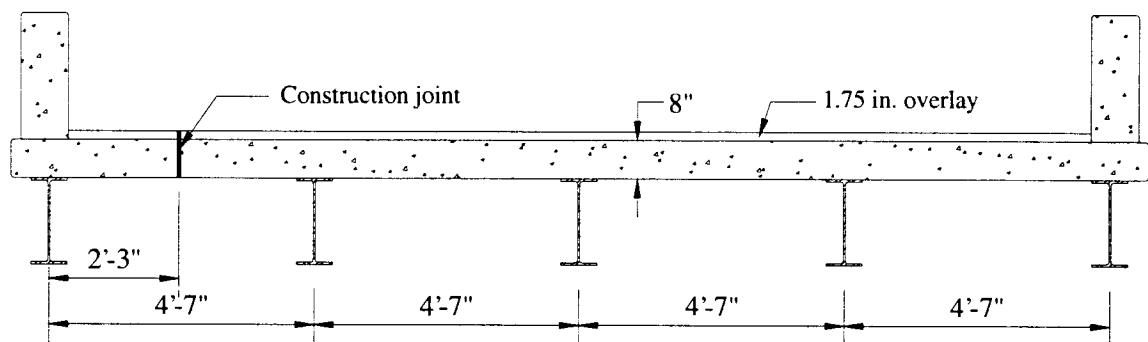
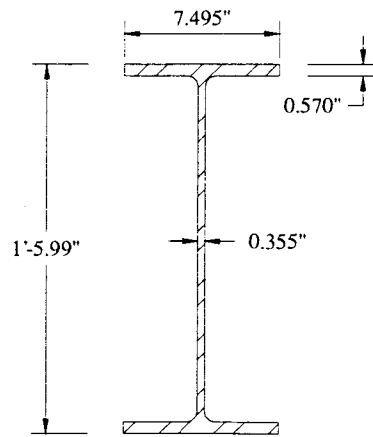


Figure 4.23. Bridge #5: Overall dimensions, gage locations, and truck paths.

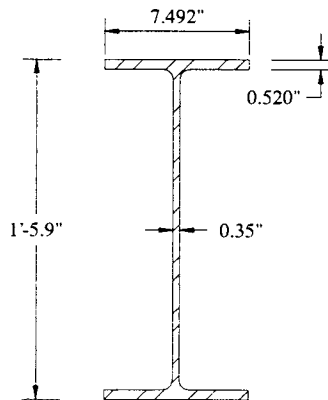


a. Cross-section of the bridge.

Figure 4.24. Bridge #5: Typical cross-sections of the girders and the bridge.



b. Cross-section of the new girder.



c. Cross-section of the old Girder.

Figure 4.24. Continued.

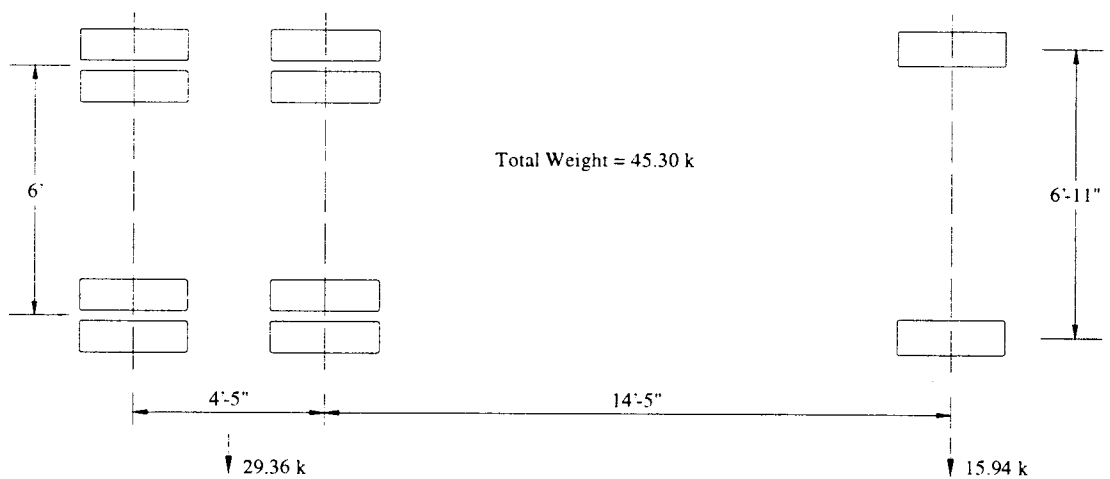


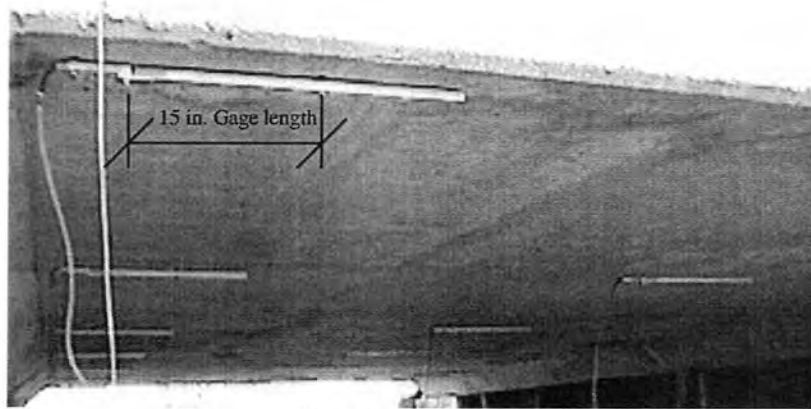
Figure 4.25. Bridge #5: Load Truck Details.

4.7. BRIDGE #6

Bridge #6, Iowa DOT Bridge Number 7530.7A 140, located in Plymouth County, IA, is a simple-span, concrete-slab bridge with no skew. This bridge, which was built in 1957, carries Iowa State Highway 140 over a drainage ditch 3.8 miles North of Kingsley. Based on a cursory visual inspection and photographic documentation (shown in Fig. 4.26) all structural elements appeared to be in good condition. It was anticipated that the bridge would exhibit significant end restraint since there are no abutment deck expansion joints. This bridge, shown in plan view in Fig. 4.27 and in cross-section in Fig. 4.28 has a span length of 20 ft from centerline to centerline of the abutment bearings with a roadway width of 38 ft and an overall structure width of 40 ft (two 12 ft traffic lanes and two shoulders – one 8 ft wide and the other 6 ft wide).

The deck consists of a uniform 15-in. thick P.C concrete deck with earth fill and Asphalt Concrete (A.C) pavement over it. The superstructure is a single span concrete-slab structure. The substructure consists of wood pile abutments with wood backing plank and concrete caps. The roadway is offset 1 ft to the East of the bridge centerline as shown in Fig. 4.28. Only one gage was installed at each instrumented sections (placed on the bottom surface of the slab) because the fill on top of the deck made the placement of transducers on top of the slab difficult. As a result, locating the neutral axis locations for this bridge is difficult. Three gages were installed on top of the West curb so the location of the neutral axis at these locations (L1, L2, and L3) could be determined. Thus, there were a total of 24 gages on the bridge installed at 21 locations, as shown in Fig. 4.27b. Gage extensions (15 in. in length) were used for all gages.

A loaded tandem-axle dump truck with a total weight of 52.1 k was used in the tests. Details for the truck are given in Fig. 4.29. Data were collected for four truck paths as shown in Fig. 4.27. Path Y1 was oriented such that the driver's side wheel line was located 4 ft from the West edge. Path Y2 was oriented with the driver's side wheel line 11 ft – 6 in. from the West edge. Path Y3 was oriented with the passenger side wheel line 11 ft – 6 in. from the East edge. Finally, path Y4 was oriented with the passenger side wheel line 4 ft from the East edge.



a. Gage installation on the bottom of the slab.

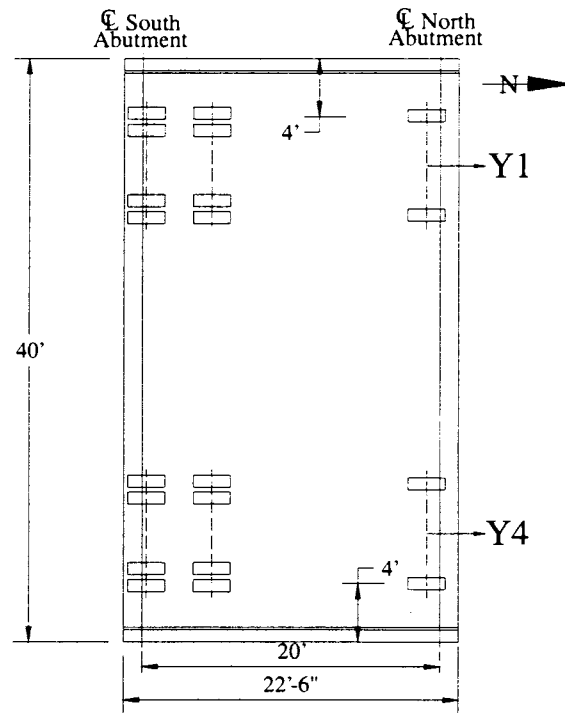


b. Side view of bridge.

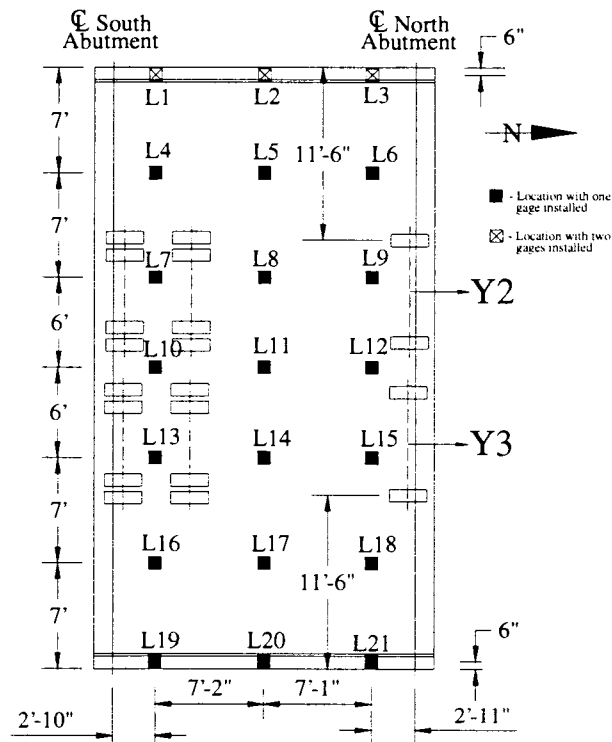


c. End view of bridge with truck path Y4.

Figure 4.26. Bridge #6: Photographs of the bridge.



a. Overall dimensions and truck paths Y1 and Y4.



b. Gage locations and truck paths Y2 and Y3.

Figure 4.27. Bridge #6: Overall dimensions, gage locations and truck paths.

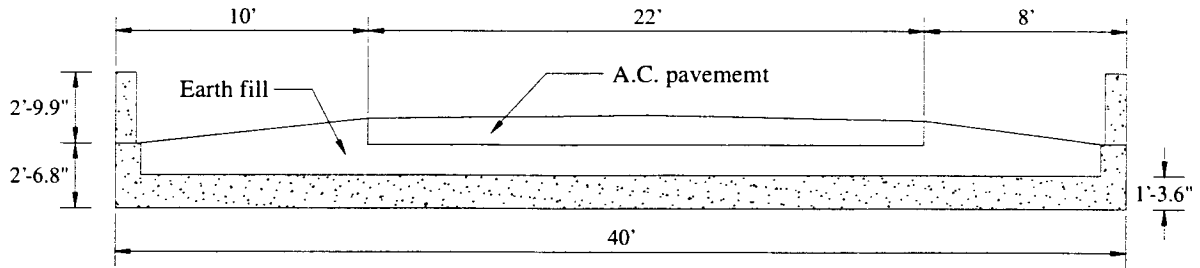


Figure. 4.28. Bridge #6: Cross-section of the bridge at midspan.

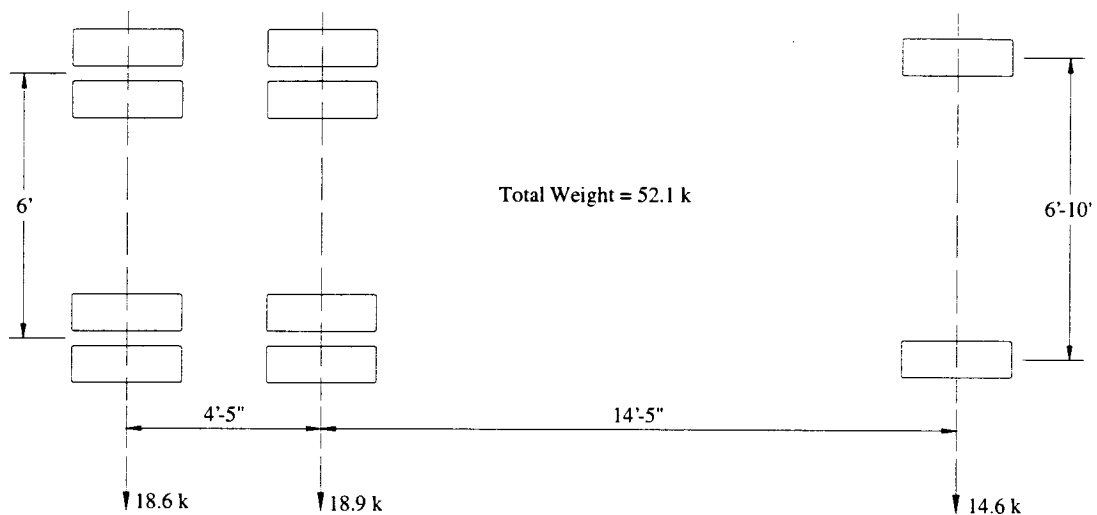


Figure 4.29. Bridge #6: Load Truck Details.

4.8. BRIDGE #7

Bridge #7, Iowa DOT Bridge Number 3718.7S 030, located in Boone County, IA, is a simple-span, concrete-slab bridge with no skew. This bridge, which was built in 1921, carries US Highway 30 over Little Beaver Creek. Based on a cursory visual inspection, there are many concerns with the bridge. The top of the deck has many hairline to wide longitudinal cracks, several hairline to narrow transverse cracks, and a few spalls along both ends of the deck. Two of the wide longitudinal cracks extend the full length of the deck, and both curbs have a few hairline vertical cracks. Photographs of this bridge are presented in Fig. 4.30: showing spalling and heavy deterioration at the edge (shown in Fig. 4.30a), a side view of bridge (shown in Fig. 4.30c), and the reinforcing steel bars exposed on bottom of the slab (shown in Fig. 4.30c). It was anticipated that the bridge would not



a. Spalling and heavy deterioration at edge.



b. Side view of bridge.



c. Reinforcing steel bars exposed on bottom of slab.

Figure 4.30. Bridge #7: Photographs of the bridge.

exhibit significant end restraint since there are abutment deck joints with a few narrow transverse cracks. This bridge, shown in plan view in Fig. 4.31 and in cross-section in Fig. 4.32, has a span length of 25 ft from centerline to centerline of abutment bearings with a roadway width of 30 ft and an overall structure width of 32 ft – 4 in. (two 12 ft traffic lanes and two 3 ft shoulders). Originally (in 1921), the roadway width measured 24 ft, but the bridge was widened in 1952 to accommodate two traffic lanes.

The deck consists of a uniform P.C. concrete-slab. The original slab thickness was 1 ft – 10 in., but was increased to 2 ft in 1952. In addition, the bridge was overlaid with additional concrete in 1978 such that the total deck thickness varied (i.e., 29 in. at the curb, and 33 in. at the centerline). The construction joint created due to the bridge widening (shown in Fig. 4.31) is located at approximately 6 ft from the East edge of the bridge. The superstructure is a single span concrete-slab structure. The substructure is a full height concrete abutment supported on untreated wood friction piling and a concrete wingwall. The gage instrumentation focused on the construction joint created during the widening of the bridge to establish its ability to transfer loads across the joint: gage pairs were installed on top and bottom surfaces of the deck at locations L14, L17 and L20 (shown in Fig. 4.31). However, these gages on top of the slab were only included for Path Y2 so that they would not be damaged while the truck was driven along other paths. The tops of the concrete rails were also instrumented near the abutments and at midspan (i.e., at locations L1, L2, L3, L22, L23 and L24) to quantify its contribution to edge stiffening. In addition, gages were placed on the bottom of the slab at all instrumented sections, thus there were a total of 33 gages (for Path Y2) on the bridge installed at 24 locations, as shown in Fig. 4.31. For all other paths, a total of 30 gages on the bridge were installed. Gage extensions (12 in. in length) were used for all gages on the bottom of the slab. No gage extensions were used for gages on top of the slab and on the curb.

A loaded tandem-axle dump truck with a total weight of 44.44 k was used in the tests. Details for the truck are given in Fig. 4.34. Data were collected for five truck paths as shown in Fig. 4.32, where the truck paths were oriented as follows with respect to the left wheel line measured from the Eastern structure end: path Y1 was 10 ft – 1 in. from the end, path Y2 was 16 ft from the end and path Y3 was 12 ft – 10 in. from the end. With respect to the left wheel line measured from the Western structure end: path Y4 was 2 ft – 9 in. from the end and path Y5 was 5 ft – 6 in. from the end (shown in Fig. 4.37b).

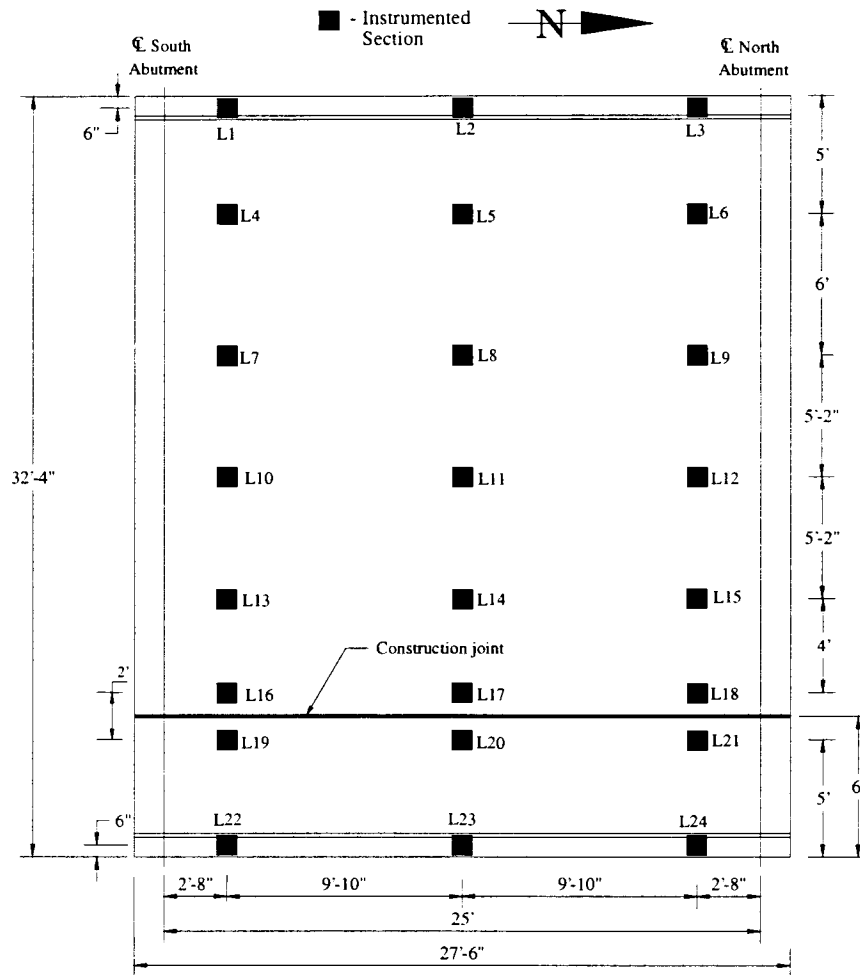


Figure 4.31. Bridge #7: Overall dimensions and gage locations.

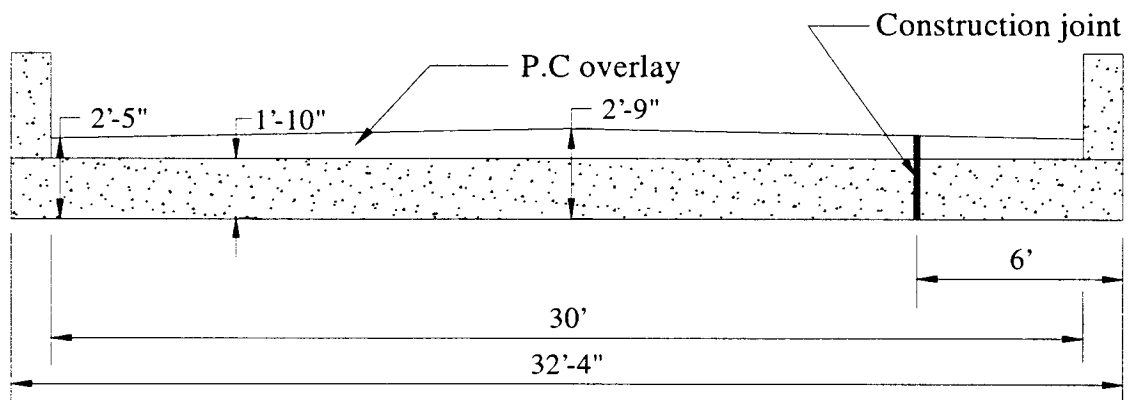
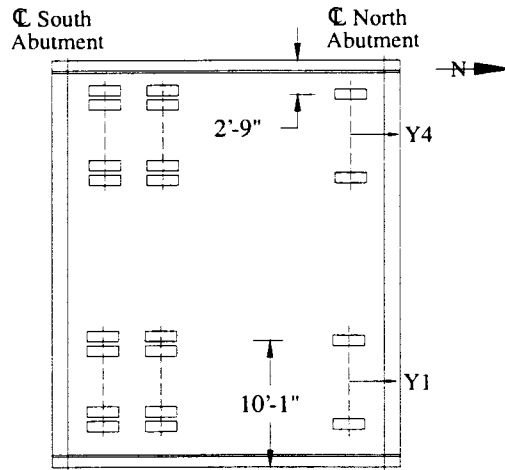
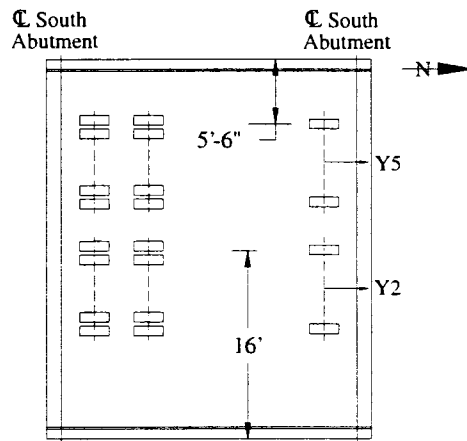


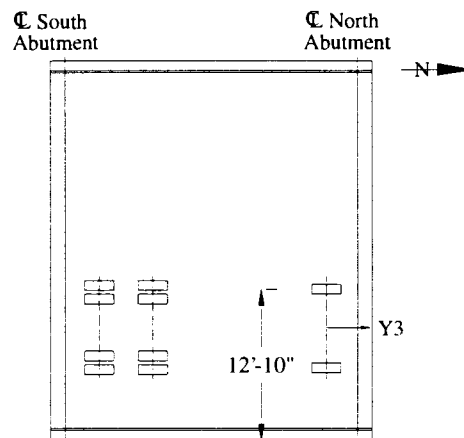
Figure 4.32. Bridge #7: Cross-section of the bridge at midspan.



a. Truck paths Y1 and Y4.



b. Truck paths Y2 and Y5.



c. Truck path Y3.

Figure 4.33. Bridge #7: Truck path information.

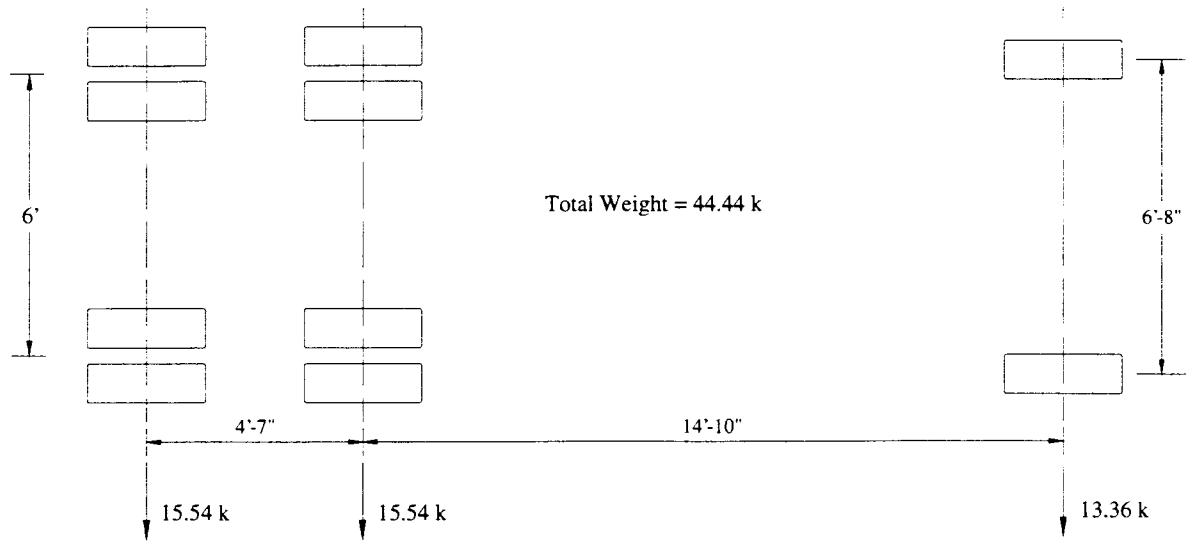


Figure 4.34. Bridge #7: Load Truck Details.

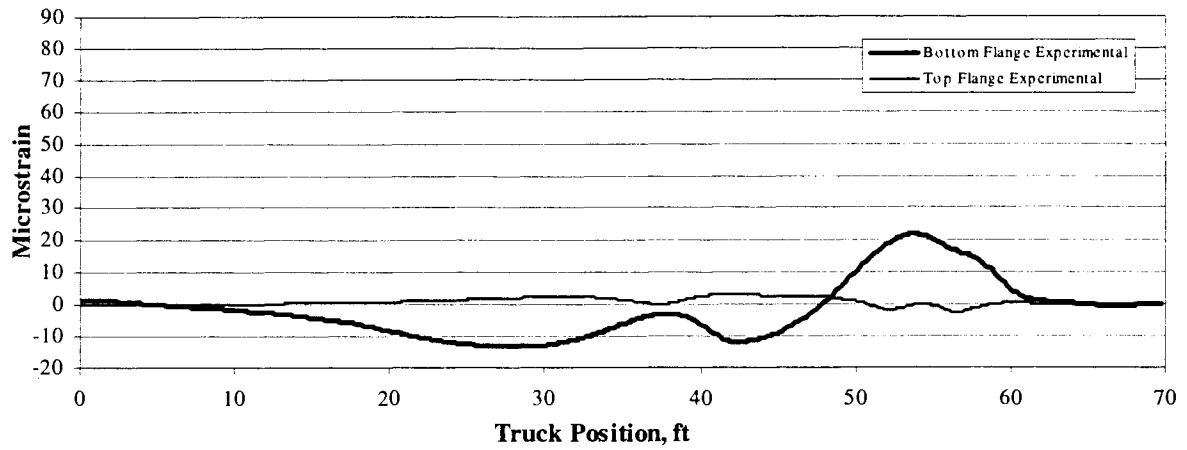
5. MODEL VERIFICATION AND BRIDGE RATING RESULTS

This chapter presents the results obtained for the bridge used in the modeling verification process and for the bridges tested as part of this investigation. Included, for each bridge, is information on the preliminary investigation of data, a description of the analytical model, analytical results such as statistics and data, and rating results. Also included is information on a sensitivity test conducted on the Cedar Creek Bridge model, a partial proof load test completed on Bridge #1 using a full, half-full, and empty truckload, and a test that was performed for Bridge #2 to verify that one can predict strains at locations where there is no instrumentation.

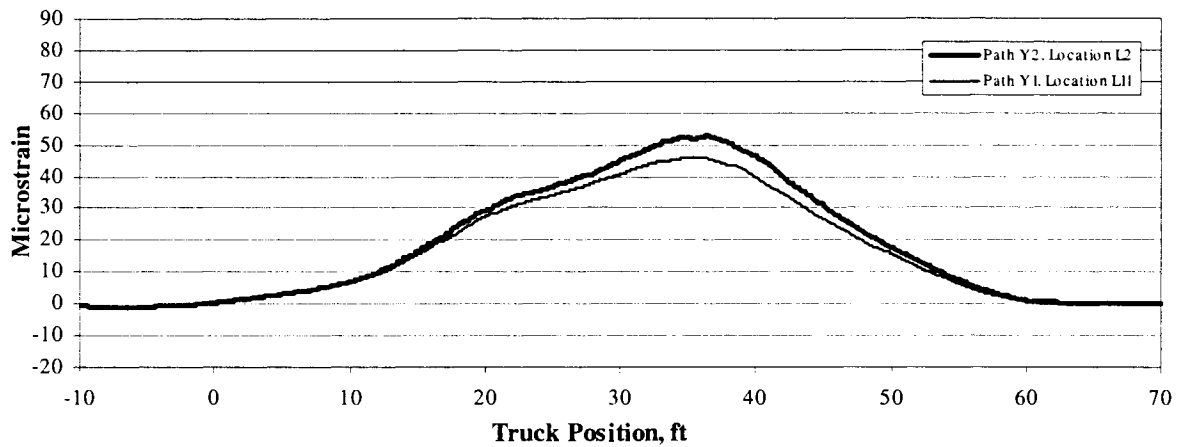
5.1. CEDAR CREEK BRIDGE: MODEL VERIFICATION

As shown in Fig. 5.1a, Cedar Creek Bridge exhibits compression in the girder bottom flange near the abutment. This indicates that end restraint exists. The location of the neutral axis lies approximately in the top flange as illustrated in Fig. 5.1a by the relatively small top flange strain levels shown; hence composite action is verified. Moreover, experimental strains presented in Figs. 5.1b and 5.1c illustrate transverse and longitudinal strain symmetry, respectively. The data for transverse symmetry show that maximum compression strains are approximately the same magnitude (15-20 microstrain). Longitudinal strain symmetry, to investigate boundary condition similarities, is difficult to verify due to the unidirectional movement of the load truck; however, longitudinal strain symmetry was assumed since the strains were relatively small.

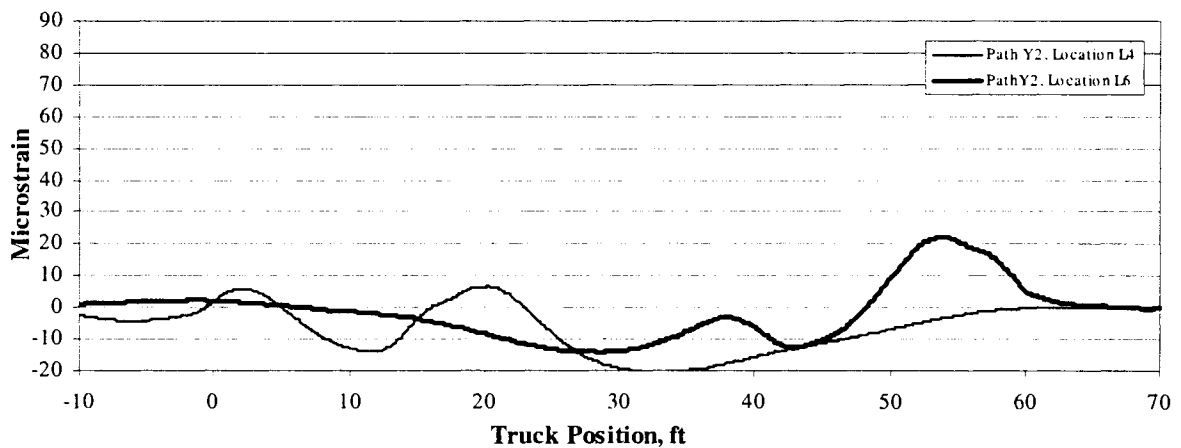
Based on the initial review of the data briefly discussed in the previous paragraph, an analytical model was created as shown in Fig. 5.2 using twelve elements in the longitudinal direction and nine elements in the transverse direction. Translational springs (with an eccentricity of 30 in. from the neutral axis to bottom flange) were included for all girders at the centerline of the abutment to simulate possible end restraint. Since the potential for moment reversal exists due to the significant end restraint, all girders were modeled with two different sections along the length (i.e., a positive and a negative moment section). In addition, the exterior girders were modeled separately from the interior girders to account for possible edge stiffening. All girder sections were modeled with beam elements. The reinforced concrete slab was modeled with quadrilateral plate elements with a uniform thickness of 8.28 in. Table 5.1 summarizes the optimized model parameter results. These data indicate that most results compare well with results previously obtained by BDI. The only exception is the optimized value for the exterior beam near the abutment where the BDI value is almost twice the ISU value. A possible explanation for this is that different neutral axis locations may have been



a. Experimental strains at Location L9 for Path Y1.



b. Experimental strains showing transverse strain symmetry for bottom flanges.



c. Comparison of experimental strains for bottom flanges to identify longitudinal strain symmetry.

Figure 5.1. Cedar Creek Bridge: End restraint, composite action and strain symmetry.

used by BDI and herein. The optimized stiffness parameters depend on the distance from the neutral axis to bottom gage, and if this distance is significantly different in the two models, the optimized stiffness parameters will also be different.

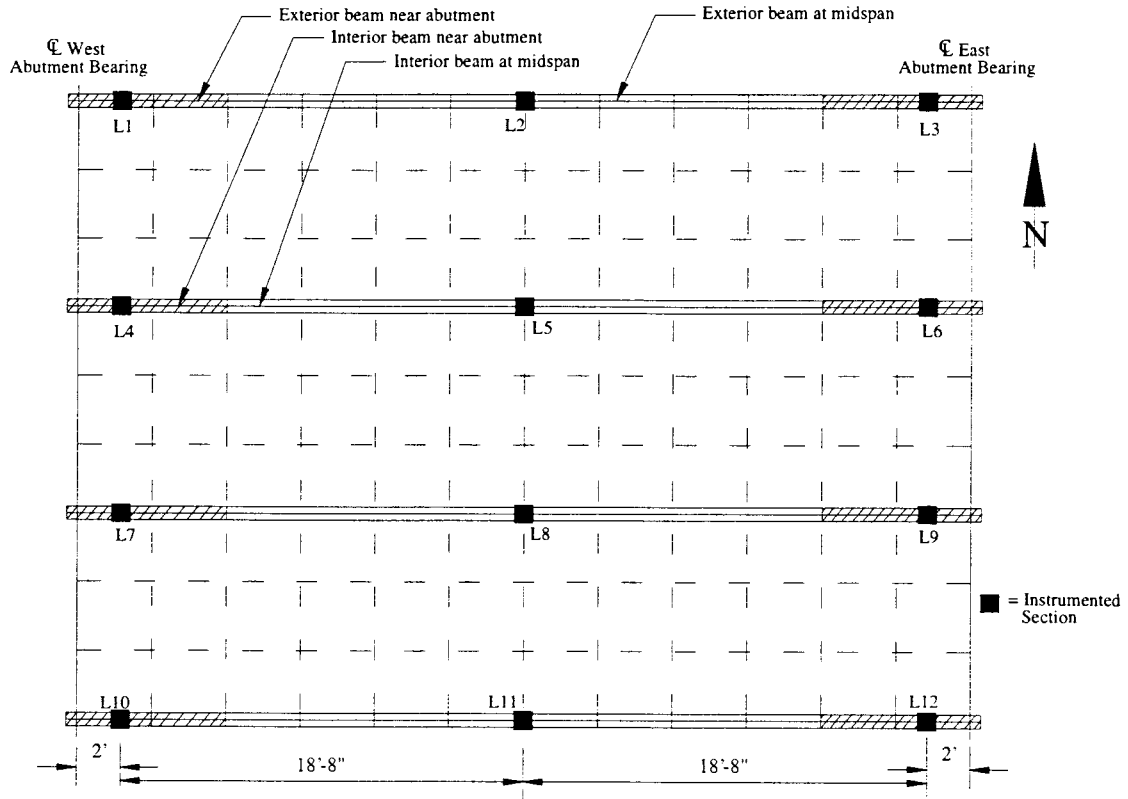


Figure 5.2. Cedar Creek Bridge: Bridge mesh, gage locations and section property names.

Table 5.1. Cedar Creek Bridge: Adjustable parameters.

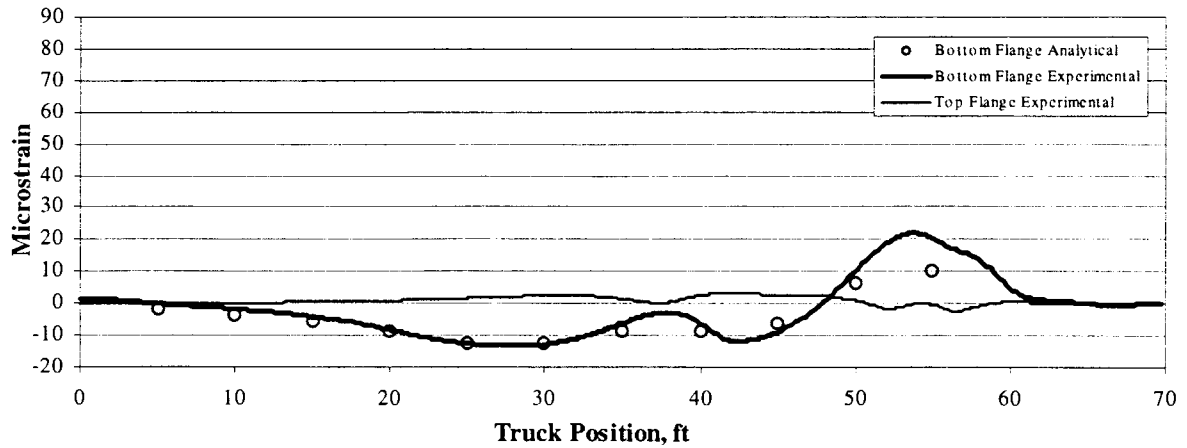
Section	Property	Units	Optimized value		%
			BDI value	ISU value	Difference
Slab modulus	E	ksi	5,815	5,990	3.1
Exterior beam at midspan	I_y	in^4	29,460	29,340	-0.4
Exterior beam near abutment	I_y	in^4	15,910	7,970	-49.9
Interior beam at midspan	I_y	in^4	16,660	17,360	4.2
Interior beam near abutment	I_y	in^4	10,490	11,270	7.4
Abutment spring (translational)	K_x	Kips/in	1,770	1,470	-16.8

The accuracy of the model is shown graphically in Fig. 5.3 for typical data at various locations. Generally, the model results and experimental results compare well. Table 5.2 summarizes the model accuracy in statistical terms. These data also illustrate the similarity between the two models (i.e., BDI and ISU), and shows a very good correlation. The absolute errors and the scale error differ slightly, but the differences are possibly due to reasons as previously mentioned (using a different location of the neutral axis for the exterior beam near the abutment).

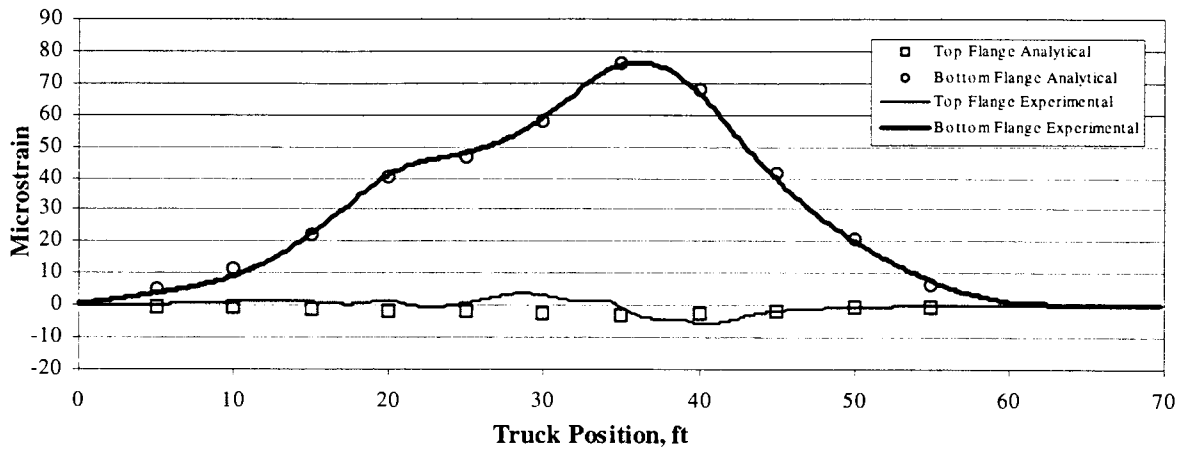
Table 5.2. Cedar Creek Bridge: Model accuracy.

Statistical Term	Units	Final value	
		BDI value	ISU value
Absolute Error	Microstrain	911	836
Percent Error	%	6.0	5.8
Scale Error	%	4.2	7.2
Correlation Coefficient	-	0.97	0.97

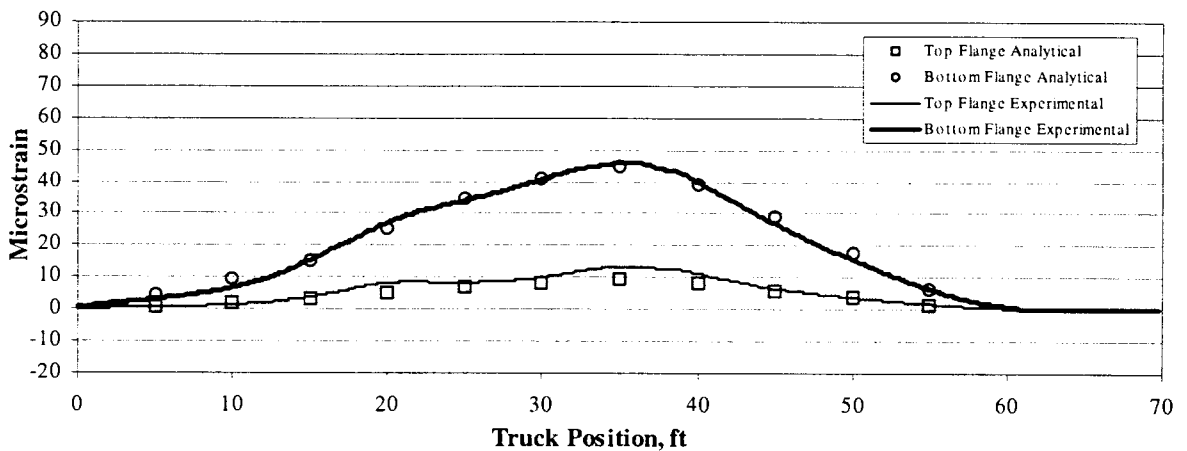
In addition to comparing the overall results, a sensitivity study was conducted using the optimized model. In this study, the neutral axis location for the interior beams in the midspan region was varied. The purpose of this was to observe what influence changing the neutral axis location would have on the optimized stiffness parameters (shown in Table 5.3), on the moment distribution (shown in Table 5.4), and on the accuracy of the modeling and optimization process (shown in Table 5.5). This was completed because one important step in the initial model generation is the establishment of the neutral axis location. Typically, this is determined from the strain data. However, this is a subjective determination. To study the impact of this determination, the neutral axis location was “moved” by changing the effective width of the concrete slab in the composite steel section for the interior girders near midspan, and the optimization was re-run. When optimizing the models for each neutral axis location, the same truck paths were used as previously described. Table 5.3 shows the difference in stiffness parameter values due to variations in neutral axis locations and indicates that all parameters vary slightly due to a change in the neutral axis at a single location (i.e., interior beam at midspan). The moments shown in Table 5.4 are the maximum girder live load moments when the field truck is positioned as shown in Fig. 5.4 (Path Y2 previously shown in Fig. 4.2). By varying the neutral axis location by 7 in., the midspan moments varied by up to 10 % and the moments near the abutment varied by up to 25%. These differences illustrate the importance of



a. Experimental strains and analytical strains at Location L9.



b. Experimental and analytical strains at Location L8.



c. Experimental and analytical strains at Location L11.

Figure 5.3. Cedar Creek Bridge: Typical experimental and analytical strains for load Path Y1.

establishing accurate neutral axis locations. The difference in model accuracies are illustrated in Table 5.5, and shows that the percent error (which is the objective function for the optimization process) varies between 5.8 % and 7.3 %, depending on the neutral axis location.

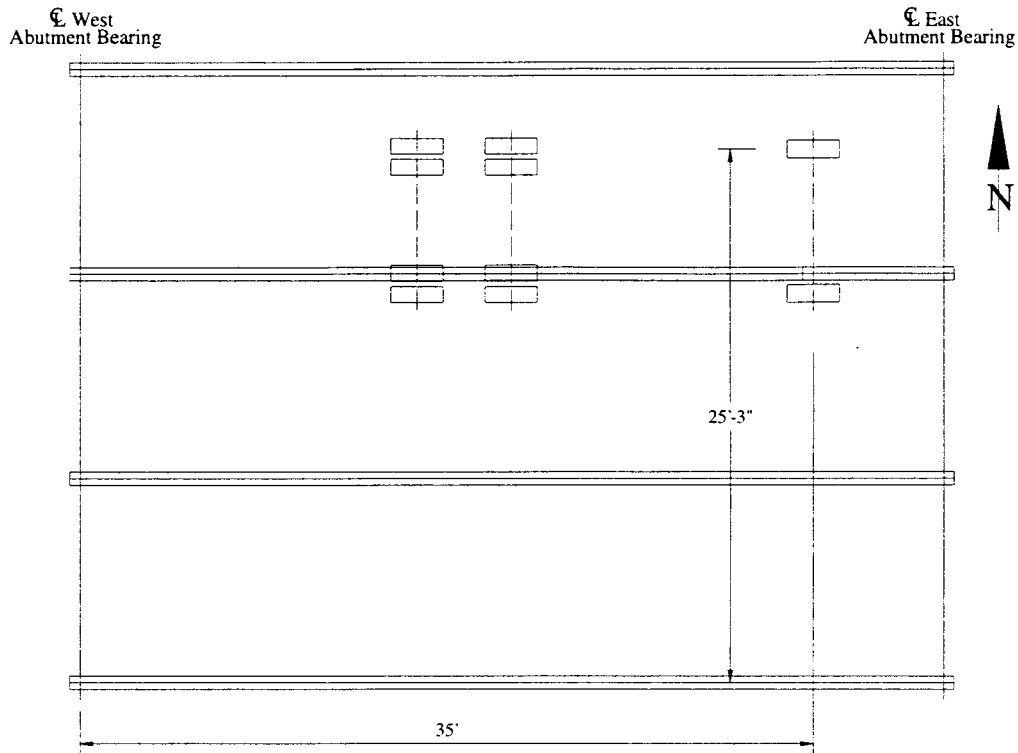


Figure 5.4. Cedar Creek Bridge: Truck position in sensitivity test.

Table 5.3. Cedar Creek Bridge: Stiffness parameters from Sensitivity Test when changing the location of the neutral axis for the interior girders at midspan.

Section	Property	Units	Distance from bottom of steel to neutral axis, in.							
			23	24	25	26	27	28	29	30
Int beam - abut	I_y	in^4	10,330	10,590	10,880	11,230	11,610	12,000	12,390	12,850
Ext beam - mid	I_y	in^4	29,910	29,750	29,570	29,350	29,120	28,860	28,590	28,270
Ext beam - abut	I_y	in^4	8,950	8,660	8,340	8,000	7,655	7,300	6,945	6,600
Int beam - mid	I_y	in^4	15,500	16,010	16,590	17,290	18,070	18,920	20,260	20,840
Deck	E	ksi	5,480	5,715	5,985	6,000	6,000	6,000	6,000	6,000
Spring (translational)	F_x	K/in	1,410	1,425	1,445	1,470	1,490	1,520	1,540	1,565

Table 5.4. Cedar Creek Bridge: Maximum moments from Sensitivity Test when changing the location of the neutral axis for the interior girders at midspan.

Section	Property	Units	Distance from bottom of steel to neutral axis, in.							
			23	24	25	26	27	28	29	30
Int beam - abut	M_y	K-in	150	145	140	137	134	130	124	123
Ext beam - mid	M_y	K-in	1,450	1,445	1,435	1,410	1,400	1,385	1,360	1,350
Ext beam - abut	M_y	K-in	78	80	82	85	87	90	93	97
Int beam - mid	M_y	K-in	1,415	1,420	1,430	1,450	1,475	1,505	1,545	1,560

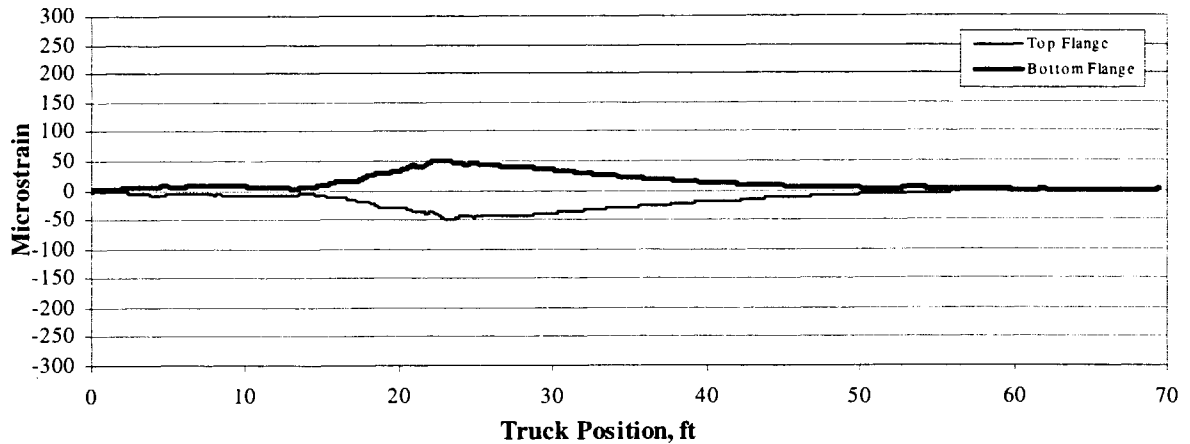
Table 5.5. Cedar Creek Bridge: Model accuracy from Sensitivity Test when changing the location of the neutral axis for the interior girders at midspan.

Statistical Term	Units	Distance from bottom of steel to neutral axis, in.							
		23	24	25	26	27	28	29	30
Total Error	Microstrain	956	910	868	838	836	852	880	913
% Error	%	7.3	6.5	6.0	5.8	5.8	6.0	6.3	6.8
Scale Error	%	12.8	10.8	9.0	7.3	6.2	7.8	9.2	10.7
Correlation Coefficient	-	0.963	0.967	0.967	0.971	0.971	0.970	0.968	0.966

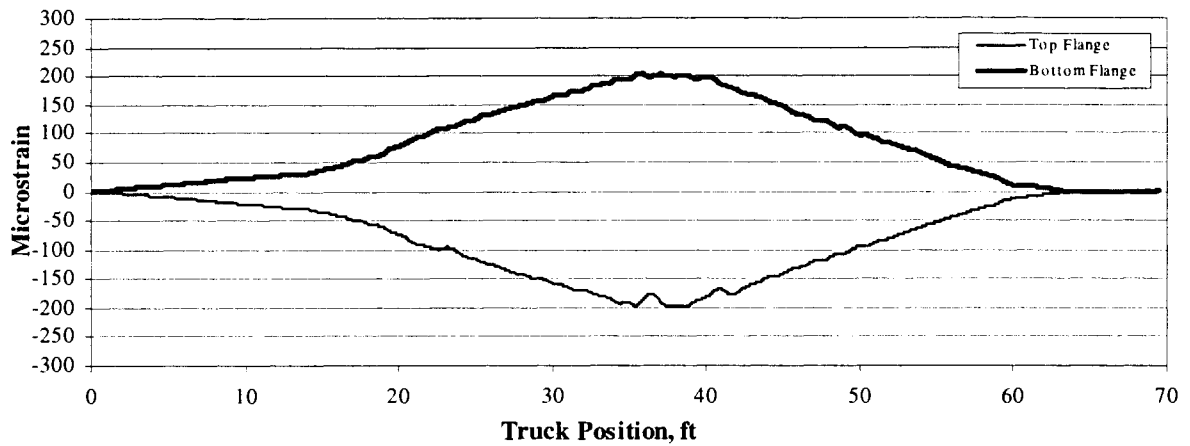
5.2. BRIDGE #1

As shown in Fig. 5.5a, compression was induced in the top flange and tension occurred in the bottom flange near the abutment. This indicates that Bridge #1 exhibits little end restraint. The location of the neutral axis lies approximately at mid depth of the steel sections since strains are approximately the same for both top and bottom gages at midspan as shown in Fig. 5.5b; hence non-composite action is verified. Moreover, the strain is symmetric in the transverse direction as shown in Fig. 5.5c. Strain symmetry in the longitudinal direction was not possible to verify as no gages were installed near the West abutment (shown in Figs. 4.7b and 5.6).

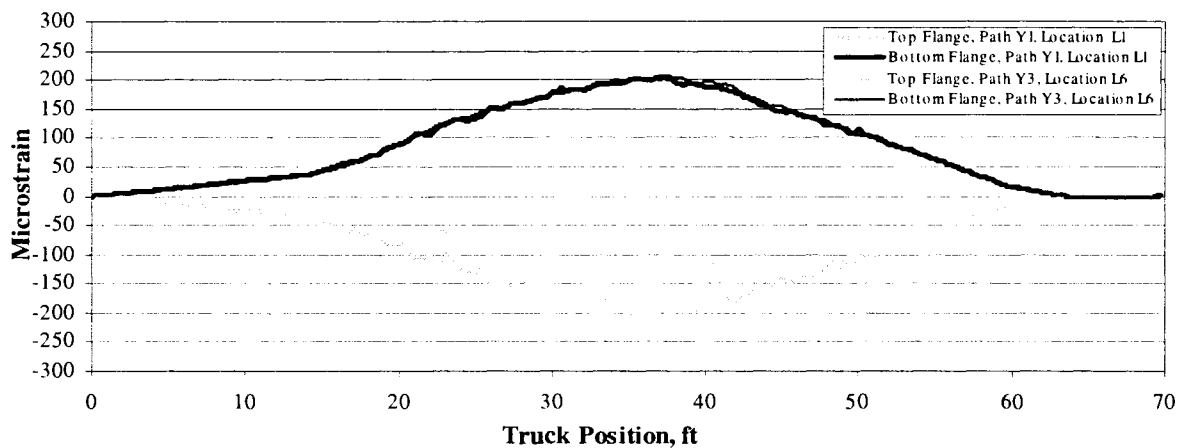
Based on the initial review of the data briefly discussed in the previous paragraph, an analytical model (named Model 1 for future reference) was created as shown in Fig. 5.6 using one element between each girder in the transverse direction and twelve elements in the longitudinal direction. The channel diaphragm lines were not included in the analytical model because the BDI Software treats transverse beams as floor-beams. Therefore, it is appropriate to disregard the diaphragms in the analytical model. Even though experimental data indicate insignificant presence of



a. Experimental strains for Path Y3 at Location L11



b. Experimental strains for Path Y3 at Location L5.



c. Experimental strains showing transverse strain symmetry.

Figure 5.5. Bridge #1: End restraint, non-composite action and strain symmetry.

of end restraint, rotational springs were included for all girders at the centerline of the abutment bearings to verify this behavior. As indicated by the experimental data, the girders in the analytical model were modeled as one uniform, non-composite section. In addition, the rail did not contribute to any edge stiffening (the neutral axis location for an exterior girder lies approximately at mid depth as shown in Fig. 5.7a), so the exterior girders were not distinguished from the interior girders. The girder section was modeled with beam elements and the timber deck was modeled with quadrilateral plate elements with a uniform thickness of 4 in. Table 5.6 summarizes the optimized stiffness parameter results. These results indicate that all optimized stiffness parameters (excluding the springs) compare very well with the initial parameters. The magnitude of the optimized spring value (21,000 in-k/rad) is insignificant indicating a nearly pinned condition; a 90 % fixed case would have a rotational restraint (in-k/rad) to the power of six.

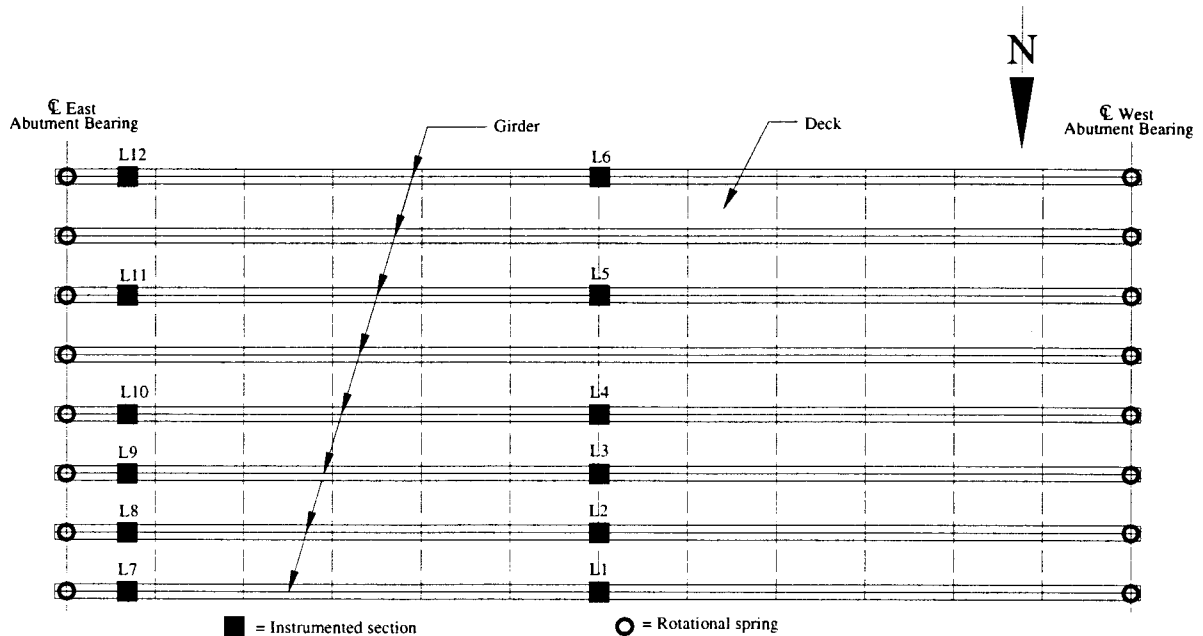
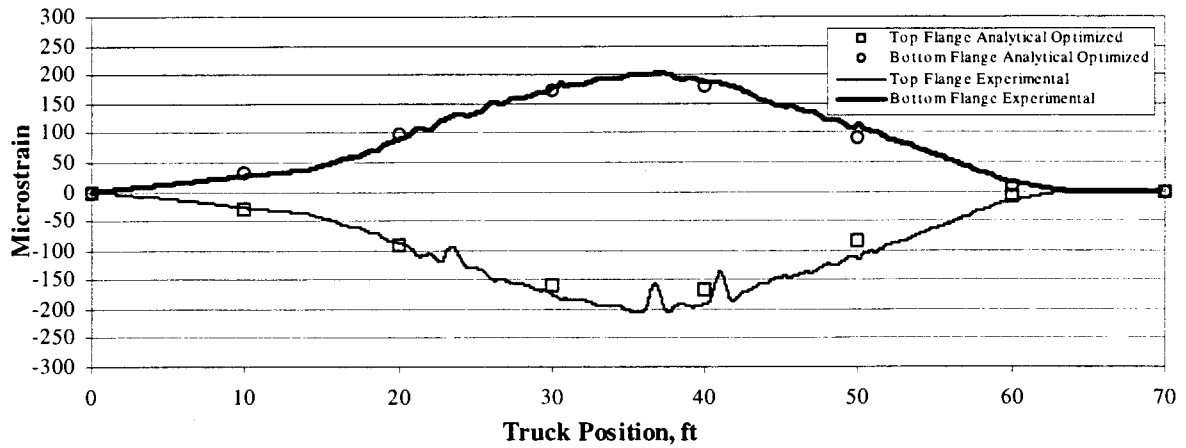


Figure 5.6. Bridge #1: Bridge mesh, gage locations and section property names.

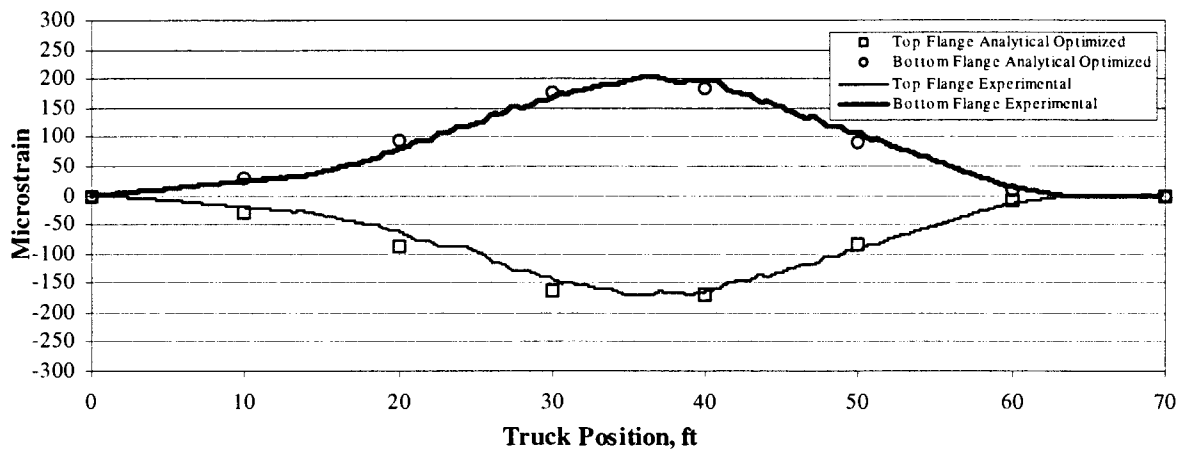
Table 5.6. Bridge #1: Adjustable parameters using full truckload (Model 1).

Section	Property	Units	Initial	Optimized
Girder	I_y	in^4	1,480	1,560
Timber deck	E	ksi	1,000	925
Spring (rotational)	K_y	in-k/rad	0	21,090 ^a

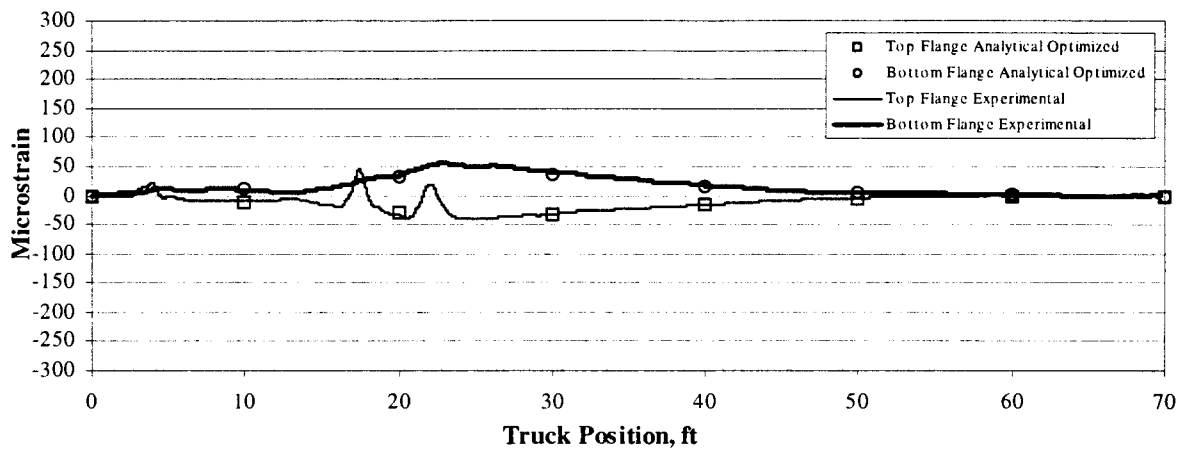
^a Corresponds to approximately 5 % fixity.



a. Location L1.



b. Location L3.



c. Location L9.

Figure 5.7. Bridge #1: Typical strain plots using Path Y1 and full truckload.

The accuracy of the model is shown graphically in Fig. 5.7 for typical data at various locations using the “full” truckload condition, where Fig. 5.7a compares exterior girder strains at midspan, Fig. 5.7b shows interior girder strains at midspan, and Fig. 5.7c illustrates interior girder strains near the abutment. All results are very comparable. Table 5.7 summarizes the model accuracy and shows a very good correlation. The initial model assuming a simply supported condition and initial section property values results in an error of only 4.4 %. This low initial error verifies that the bridge is almost simply supported and that the girders are non-composite. The optimized error of 2.2 % implies a very good correlation of the experimental and analytical data.

Table 5.7. Bridge #1: Model accuracy for the full truckload.

Statistical Term	Units	Initial	Optimized
Total Error	microstrain	3,924	2,674
% Error	%	4.4	2.2
% Scale Error	%	6.7	2.4
Correlation Coefficient	-	0.99	0.99

By using this optimized model with the appropriate rating trucks and by applying dead load to the structure, the rating model was developed. Dead load applied to the structure includes the self-weight of the steel girders and a four-in. thick timber deck, a 6.5 in. x 6.5 in. wood curb applied to the exterior girders, a weight of 25 lb/ft distributed uniformly over both exterior girders to take into account the steel rail on top of the wood curb, a uniform load distributed over the interior beams to account for the dead load of the diaphragms, and an additional 1 in. deep asphalt and 3 in. gravel overlay on top of the timber deck. For rating purposes, the following truck paths were considered:

- Paths A and B: The outer wheel line two ft from each curb.
- Paths C, D, E and F: The outer wheel line on the four interior girders to the far North.
- Path G: The outer wheel line on the interior girder to the far South.
- Path H: The truck centered across roadway width.

Each path was analyzed at 6 in. intervals in the longitudinal direction. The bridge was designed as a single-lane bridge, so no truck path combinations were considered. Individual member capacities were calculated following appropriate AASHTO Standard Specifications (4) and are presented in Appendix D. Table 5.8 and Table 5.9 present the resulting ratings by the LFD Method (by applying AASHTO Standard Specifications (4)) and by using the BDI Software, respectively. These results

show that all BDI Method ratings are greater than the LFD ratings. Table 5.10 summarizes the percent difference in inventory ratings between the LFD Method and the BDI Method (note: a positive percent difference indicates that the BDI Software rating value is greater than the LFD Method rating value, and negative percent difference indicates that the BDI rating value is less than the LFD Method value). The critical rating condition is for flexure at the interior girder (0.81 by the LFD Method and 1.17 by the BDI Method for a difference of 44 %). It should be pointed out that lane loadings were investigated in accordance with AASHTO Standard Specifications (4) and found to not be critical.

Table 5.8. Bridge #1: Design Truck Rating Factors by the LFD Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv. ^a	Ope. ^b	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Interior Girders	0.81	1.36	3.18	5.31	1.09	1.83	4.81	8.03	1.06	1.77	4.34	7.25
Exterior Girders	0.90	1.49	3.54	5.91	1.20	2.01	5.35	8.93	1.17	1.95	4.83	8.06

^a Inv. = Inventory Rating Factor

^b Ope. = Operating Rating Factor

Table 5.9. Bridge #1: Design Truck Rating Factors by the BDI Software.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Interior Girders	1.17	1.95	3.95	6.59	1.51	2.51	5.25	8.62	1.58	2.64	5.50	9.17
Exterior Girders	1.32	2.21	6.00	10.01	1.82	3.03	9.43	15.74	1.75	2.92	8.28	13.82

Table 5.10. Bridge #1: Percent difference in inventory ratings between LFD Method and BDI Software.

Section	HS-20		H-20		Type-3	
	Flexure	Shear	Flexure	Shear	Flexure	Shear
Interior Girders	44.4	24.2	38.5	9.1	49.1	26.7
Exterior Girders	46.7	69.5	51.7	76.3	49.6	71.4

In addition to generating the previously described optimized model using a full truckload (Model 1 as previously described) and comparing the overall results, a sensitivity study was completed by creating additional models using the half-full truck (Model 2) and the empty truck (Model 3) with the respective data. All three models were optimized separately with appropriate loads and strain results, with the adjustable stiffness parameters for each model presented in Table 5.11. These results illustrates that the optimized values for all three models are similar. Model accuracies are presented in Table 5.12 and Table 5.13, respectively, and show that all results compare very well indicating that the optimization process is, for this bridge, independent of the load used.

Table 5.11. Bridge #1: Adjustable parameters for all truckloads.

Section	Property	Units	Full truck Half-full truck Empty truck			
			Initial	Optimized	Optimized	Optimized
Girder	I_y	in^4	1,480	1,560	1,525	1,595
Timber deck	E	ksi	1,000	925	1,100	1,210
Spring (rotational)	K_y	in-k/rad	0	21,090	35,560	31,560

Table 5.12. Bridge #1: Model accuracy for the half-full truckload (Model 2).

Statistical Term	Units	Initial	Optimized
Total Error	microstrain	3,279	1,870
% Error	%	6.0	2.1
% Scale Error	%	11.2	2.7
Correlation Coefficient	-	0.98	0.99

Table 5.13. Bridge #1: Model accuracy for the empty truck (Model 3).

Statistical Term	Units	Initial	Optimized
Total Error	microstrain	2,035	1,259
% Error	%	8.1	5.0
% Scale Error	%	13.3	4.0
Correlation Coefficient	-	0.99	0.98

The half-full truck and the empty truck cases were also analyzed using Model 1 to observe the effect. When the half-full truck and the empty truck were analyzed with Model 1, the results are referred to as M1 Half and M1 Empty (as shown in Table 5.14), respectively. The accuracies of these analyses are shown graphically in Fig. 5.8 for typical data at one location. All results show good correlation between experimental and analytical strains.

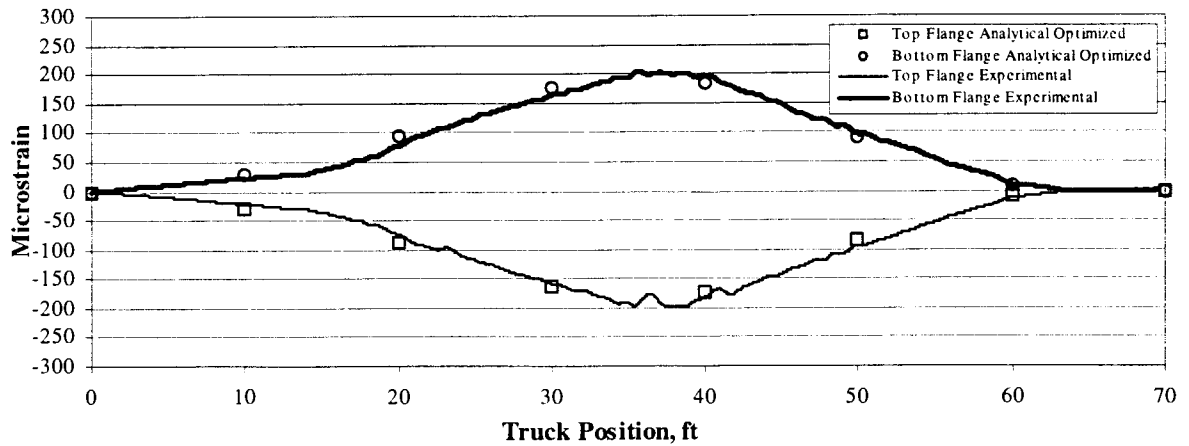
Table 5.14. Bridge #1: Model accuracy for M1 Half and M1 Empty.

Statistical Term	Units	M1 Half	M1 Empty
Total Error	microstrain	1,942	1,327
% Error	%	2.4	5.5
% Scale Error	%	4.2	4.7
Correlation Coefficient	-	0.99	0.97

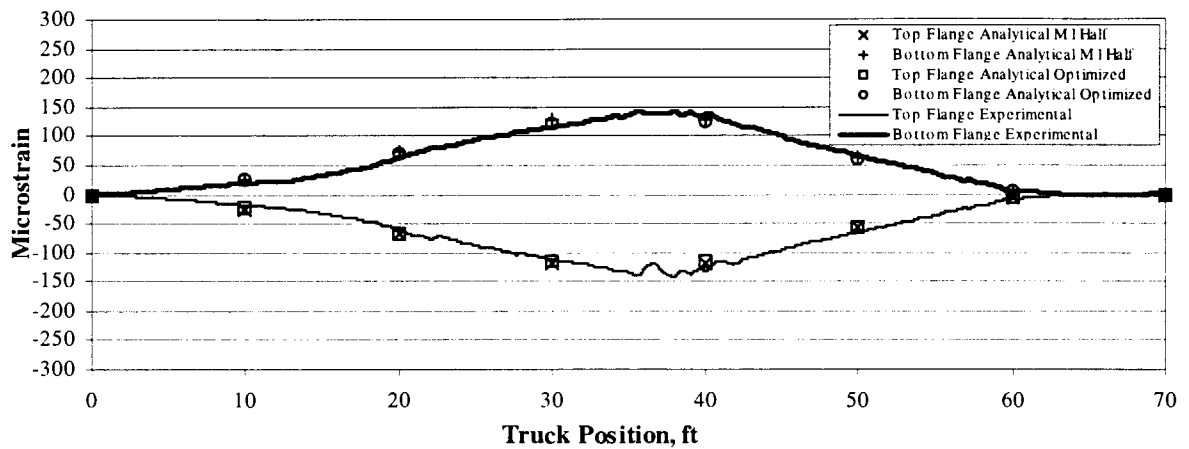
5.3. BRIDGE #2

The experimental data presented in Fig. 5.9a at Location L4 show that compression was induced in the top flange and tension occurred in the bottom flange near the abutment. This indicates that Bridge #2 does not exhibit significant end restraint. The location of the neutral axis is approximately at mid depth of the steel sections since strains are approximately the same for both top and bottom gages at midspan also as shown in Fig. 5.9a at Location L8; hence non-composite action is verified. Moreover, typical strain plots indicating transverse symmetry are illustrated in Fig. 5.9b. Experimental strains are also presented in Fig. 5.9c to identify longitudinal strain symmetry (note: longitudinal strain symmetry difficult to verify due to the unidirectional movement of the load truck).

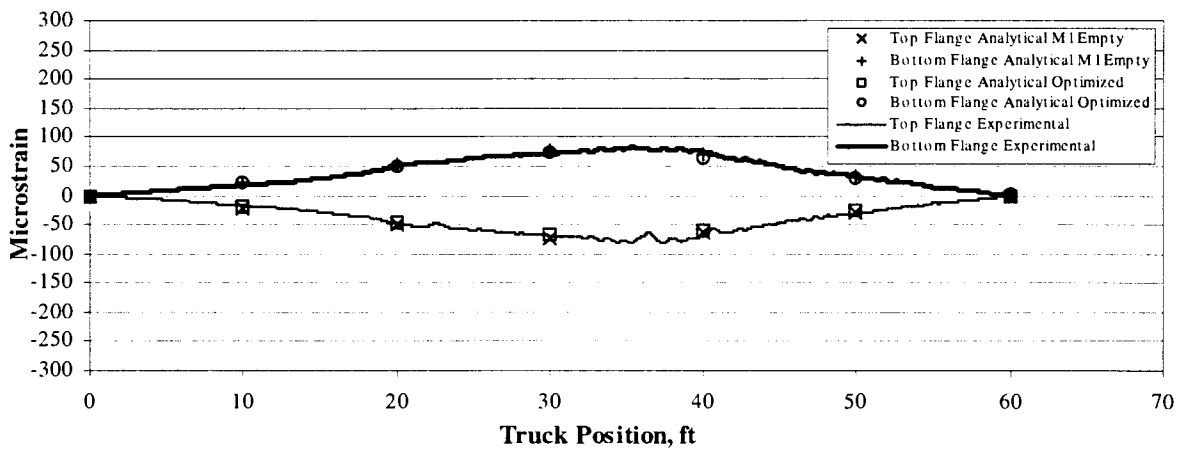
Based on the initial review of the data briefly discussed in the previous paragraph, an analytical model (Model 1) was created as shown in Fig. 5.10a using one element between each girder in the transverse direction and twelve elements in the longitudinal direction to obtain approximate square plate elements for the deck. The channel diaphragm lines were not included in the analytical model because the BDI Software treats transverse beams as floor-beams, hence it is appropriate to disregard the diaphragms in the analytical model. Even though experimental data indicate insignificant presence of end restraint, rotational springs were included for all girders at the centerline of the abutment bearings to verify this behavior. As a result of the experimental data indicating that all girders behave non-compositely, the girders in the analytical model were created as one uniform, non-composite section. In addition, the rail did not contribute to any edge stiffening (the thickness of 4 in. Table 5.15 summarizes the optimized parameter results. These results indicate that



a. Full truckload.

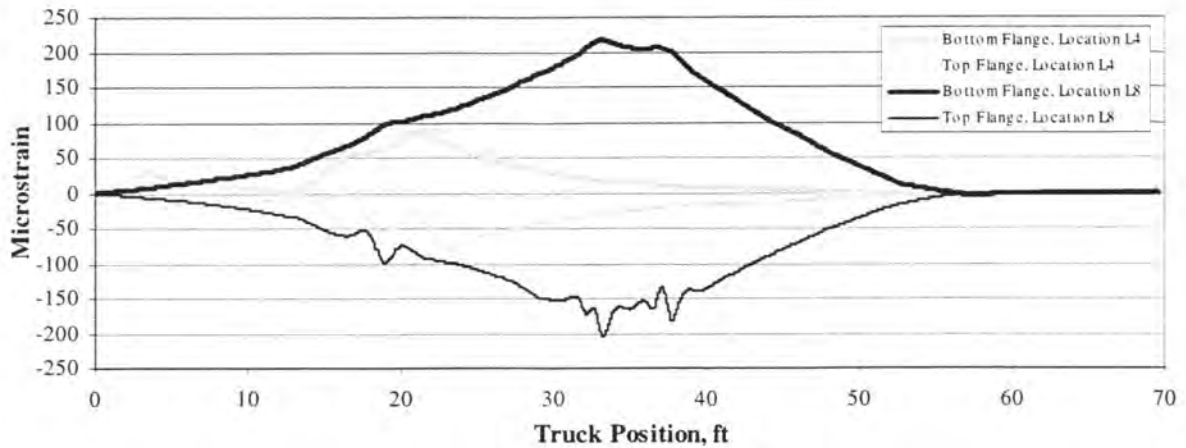


b. Half full truckload.

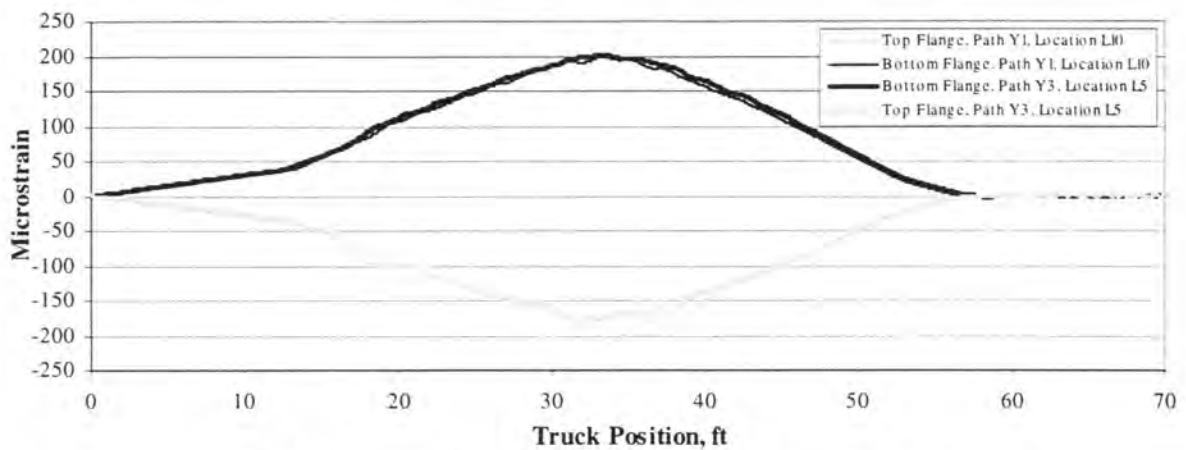


c. Empty truck.

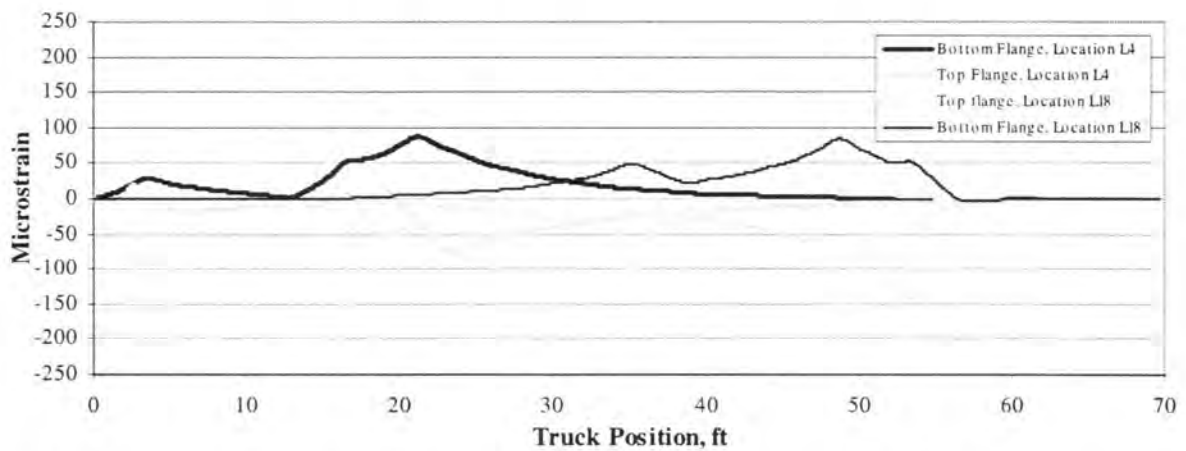
Figure 5.8. Bridge #1: Typical strain plots at Location L5 using Path Y3.



a. Experimental strains for Path Y3 near the abutment and at midspan for an interior girder.

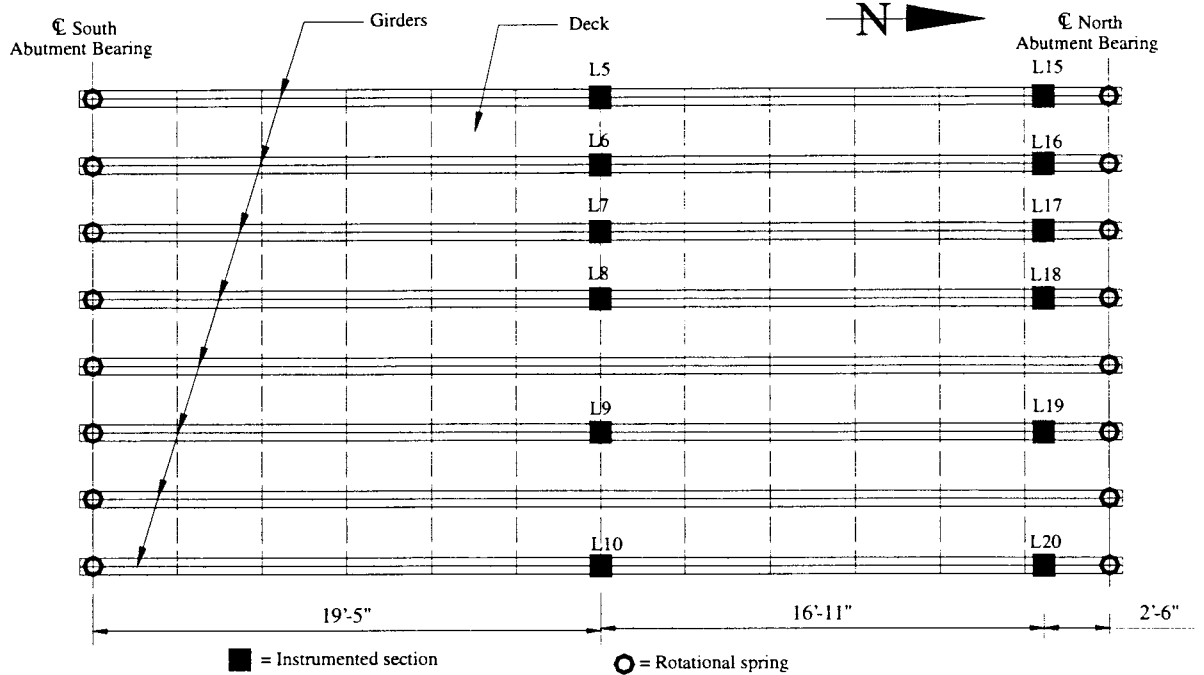


b. Experimental strains verifying transverse symmetry.

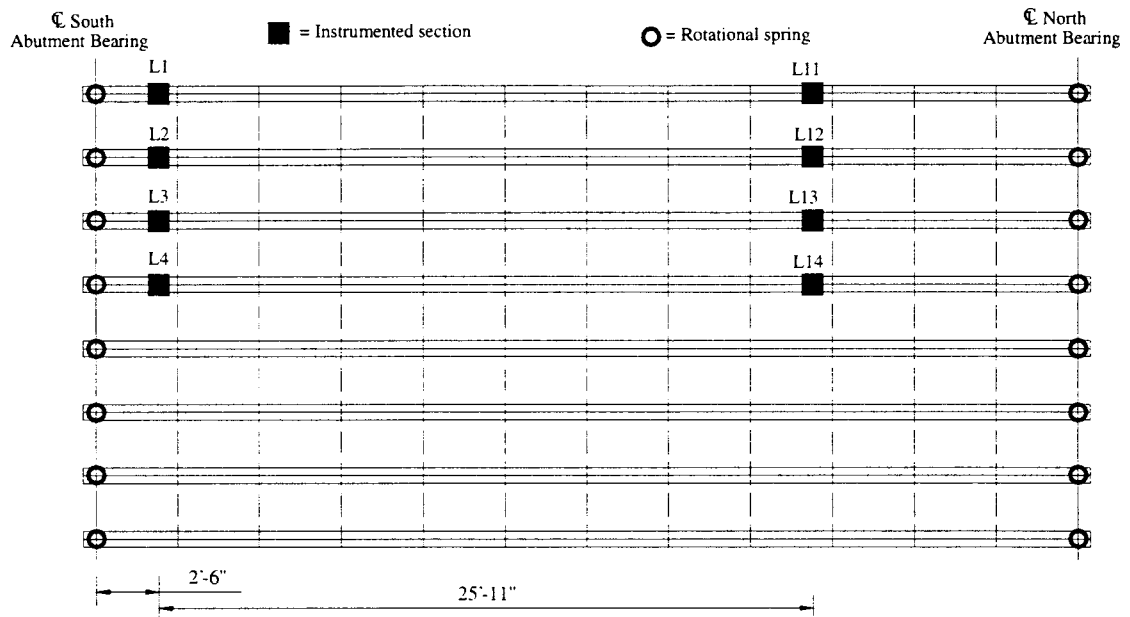


c. Comparison of experimental strains for bottom flanges to identify longitudinal strain symmetry.

Figure 5.9. Bridge #2: Typical data for end restraint, non-composite action and strain symmetry.



a. Gage instrumentation included in the optimization process.



b. Gage instrumentation for predicting strains using the optimized model.

Figure 5.10. Bridge #2: Bridge mesh, gage locations and section property names.

Table 5.15. Bridge #2: Adjustable parameters for Model 1.

Section	Property	Units	Initial	Optimized
Girder	I_y	in^4	1,230	1,255
Timber deck	E	ksi	1,000	845
Spring (rotational)	K_y	in-k/rad	0	29,210 ^a

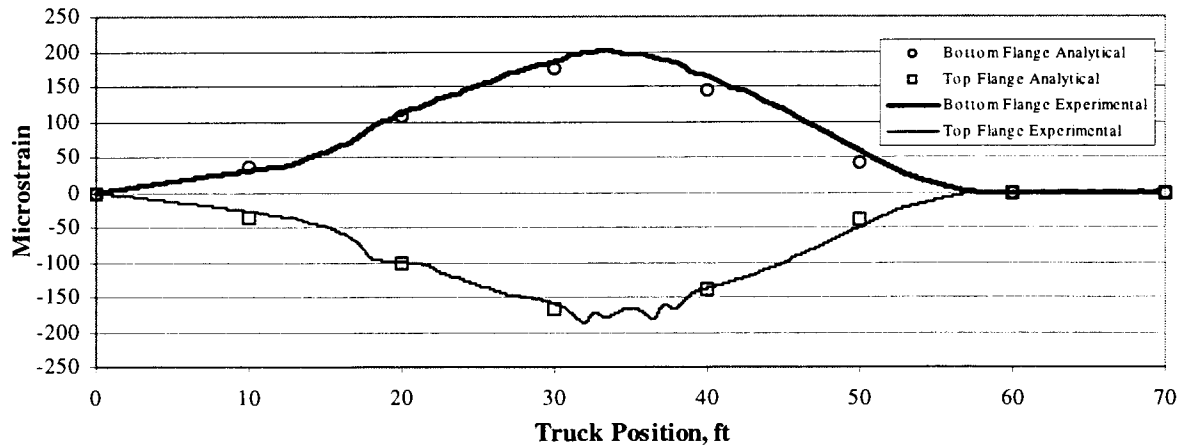
^a Corresponds to approximately 8 % fixity.

neutral axis location for an exterior girder is approximately at mid depth as shown in Fig. 5.9a), so the exterior girders were not distinguished from the interior girders. The girder section was modeled with beam elements. The timber deck was modeled with quadrilateral plate elements with a uniform all optimized parameters (excluding the springs) compare very well with the initial parameters. The magnitude of the optimized spring value (29,210 in-k/rad) is insignificant as previously discussed. The accuracy of the model is shown graphically in Fig. 5.11 for gages at the locations shown in Fig. 5.10a. Figure 5.11a compares exterior girder strains at midspan, Fig. 5.11b shows interior girder strains at midspan, and Fig. 5.11c illustrates interior girder strains near the abutment. All results compare well: Table 5.16 summarizes the model accuracy and verifies the good correlation. The initial model assuming a simply supported condition and the initial section property values results in an error of only 4.6 %. This low initial value verifies that the bridge does not exhibit significant end restraint and that the girders are non-composite. The optimized error of 1.8 % implies a very good correlation between the experimental and analytical data.

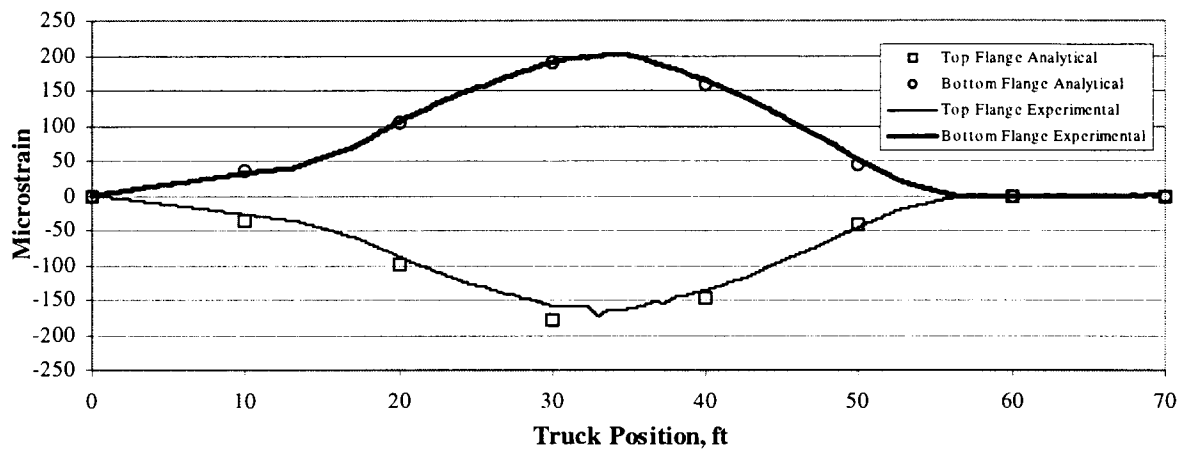
Table 5.16. Bridge #2: Model accuracy for initial and optimized model (Model 1).

Statistical Term	Units	Initial	Optimized
Total Error	microstrain	3,740	2,055
% Error	%	4.6	1.8
% Scale Error	%	6.1	1.5
Correlation Coefficient	N/A	0.99	0.99

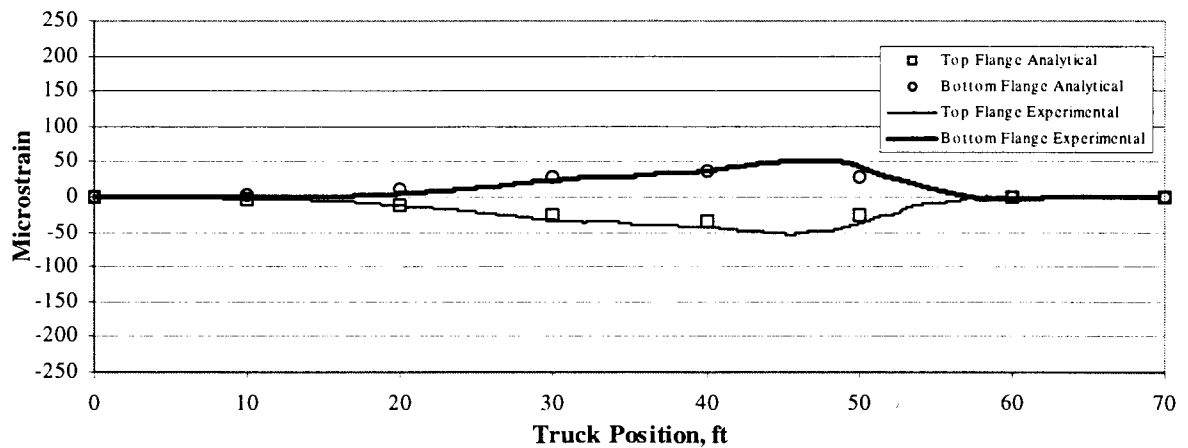
The rating model was created by using the optimized model with the appropriate rating trucks and by applying dead load to the structure. Dead load applied to the structure includes the self-weight of the steel girders and a four-in. thick timber deck, a 6 in. x 15 in. wood curb applied on the exterior girders, a weight of 25 lb/ft distributed uniformly over both exterior girders to take into account the steel rail on top of the wood curb, a uniform load distributed over the interior beams to take into



a. Location L5.



b. Location L7.



c. Location L17.

Figure 5.11. Bridge #2: Typical strain plots for Path Y3 using optimized strains.

account the dead load of the diaphragms, and an additional 6-in. deep gravel overlay on top of the timber deck. For rating purposes, the following truck paths were considered:

- Paths A and B: The outer wheel line two ft from each curb.
- Paths C, D, E and F: The outer wheel line on the four interior girders to the far East.
- Path G: The outer wheel line on the interior girder to the far West.
- Path H: The truck centered across roadway width.

Each path was analyzed at 6 in. intervals in the longitudinal direction. The bridge was designed as a single-lane bridge, so no truck path combinations were created. Individual member capacities were calculated following appropriate AASHTO Standard Specifications (4) and are presented in Appendix D. Table 5.17 and Table 5.18 show the ratings by the LFD Method (by applying AASHTO Standard Specifications (4)) and by using the BDI Software, respectively. Table 5.19 summarizes the percent difference in inventory ratings between the LFD Method and the BDI Method (note: a positive percent difference indicates that the BDI Software rating value is greater than the LFD Method rating value). The critical rating condition is for flexure at the interior girder (0.92 by the LFD Method and 1.31 by the BDI Method for a difference of 42 %). It should be pointed out that lane loadings were investigated in accordance with AASHTO Standard Specifications (4) and found to be not critical.

Table 5.17. Bridge #2: Design Truck Rating Factors by the LFD Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Interior Girders	0.92	1.53	3.94	6.57	1.16	1.94	5.76	9.62	1.17	1.95	5.32	8.87
Exterior Girders	1.00	1.67	4.22	7.04	1.27	2.12	6.41	10.70	1.27	2.13	5.91	9.87

Table 5.18. Bridge #2: Design Truck Rating Factors by the BDI Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Interior Girders	1.31	2.18	4.78	7.97	1.58	2.64	6.09	10.16	1.75	2.92	6.63	11.06
Exterior Girders	1.54	2.57	7.61	12.70	1.97	3.29	11.56	19.29	1.99	3.33	10.37	17.31

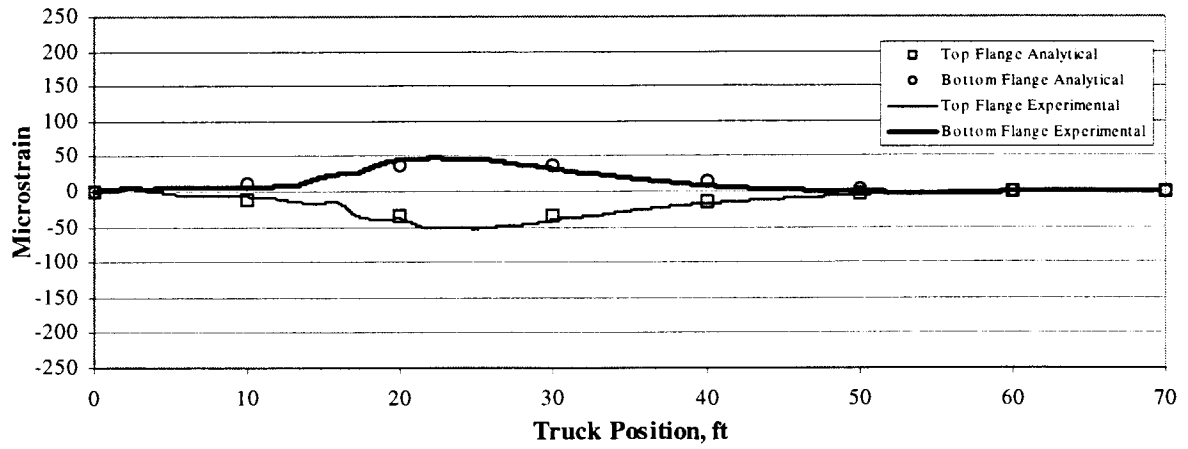
Table 5.19. Bridge #2: Percent difference in Design Truck Rating Factors between LFD Method and BDI Software.

Section	HS-20		H-20		Type-3	
	Flexure	Shear	Flexure	Shear	Flexure	Shear
Interior Girders	42.4	21.3	36.2	5.7	49.6	24.6
Exterior Girders	54.0	80.3	55.1	80.3	56.7	75.5

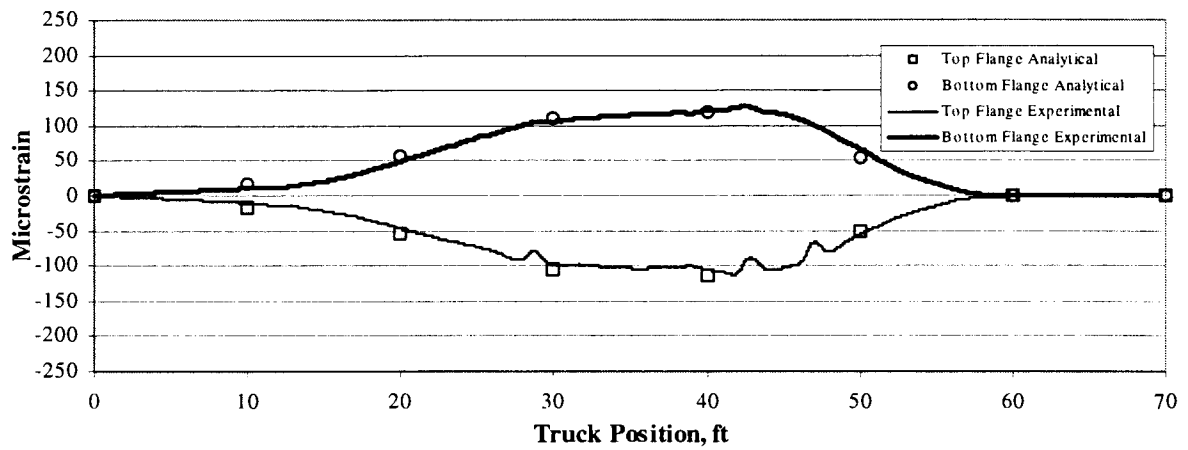
As previously described, gages used in the testing were located near the abutments, at midspan and at the quarter-span near one end as shown in Fig. 4.11b. However, the gages included in the optimization process are shown in Fig. 5.10a (gage locations used in the optimization process for Bridge #2 are the same as for Bridge #1) and were located at midspan and near the North abutment. After the optimized model was obtained (based on the limited number of gages), the bridge was analyzed to predict the behavior at the locations not used in the optimization process (shown in Fig. 5.10b). The purpose of this study was to verify that it is possible to predict strains at locations where no gages are attached. It was found that the predicted strains (shown in Fig. 5.12) correlate very well with the experimental strains. The model accuracy with all gages included (including the gages not used in the optimization process) using the optimized model is presented in Table 5.20 and shows an error of 2.1 %.

Table 5.20. Bridge #2: Model accuracy for the optimized model including gage instrumentation for predicted strains.

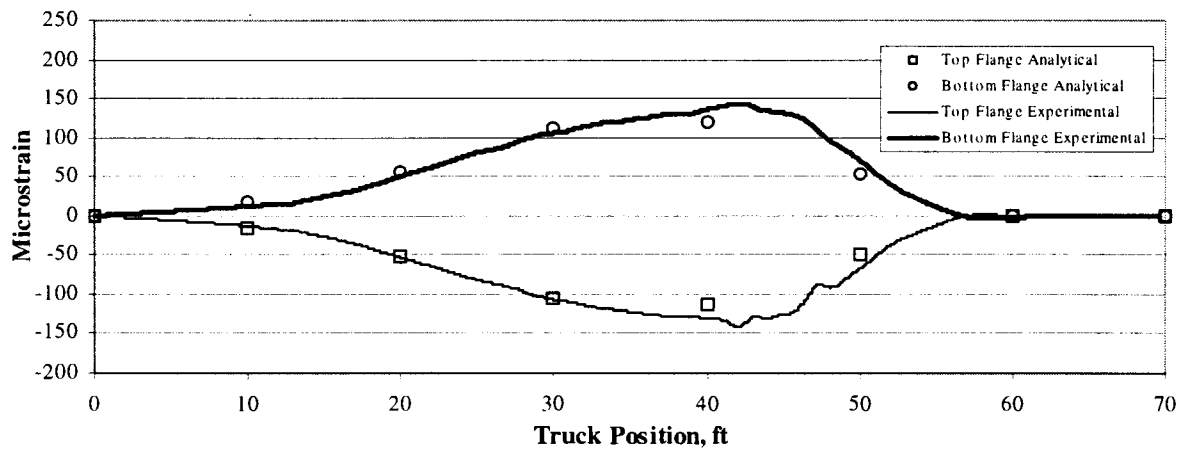
Statistical Term	Units	Optimized
Total Error	microstrain	3,304
% Error	%	2.1
% Scale Error	%	1.9
Correlation Coefficient	N/A	0.99



a. Location L3.



b. Location L11.



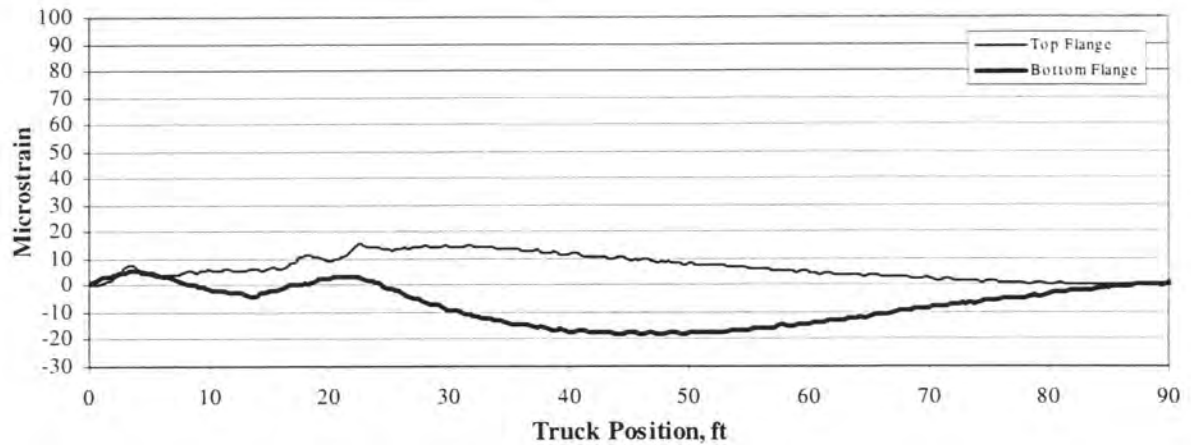
c. Location L13.

Figure 5.12. Bridge #2: Typical strain plots for Path Y3 using predicted strains.

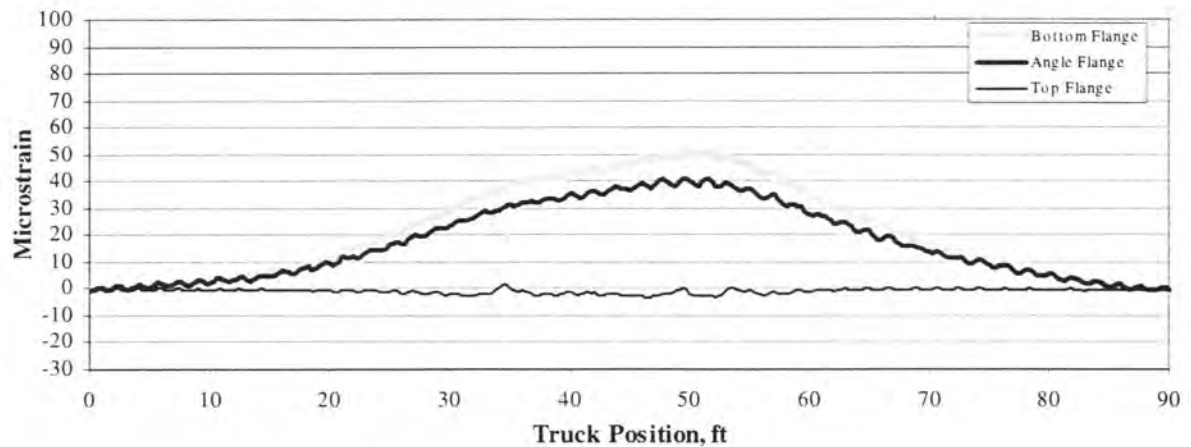
5.4. BRIDGE #3

As mentioned previously, it was anticipated that this bridge would not exhibit significant end restraint as the beams are not integral with the abutments. However, experimental results, as shown for typical strains on the girder near the abutment in Fig. 5.13a, indicate the presence of end restraint due to compression in the bottom flange. Further, as can be seen in Fig. 5.13b, the neutral axis is located near the top flange, hence composite action for the girder is verified. Figure 5.13c and Fig. 5.14a indicate that the neutral axis is located approximately in the top flanges for the stringers and the floor beams indicating the presence of composite action. Moreover, experimental strains are presented in Figs. 5.14b and 5.14c to illustrate transverse and longitudinal strain symmetry, respectively.

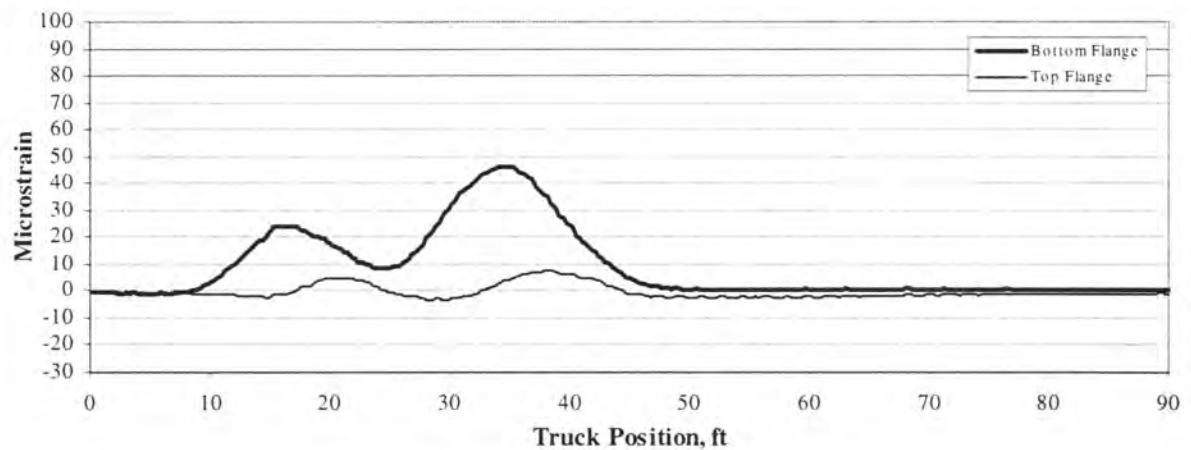
From the results described above, the analytical model shown in Fig. 5.15 was developed. Since end restraint was present in the experimental data, rotational springs were included for the girders at the centerline of the abutment bearings to verify this behavior. Four different sections for the main girders (all sections were previously described and account for the cover plates and the angle) that were used (Girder no angle, Girder no cover, Girder first cover and Girder second cover), three sections for the floor beams were used (25"8 Beth I 85.5, 27" Beth I 100, and 28" Beth I 113 as shown in the Steel Manual of 1930 (7)), and two sections for the exterior beams were used (Exterior beam at end, and Exterior beam at midspan) in the model. As described previously and shown in Fig. 4.14c, Bridge #3 has non-uniform transverse members between the exterior beams and the main girders. It is not possible to model non-uniform sections with the BDI Software; however, to approximate the behavior, each non-uniform member was divided into three uniform sections where each section was assigned average properties. The non-uniform members were also separated into two parts: one near the abutment and one near midspan. Hence, six different sections were created (i.e., End Plate 16.0, End Plate 19.7, End Plate 23.4, Int Plate 18.1, Int Plate 21.8 and Int Plate 25.5, where the numbers indicate the steel depth) to complete the model. Typical data verifying composite action are presented in Fig. 5.13b for the main girder, in Fig. 5.13c for the stringers, and in Fig. 5.14a for the floor beams. As a result, all sections were modeled as composite sections. Since some beam sections were modeled where no gages were attached, master-slave parameters were created for those sections (for these parameters, the slave parameter changes proportionally to the master parameter so that the ratio of the final optimized inertia-values for the two parameters (one slave and one master variable) is the same as the initial inertia-ratio). For this bridge, four slave parameters were selected in the optimization process since no gages were installed on these sections, where each of the four parameters was assigned to a corresponding master variable:



a. Strains on a girder near the abutment (Location L1).

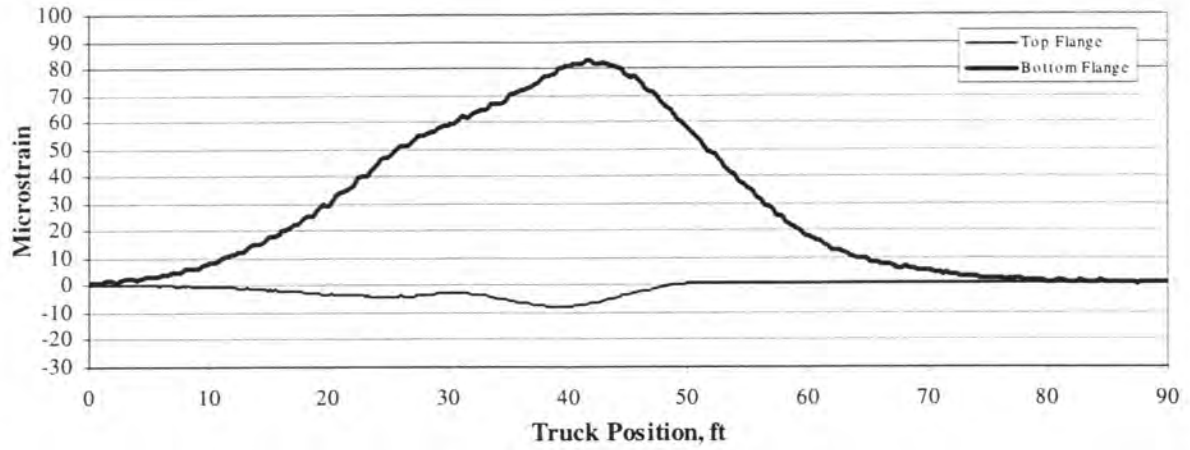


b. Strains on a girder at midspan (Location L7).

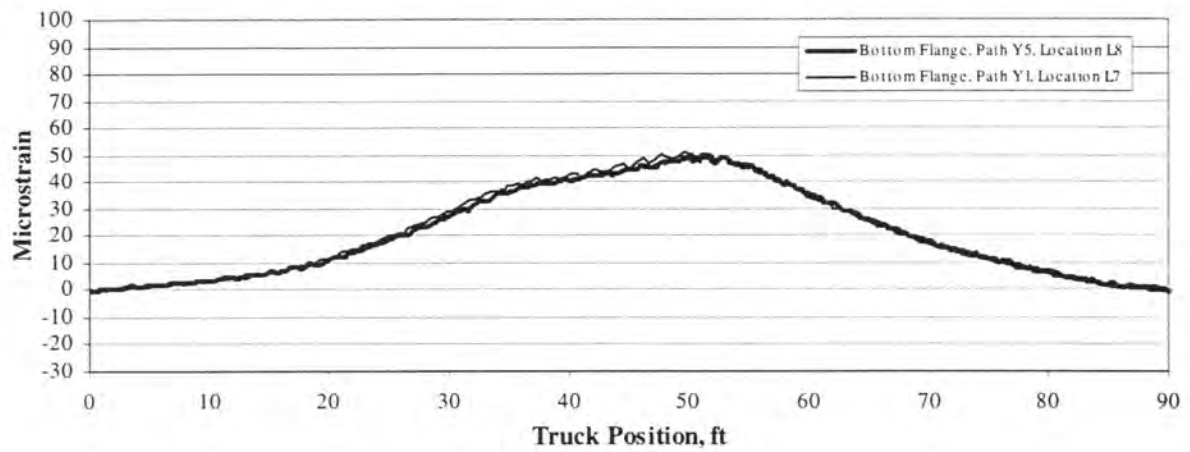


c. Strain on a stringer at midspan (Location L12).

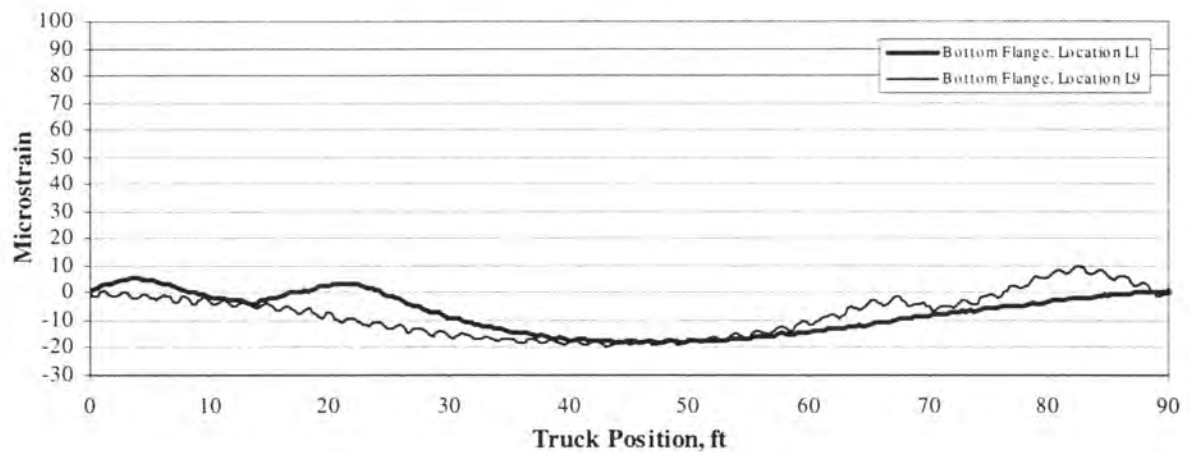
Figure 5.13. Bridge #3: Experimental strains verifying end restraint and composite action.



a. Strains on a floor beam at midspan (Location L16).



b. Transverse strain symmetry.



c. Longitudinal strain symmetry for Path Y1.

Figure 5.14. Bridge #3: Experimental strains verifying composite action and strain symmetry.

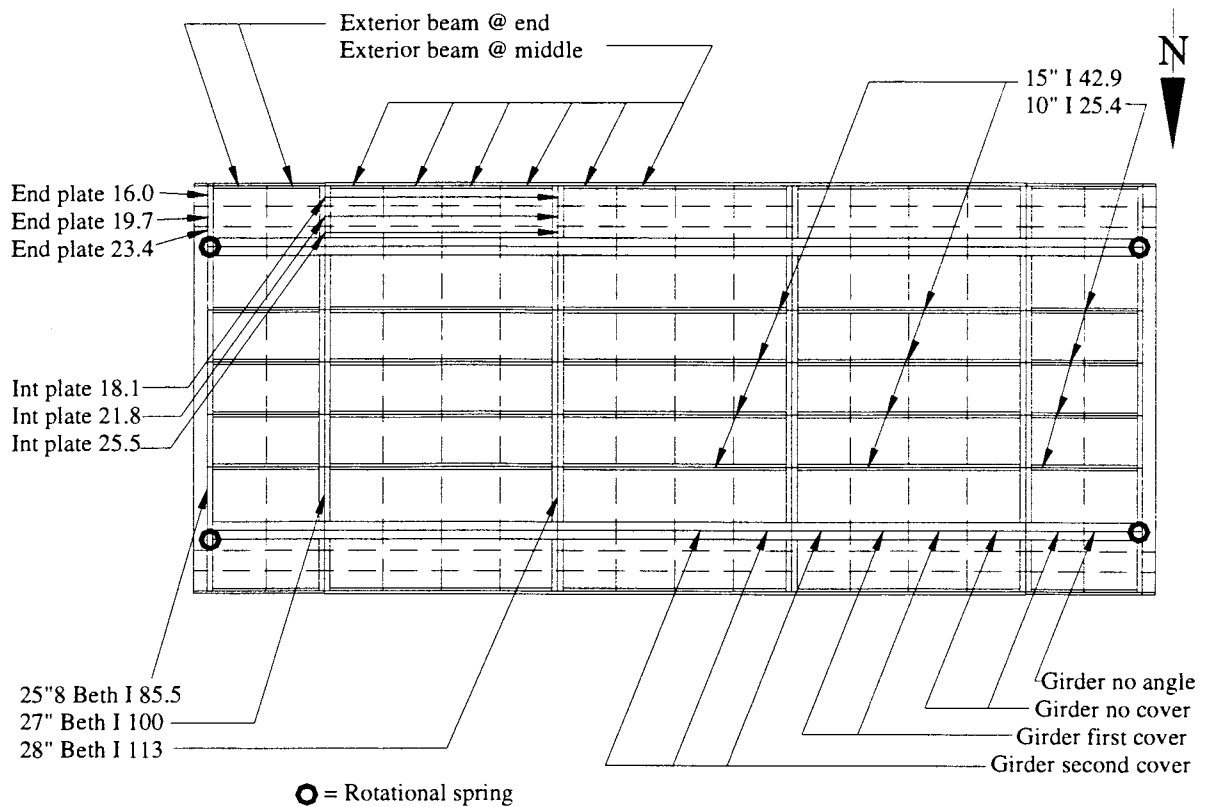


Figure 5.15. Bridge #3: Mesh of analytical model and section property names.

- Girder with no cover plates was a slave to the Girder first cover (main girder).
- 25"8 Beth I 85.5 was a slave to 28" Beth I 113 (floor beam).
- 27" Beth I 100 was a slave to 28" Beth I 113 (floor beam).
- 10" I 25.4 was a slave to 15" I 42.9 (stringer).

All girders, stringers, and floor beams were modeled with beam elements, and the concrete deck was modeled with quadrilateral plate elements with a uniform thickness. Table 5.21 summarizes the optimized parameter results. These results indicate that the optimized parameters (excluding the springs) compare well with the initial parameters. Also, for reference, non-composite and composite section properties corresponding with AASHTO Standard Specifications (4) are also summarized in Table 5.21. Note, the optimized values were limited to a minimum of 80 % of the non-composite values to a maximum of 120 % of the composite values. The parameters not included in the optimization process are listed in Table 5.22.

Table 5.21. Bridge #3: Adjustable parameters.

Section	Property	Units	Non-Composite	Composite	Initial	Optimized
25"8 Beth I 85.5	I_y	in^4	2,600	7,550	7,550	9,050
27" Beth I 100	I_y	in^4	3,725	10,280	10,280	12,340
28" Beth I 113	I_y	in^4	4,285	11,440	11,440	13,710
10" I 25.4	I_y	in^4	122	701	701	840
15" I 42.9	I_y	in^4	442	1,945	1,945	2,335
Girder no angle	I_y	in^4	21,360	46,400	46,400	47,350
Girder no cover	I_y	in^4	26,630	64,490	64,490	77,150
Girder first cover	I_y	in^4	30,290	76,630	76,630	91,840
Girder second cover	I_y	in^4	32,070	82,800	82,800	99,230
Spring (rotational)	K_y	in-k/rad	N/A	N/A	0	7,547,000 ^a
Deck	E	ksi	N/A	N/A	3,300	3,925

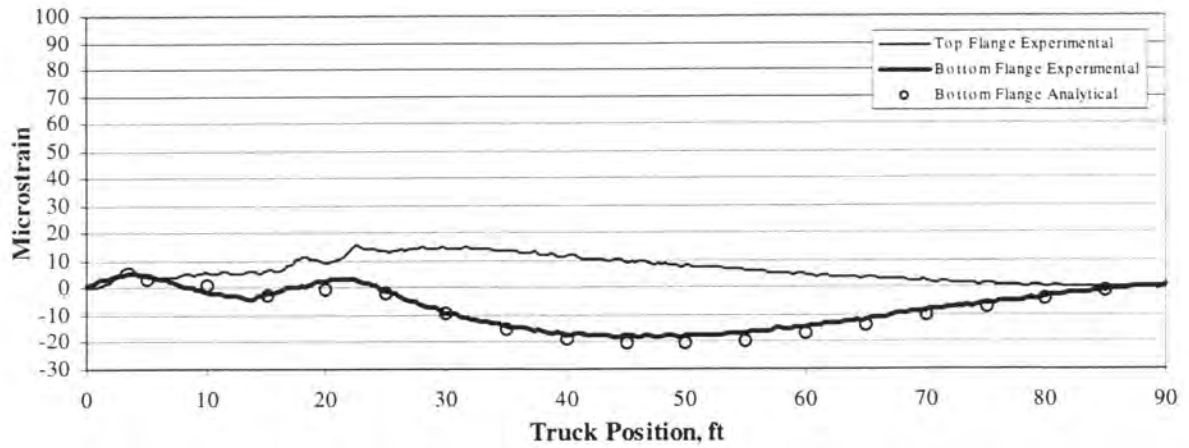
^a Corresponds to approximately 40 % fixity.

Table 5.22 Bridge #3: Section properties for non-optimized parameters.

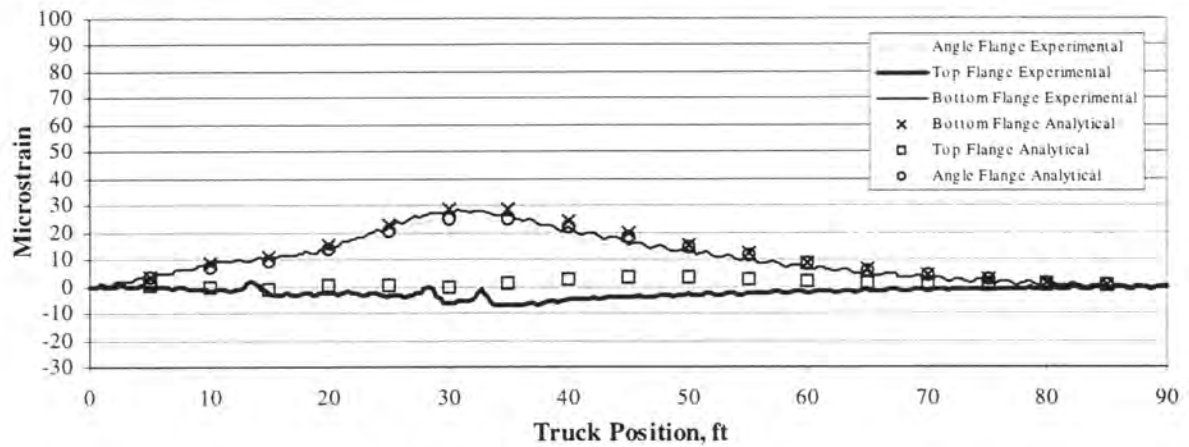
Section	Property	Units	Non-Composite	Composite	Fixed value
Exterior beam at end	I_y	in^4	122	11,260	1,616*
Exterior beam at middle	I_y	in^4	442	13,870	1,936*
End plate 16.0	I_y	in^4	434	N/A	434
End plate 19.7	I_y	in^4	716	N/A	716
End plate 23.4	I_y	in^4	1,110	N/A	1,110
Int plate 18.1	I_y	in^4	710	N/A	710
Int plate 21.8	I_y	in^4	1,110	N/A	1,110
Int plate 25.5	I_y	in^4	1,630	N/A	1,630

* Calculated as the sum of steel beam, concrete slab, and curb.

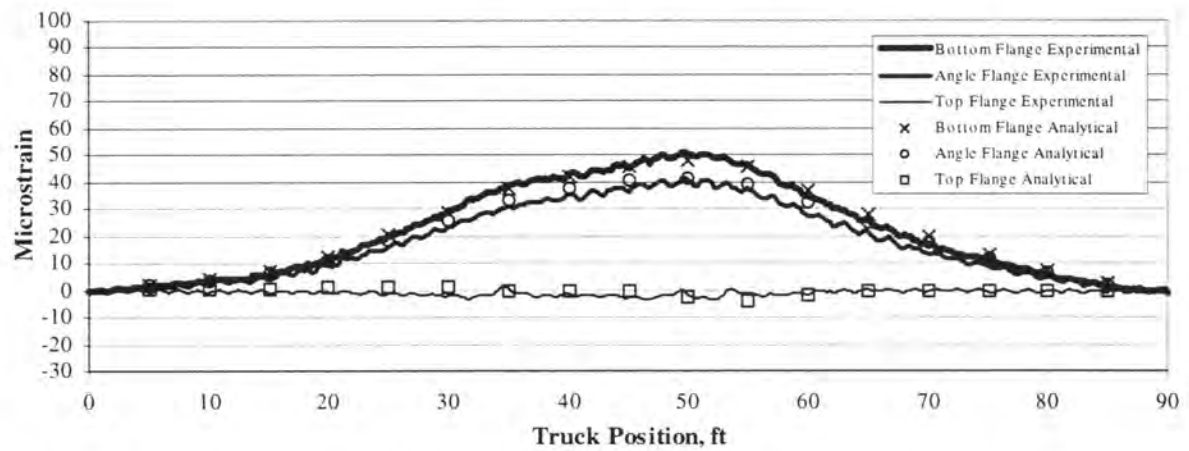
The accuracy of the model is shown graphically in Fig. 5.16 and Fig. 5.17 for various truck paths and various locations and generally indicates that the model predicts the bridge behavior. Table 5.23 summarizes the statistical accuracy and verifies a good correlation since the optimized model has an error of 7.4 % and a correlation coefficient of 0.97. Note, the initial error of 69.4 % can be primarily attributed to the presence of significant end restraint.



a. Location L1 (Girder no angle).

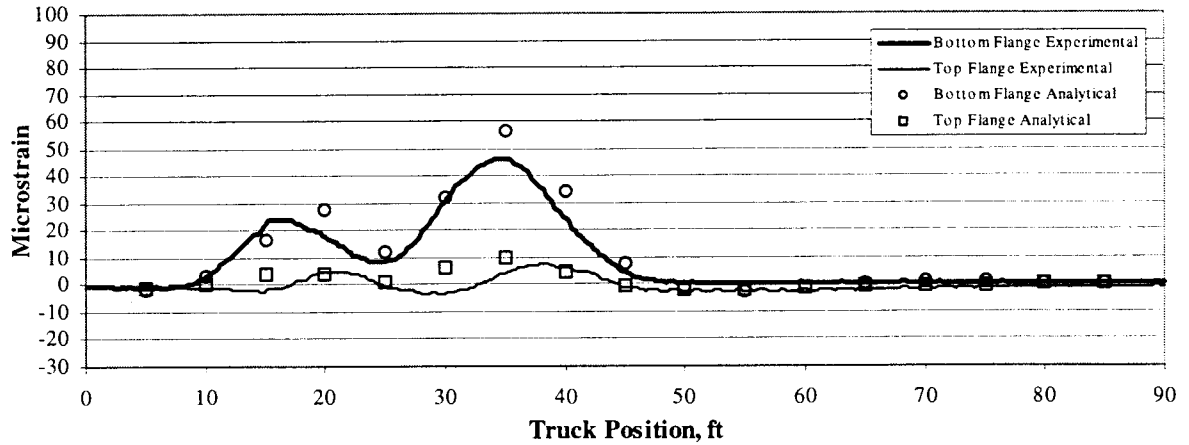


b. Location L3 (Girder first cover).

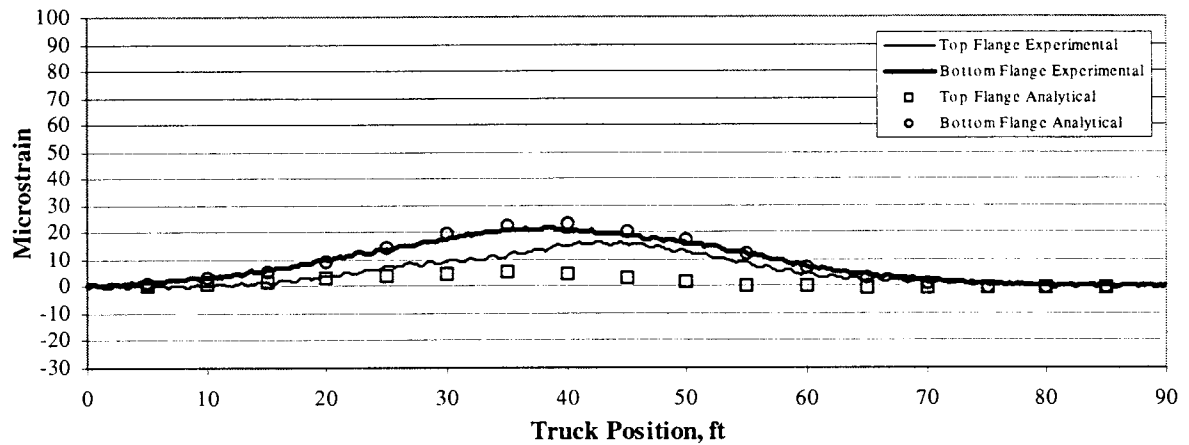


c. Location L7 (Girder second cover).

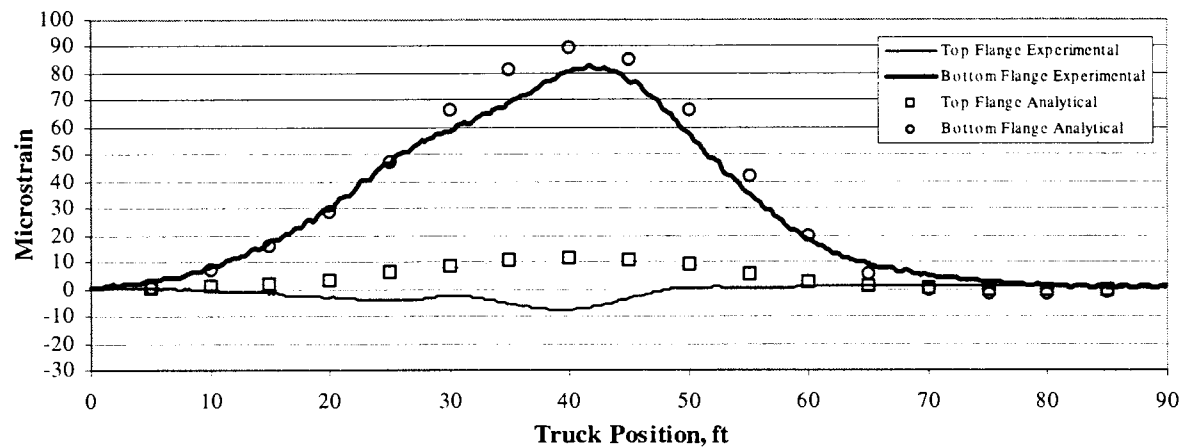
Figure 5.16. Bridge #3: Typical strain plots on the girders for truck Path Y1.



a. Location L12 (Stringer) for truck Path Y3.



b. Location L15 (Floor beam) for truck Path Y4.



c. Location L16 (Floor beam) for truck Path Y4.

Figure 5.17. Bridge #3: Typical strain plots on the stringers and floor beams.

Table 5.23 Bridge #3: Model accuracy for initial and optimized model.

Error	Units	Initial	Optimized
Total Error	microstrain	14,372	4,618
Percent Error	%	69.4	7.4
Scale error	%	22.7	9.4
Correlation coefficient	-	0.87	0.97

The rating model was created by using this optimized model with the appropriate rating trucks and by applying dead load to the structure. Dead load applied to the structure includes the self-weight of all steel sections, the concrete deck, and the concrete curb and parapet. In addition, a 1.89-in. thick overlay was included. For rating purposes, the following truck paths were considered:

- Path A: The passenger side wheel line 2 ft from the North curb.
- Path B: Truck positioned 10 ft to the South of Path A.
- Path C: The driving side wheel line on the second stringer from the North.
- Path D: Truck positioned 10 ft to the South of Path C.

Each path was analyzed at 1 ft intervals in the longitudinal direction. The bridge was designed as a two-lane bridge, so truck path envelopes were created to account for two trucks being on the bridge at the same time (Note: AASHTO Standard Specifications (4) stipulates that the distance between two rating trucks should be 4 ft when used at the same time):

- Envelope 1: Path A combined with Path B.
- Envelope 2: Path C combined with Path D.

Individual member capacities were calculated following appropriate AASHTO Standard Specifications (4). Ratings by the LFD Method (by applying AASHTO Standard Specifications (4)) and by using the BDI Software are presented in Table 5.24 and Table 5.25, respectively. Table 5.26 summarizes the percent difference in inventory ratings between the LFD Method and the BDI Method. The critical rating condition is for shear at 10" I 25.8, which is one of the stringer sections (1.32 by the LFD Method and 1.14 by the BDI Method for a difference of 13.6 %). Note that the large BDI rating values for flexure on the Girder no angle are attributed to small BDI live load moments near the abutment (due to more accurate live load distribution and the end restraint), which results in very large ratings. These ratings will also result in very large percent errors. The relatively large rating factors by the LFD Method for flexure on the girder (i.e., 1.43 at midspan for the HS-20 truck) is credited to the angles included in the calculations (they were determined to be effective based on the experimental results). Further, the large percent difference between BDI Method ratings and LFD

Method ratings are attributed a more accurate load distribution by using the BDI Method. It shall be pointed out that lane loadings were investigated and were determined not to be critical.

Table 5.24 Bridge #3: Design Truck Rating Factors by the LFD Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Beth I 85.5	2.60	4.34	2.11	3.52	2.60	4.34	2.11	3.52	3.17	5.29	2.58	4.31
Beth I 100	2.00	3.34	1.57	2.62	2.28	3.81	1.79	2.99	2.55	4.26	2.00	3.34
Beth I 113	2.03	3.39	1.62	2.70	2.41	4.02	1.93	3.22	2.50	4.17	2.00	3.34
10" I 25.8	2.54	4.24	1.32	2.20	2.54	4.24	1.32	2.20	4.80	8.01	1.60	2.67
15" I 42.9	2.50	4.17	2.23	3.72	2.50	4.17	2.55	4.26	3.05	5.09	2.84	4.74
Girder no angle	2.11	3.52	2.29	3.82	3.40	5.68	3.72	6.21	2.94	4.91	3.20	5.34
Girder no cover	1.85	3.09	2.50	4.17	2.93	4.89	4.02	6.71	2.56	4.27	3.47	5.79
Girder first cover	1.57	2.62	2.88	4.81	2.42	4.04	4.57	7.63	2.16	3.61	4.00	6.68
Girder second cover	1.43	2.39	3.55	5.93	2.19	3.66	5.47	9.13	1.96	3.27	4.87	8.13

Table 5.25 Bridge #3: Design Truck Rating Factors by the BDI Method^a.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Beth I 85.5	2.33	3.89	2.58	4.31	2.42	4.04	2.61	4.36	2.78	4.64	3.23	5.39
Beth I 100	2.45	4.09	3.19	5.32	3.16	5.27	3.76	6.28	3.08	5.14	3.93	6.56
Beth I 113	2.22	3.71	3.21	5.36	3.16	5.27	4.09	6.83	2.95	4.92	4.09	6.83
10" I 25.8	4.27	7.13	1.14	1.90	4.27	7.13	1.14	1.90	5.86	9.78	2.13	3.56
15" I 42.9	3.60	6.01	3.68	6.14	3.59	5.99	4.03	6.73	4.17	6.96	4.45	7.43
Girder no angle	24.89	41.55	2.54	4.24	24.89	41.55	4.11	6.86	30.06	50.18	3.51	5.86
Girder no cover	5.90	9.85	2.63	4.39	8.92	14.89	4.25	7.09	7.93	13.24	3.61	6.03
Girder first cover	4.23	7.06	4.09	6.83	6.46	10.78	6.42	10.72	5.75	9.60	5.58	9.31
Girder second cover	3.75	6.26	4.60	7.68	5.63	9.40	6.96	11.62	5.05	8.43	6.13	10.23

^a Edge stiffening included in the analytical model.

Table 5.26 Bridge #3: Percent difference in Design Truck Rating Factors between LFD Method and BDI Software.

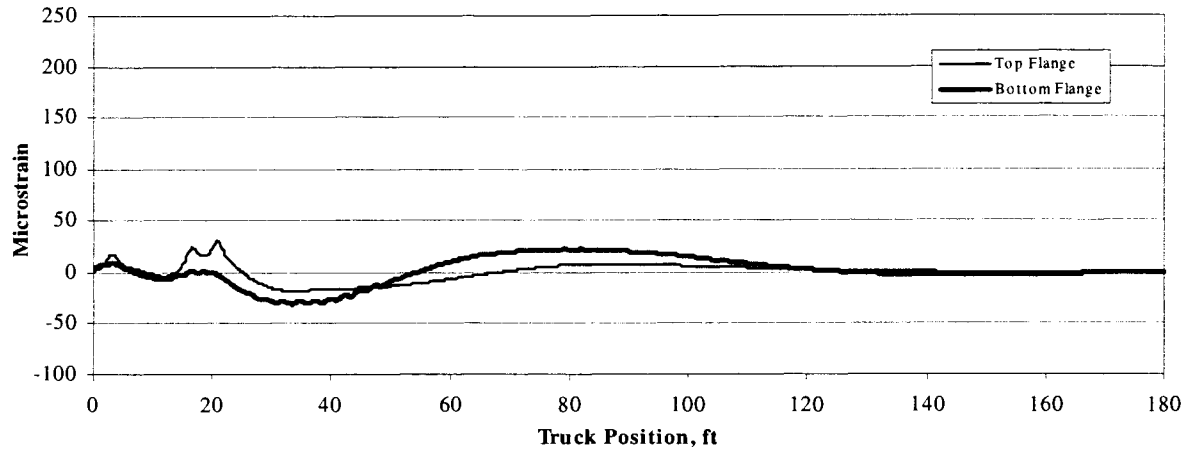
Section	HS-20		H-20		Type-3	
	Flexure	Shear	Flexure	Shear	Flexure	Shear
Beth I 85.5	-10.4	22.3	-6.9	23.7	-12.3	25.2
Beth I 100	22.5	103.2	38.6	110.1	20.8	96.5
Beth I 113	9.4	98.1	31.1	111.9	18.0	104.5
10" I 25.8	68.1	-13.6	68.1	-13.6	22.1	33.1
15" I 42.9	44.0	65.0	43.6	58.0	36.7	56.7
Girder no angle	1079.6 ^a	10.9	632.1 ^a	10.5	922.4 ^a	9.7
Girder no cover	218.9 ^b	5.2	204.4 ^b	5.7	209.8 ^b	4.0
Girder first cover	169.4 ^b	42.0	166.9 ^b	40.5	166.2 ^b	39.5
Girder second cover	162.2 ^b	29.6	157.1 ^b	27.2	157.7 ^b	25.9

^a Large percent difference due to small BDI live load moments and more accurate load distribution.

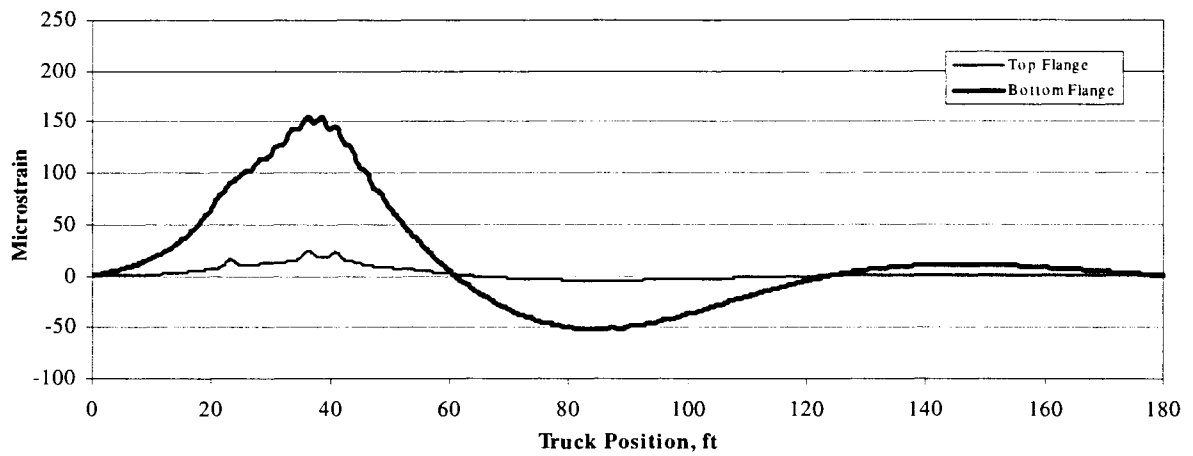
^b Large percent difference due to more accurate load distribution.

5.5. BRIDGE #4

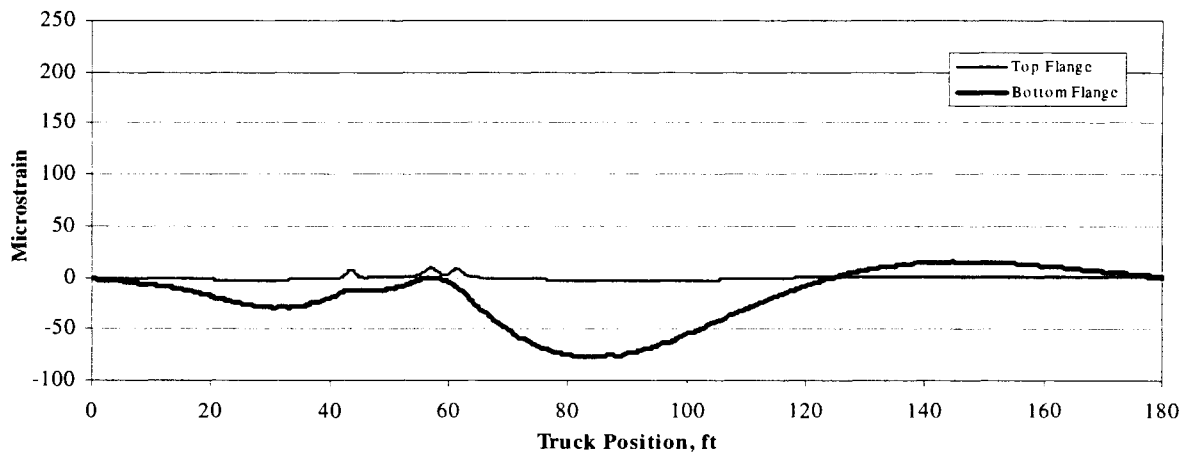
As previously mentioned, it was predicted that the bridge would not exhibit significant end restraint as the beams are not integral with the abutments. Typical experimental data on the girder near the abutment as shown in Fig. 5.18a indicates that there is some end restraint; however it is small as both flanges (top and bottom) are in compression when the truck is near the abutments and both flanges are in tension when the truck is away from the abutments. Further, since both flanges are in tension or in compression at the same time as shown in Fig. 5.18a, this indicates that the neutral axis is located near the top flange, which verifies the presence of composite action near the abutment. Experimental data for the girder section at midspan illustrated in Fig. 5.18b indicates that the neutral axis location is above the top flange, hence composite action and edge stiffening are verified for the girder section at midspan. These results are typical for all spans. Further, typical experimental data for the girder section near the piers (illustrated in Fig. 5.19c) shows that the neutral axis is located near the top flange indicating the presence of composite action (even though it was not expected) at these sections. Typical data illustrated in Figure 5.18c also indicate that the bottom flange near Pier 1 is in compression, hence there is a negative moment region near the piers. Moreover, typical experimental data for a floor beam at midspan (shown in Fig. 5.19a) and near the girder (shown in Fig. 5.19b) indicate composite action since the neutral axis locations at both locations are near the top flanges. Experimental strains are presented in Fig. 5.19c to verify transverse symmetry. Strain symmetry in



a. Strains near the South abutment at Location L2.

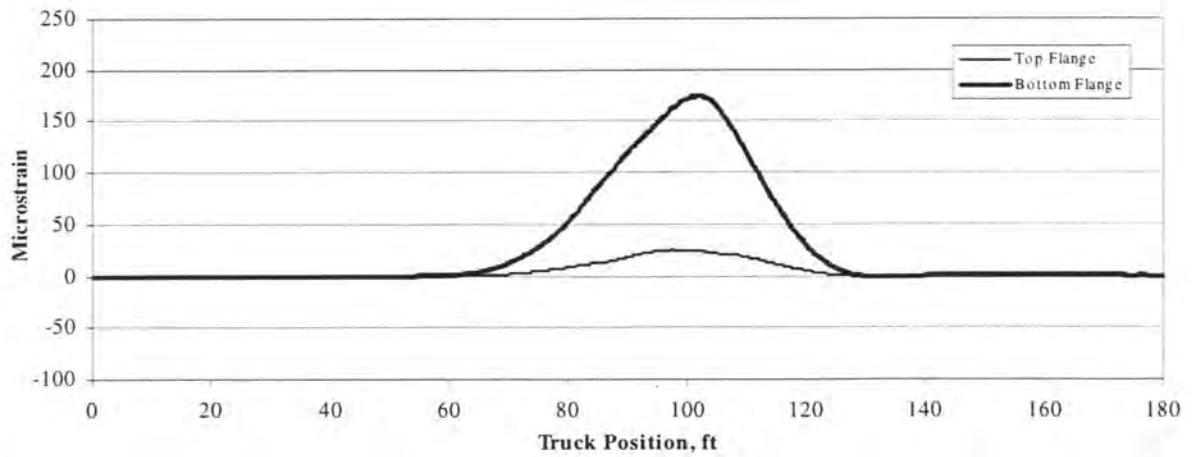


b. Strains at midspan at Location L4.

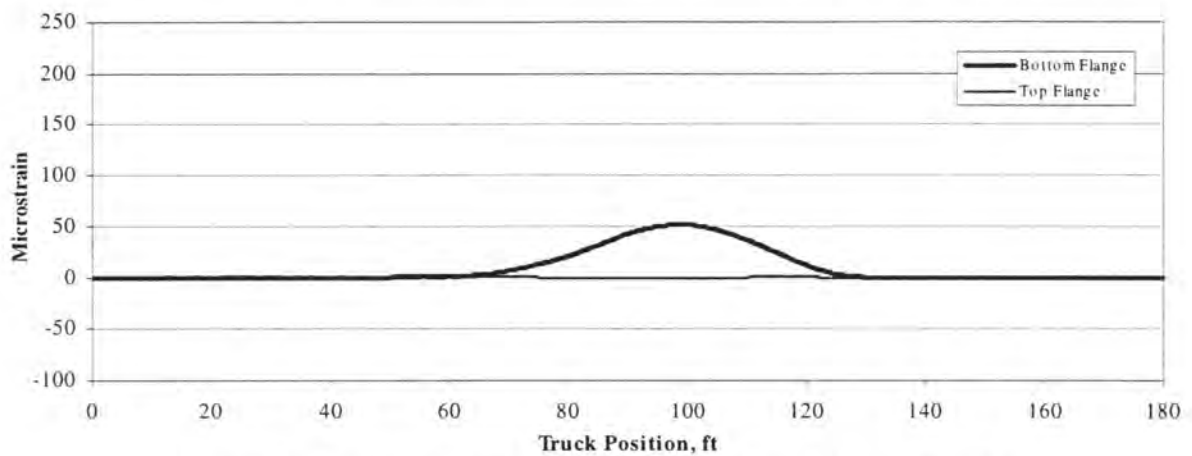


c. Strains near Pier 1 at Location L6.

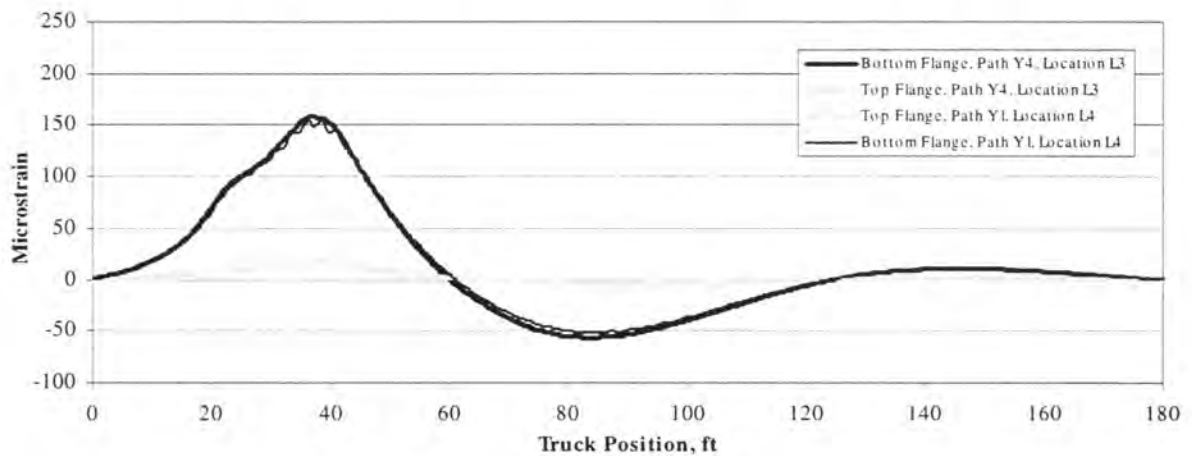
Figure 5.18. Bridge #4: Experimental data on the girders for Path Y1.



a. Strains at midspan on a floor beam at Location L15 for Path Y3.



b. Strains near the girder on a floor beam at Location L16 for Path Y3.



c. Transverse strain symmetry.

Figure 5.19. Experimental data on a floor beam and transverse strain symmetry.

the longitudinal direction was not possible to verify since gages were only installed for one half of the bridge. Strains were assumed to be symmetric since the bridge is symmetric about the bridge centerline, bearing conditions at both abutments are the same, and all structural elements appear to be in good conditions.

Based on the initial review of the data briefly discussed in the previous paragraph, an analytical model was created using four elements in the transverse direction and elements in the longitudinal directions (shown in Fig. 5.20). Rotational springs were included for the girders at the centerline of the abutment bearings. As a result of the experimental data indicating that both the girders and the floor beams behave compositely with the deck, all steel sections were modeled as composite beams in the analytical model. The girders and floor beams were modeled with beam elements, and the concrete deck was modeled with quadrilateral plate elements. Table 5.27 summarizes the optimized parameter results. These results indicate that all optimized parameters (excluding the springs) compare well with the initial parameters.

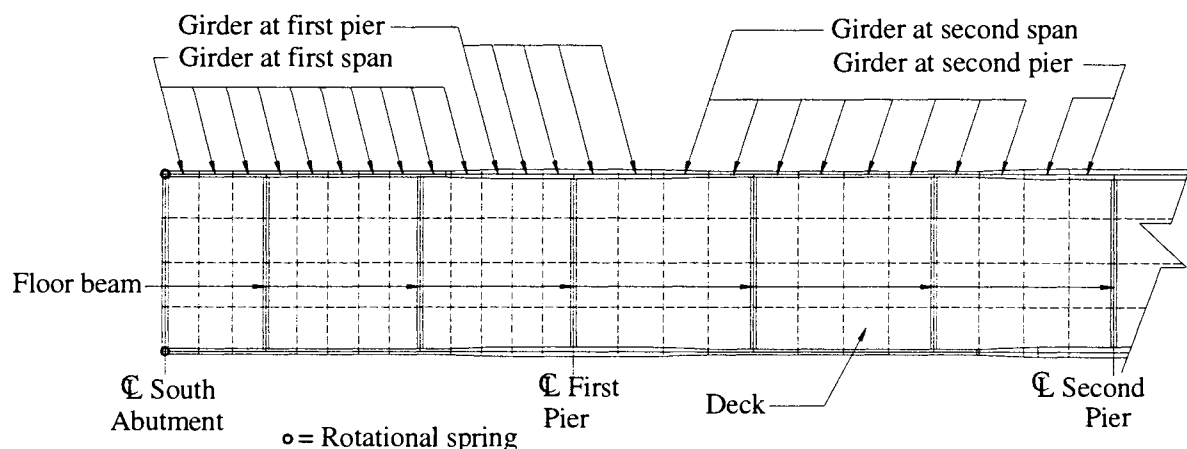
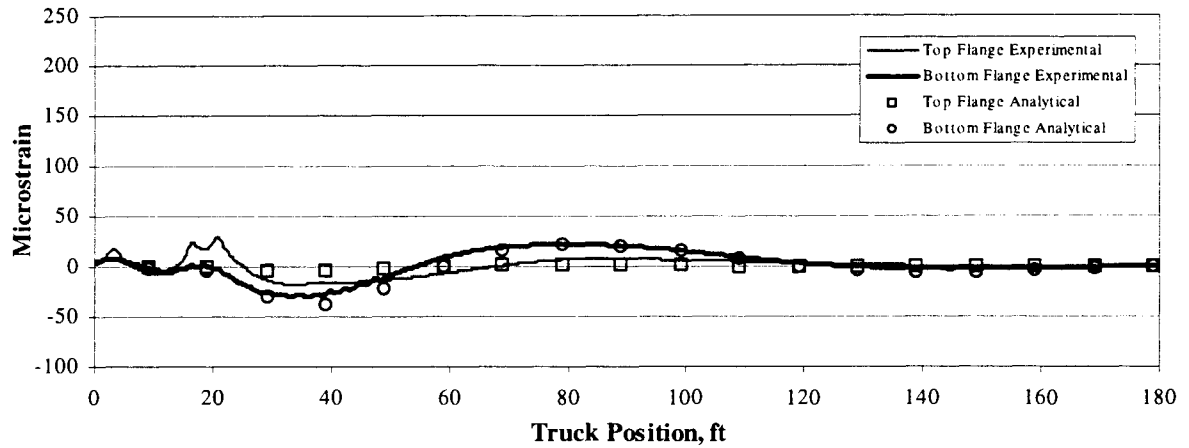
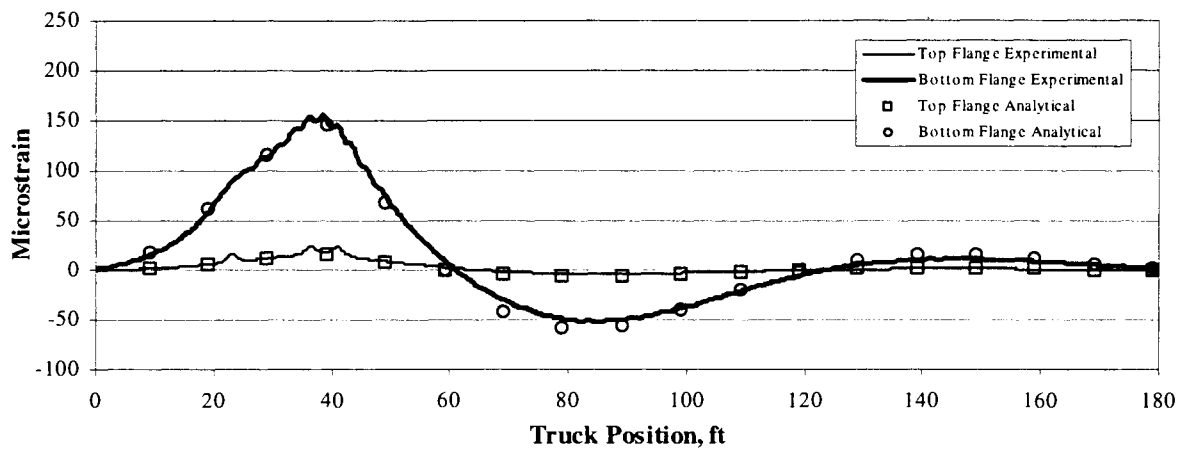


Figure 5.20. Bridge #4: Mesh of the analytical model for one half of the bridge.

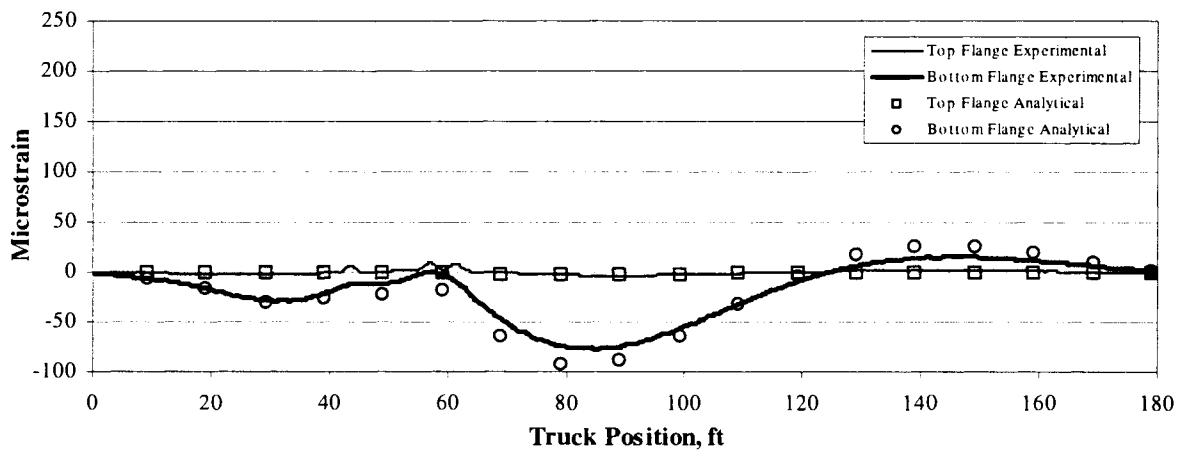
The accuracy of the generated model is shown graphically in Fig. 5.21 and Fig. 5.22 for typical data at various locations and various paths, where Fig. 5.21 illustrates typical strains on the South girder, and Fig. 5.22 presents typical strains in one of the girders at Locations L10 and L12 and one of the floor beams at Location L15. All results compare well and indicate that the model accurately predicts the bridge behavior. Table 5.28 summarizes the statistical accuracy and verifies a good correlation. The initial model assuming simply supported conditions returned an error of 10.4 % and a correlation coefficient of 0.95; with the final model, the error was reduced to 4.0 % and had a



a. Location L2

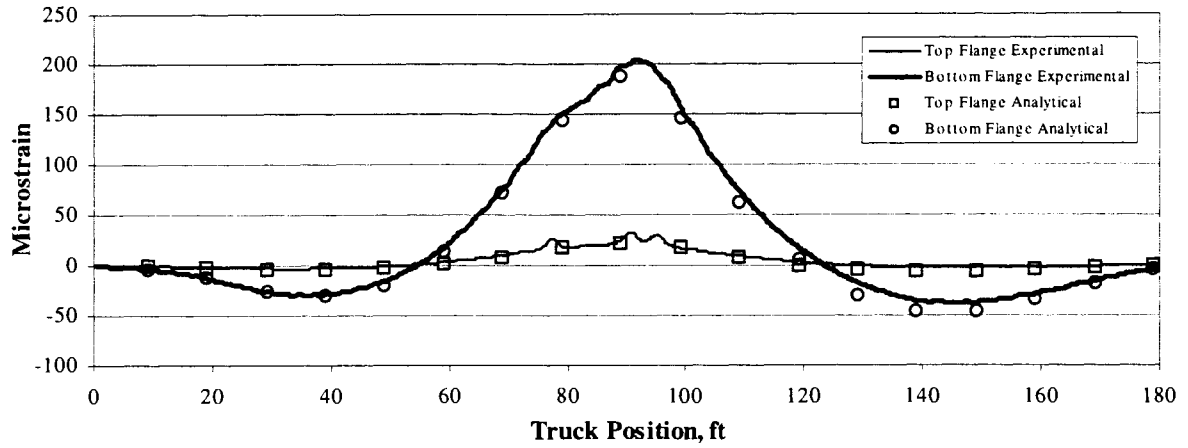


b. Location L4

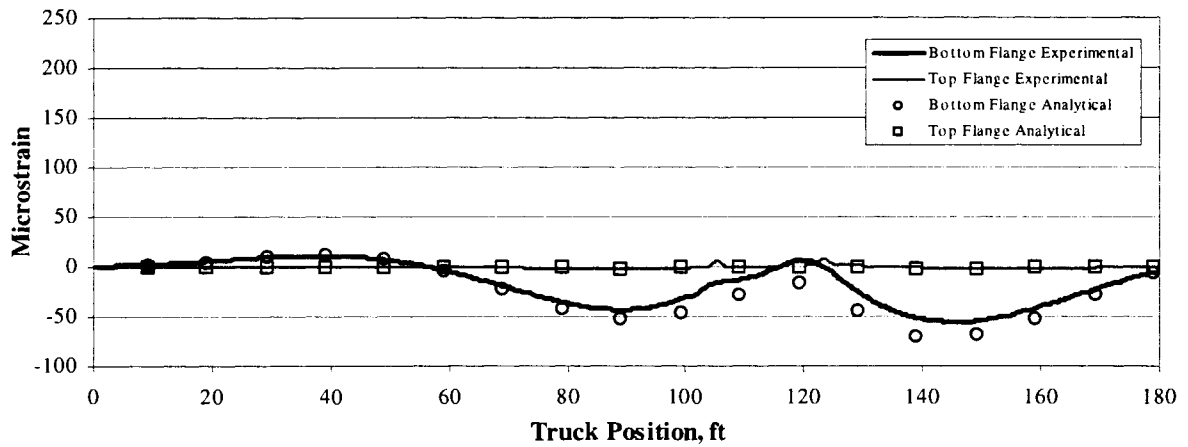


c. Location L6

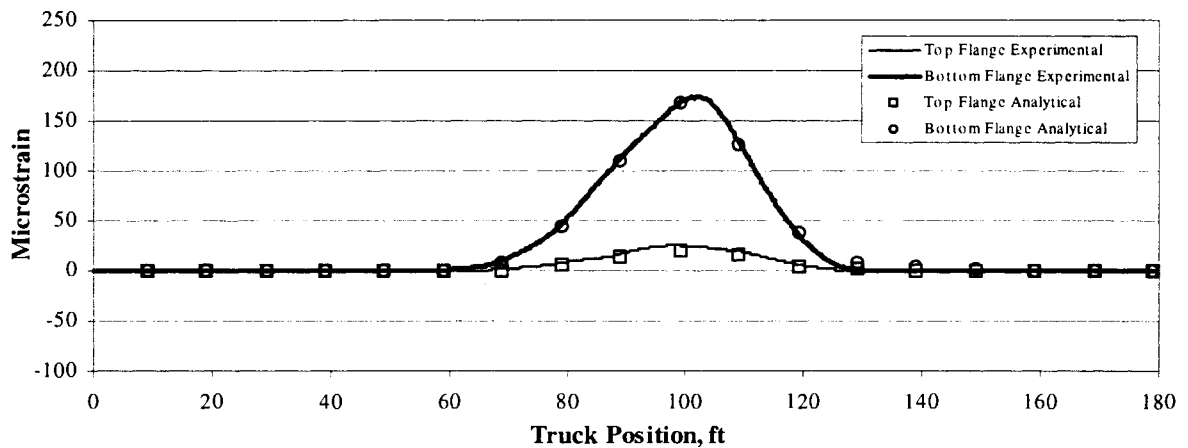
Figure 5.21. Bridge #4: Typical strains on the South girder for truck Path Y1.



a. Strains near Pier 2 at Location L10 for Path Y1.



b. Strains near Pier 2 at Location L12 for Path Y1.



c. Strains at midspan for the floor beam at Location L15 for Path Y3.

Figure 5.22. Bridge #4: Typical strain plots for truck Paths Y1 and Y3.

correlation coefficient of 0.98. These results verify the good correlation between the experimental and analytical data.

Table 5.27. Bridge #4: Adjustable parameters.

Section	Property	Units	Non-Composite	Composite	Initial	Optimized
Girder at first span	I_y	in^4	5,155	21,630	21,630	25,030
Girder at second span	I_y	in^4	5,155	21,630	21,630	24,190
Girder near first pier	I_y	in^4	11,300	35,770	35,770	37,260
Girder near second pier	I_y	in^4	12,410	37,330	37,330	44,770
Floor beam	I_y	in^4	1,085	3,905	3,905	4,755
Concrete Deck	E	ksi	N/A	N/A	3,600	2,885
Spring (rotational)	K_y	in-k/rad	N/A	N/A	0	3,455,000 ^a

^a Corresponds to approximately 30 % fixity.

Table 5.28. Bridge #4: Model accuracy for initial and optimized model.

Statistical Term	Units	Initial	Optimized
Total error	microstrain	8,301	5,974
Percent Error	%	10.4	4.0
Scale Error	%	5.4	5.1
Correlation Coefficient	N/A	0.95	0.98

The rating model was then created using this optimized model with the appropriate rating trucks instead of the field truck and by applying the structure self weight (i.e., dead load). Dead load applied to the structure includes the self-weight of all steel sections, the concrete deck, and the concrete curb. For rating purposes, the following truck positions (for the HS-20, H-20, and Type-3 trucks) were considered:

- Path A: The passenger side wheel line was 2 ft from East curb.
- Path B: Truck positioned 10 ft West of Path A.
- Path C: The driving side wheel line placed on the bridge centerline.
- Path D: The truck was positioned 10 ft West of Path B.
- Path E: The driving side wheel line was 2 ft East of the bridge centerline.
- Path F: The passenger side wheel line was 2 ft West of the bridge centerline.

Each path was analyzed at 1 ft intervals. This bridge was designed as a two-lane bridge, so truck path envelopes were created for two trucks being on the bridge at the same time (Note: AASHTO Standard Specifications (4) stipulates that the distance between two rating trucks should be 4 ft when they are both on the bridge):

- Envelope 1: Path A combined with Path B.
- Envelope 2: Path C combined with Path D.
- Envelope 3: Path E combined with Path F.

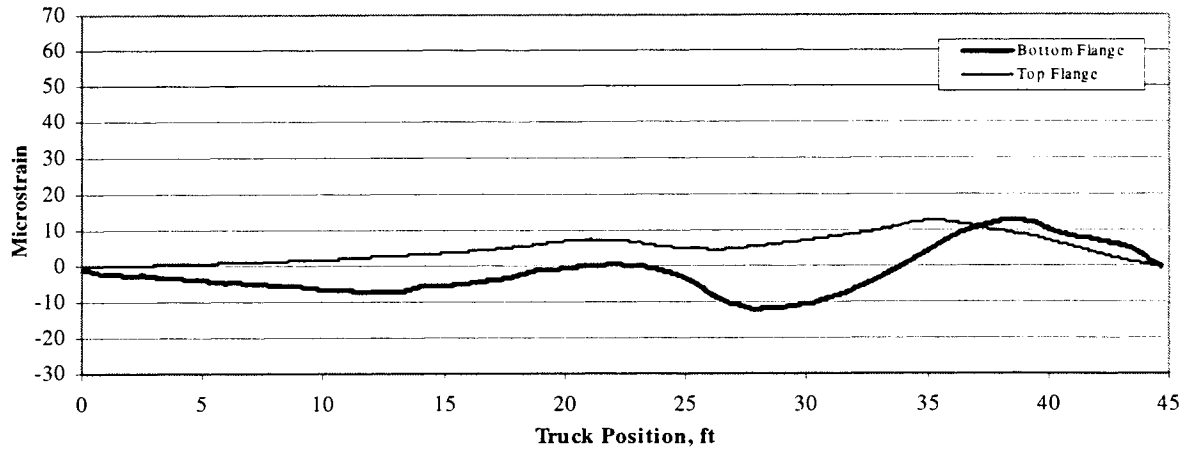
Individual member capacities were calculated following appropriate AASHTO Standard Specifications (4). Ratings by the LFD Method (by applying AASHTO Standard Specifications (4)) and by using the BDI Software are presented in Table 5.29 and Table 5.30, respectively. Table 5.31 summarizes the percent difference between inventory ratings obtained with the LFD Method and the inventory ratings obtained using the BDI Software. The critical rating condition is for flexure in the girder near the second pier (0.78 by the LFD Method and 1.38 by the BDI Software for a difference of 76.9 %). However, the critical rating condition for flexure in the floor beam by applying the BDI Software is 0.82 by the BDI Method and 0.83 by the LFD Method. The lane loadings investigated were determined not to be critical. Also, the HS-20 (30) rating truck used in the analytical rating model, was determined not to be critical (as previously mentioned, HS-20 (30) is the same truck as HS-20 but with a different distance between the rear axles).

Table 5.29. Bridge #4: Design Truck Rating Factors by the LFD Method.

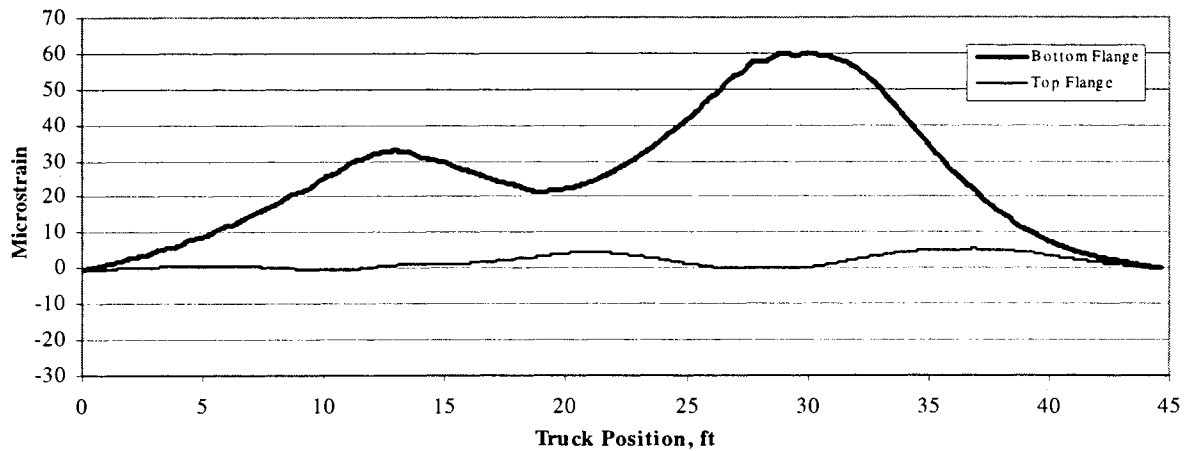
Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Girder at first span	1.05	1.75	1.41	2.35	1.37	2.28	2.08	3.48	1.33	2.22	1.91	3.19
Girder at second span	0.88	1.48	N/A	N/A	1.23	2.05	N/A	N/A	1.17	1.95	N/A	N/A
Girder near first pier	0.83	1.38	0.82	1.37	1.29	2.15	1.34	2.23	1.07	1.79	1.14	1.91
Girder near second pier	0.78	1.30	0.87	1.45	1.33	2.24	1.40	2.34	1.11	1.85	1.21	2.02
Floor beam	0.83	1.39	1.02	1.69	1.08	1.80	1.31	2.19	1.06	1.77	1.30	2.17

5.6. BRIDGE #5

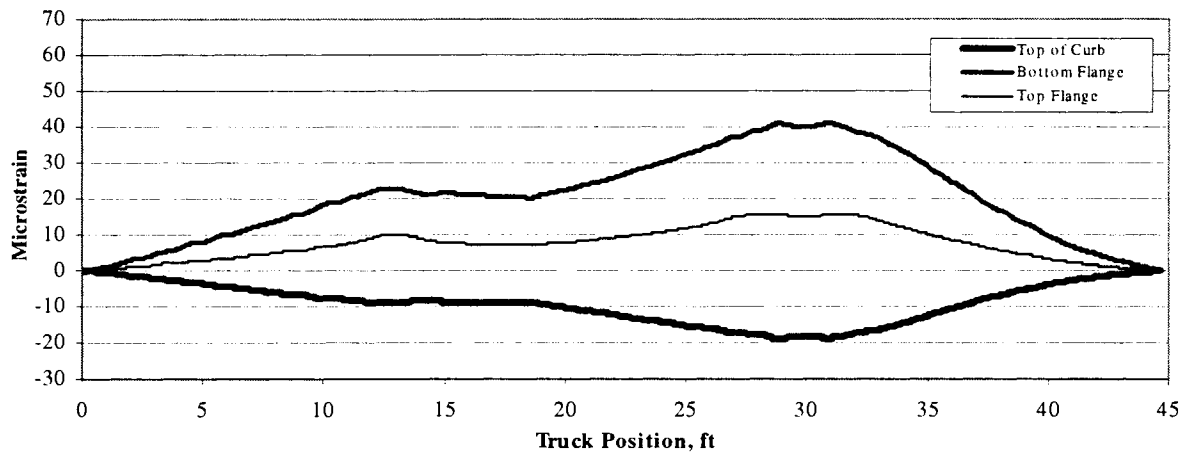
For typical experimental data shown in Fig. 5.23, Bridge #5 exhibits significant end restraint because the bottom flanges on the girder near the abutment (shown in Fig. 5.23a) are in compression.



a. Strains near the abutment for an interior girder at Location L12.



b. Strains at midspan for an interior girder at Location L11.



c. Strains at midspan for an exterior girder at Location L14.

Figure 5.23. Bridge #5: Typical experimental strains for Path Y1.

Table 5.30. Bridge #4: Design Truck Rating Factors by the BDI Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Girder at first span	1.40	2.34	1.41	2.35	1.90	3.17	2.17	3.62	1.87	3.12	1.92	3.20
Girder at second span	0.88	1.47	N/A	N/A	1.28	2.14	N/A	N/A	1.19	1.99	N/A	N/A
Girder near first pier	1.36	2.27	1.31	2.19	2.25	3.76	2.14	3.57	1.90	3.17	1.83	3.05
Girder near second pier	1.38	2.30	1.36	2.27	2.29	3.82	2.22	3.71	1.94	3.24	1.90	3.17
Floor beam	0.82	1.37	1.90	3.17	1.06	1.77	2.28	3.81	1.06	1.77	2.45	4.09

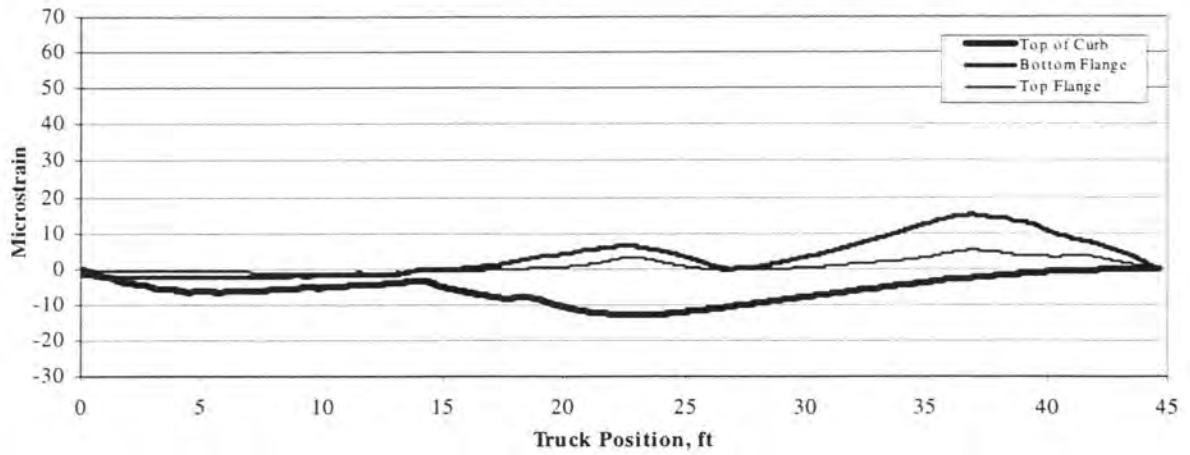
Table 5.31. Bridge #4: Percent difference in Design Truck Rating Factors between LFD Method and BDI Software.

Section	HS-20		H-20		Type-3	
	Flexure	Shear	Flexure	Shear	Flexure	Shear
Girder at first span	33.3	0.0	38.7	4.3	40.6	0.5
Girder at second span	0.0	N/A	4.1	N/A	1.7	N/A
Girder near first pier	63.9	59.8	74.4	59.7	77.6	60.5
Girder near second pier	76.9	56.3	72.2	58.6	74.8	57.0
Floor beam	-1.2	86.3	-1.9	74.0	0.0	88.5

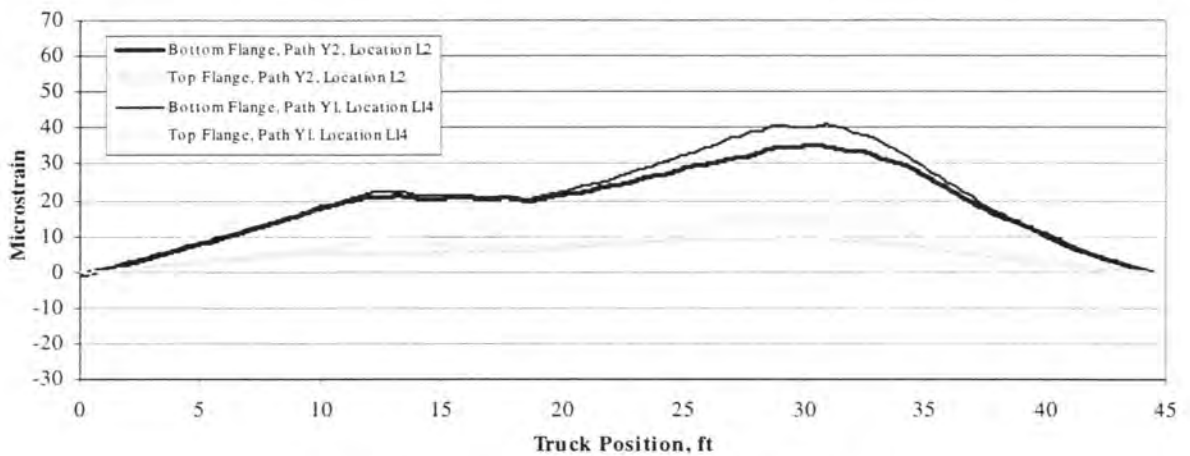
The neutral axis at this location varies from mid-depth of the steel-section to the top flange.

Experimental data at midspan for an interior girder presented in Fig. 5.23b indicate composite action since the neutral axis location is near the top flange. Further, as shown in Fig. 5.23c, experimental data at midspan for an exterior girder indicate that the neutral axis location lies well above the top flange since the top flange is in tension, hence composite action and edge stiffening due to the curb are verified. Moreover, experimental strains presented in Figs. 5.24b and 5.24c verify transverse and longitudinal strain symmetry (Note: Longitudinal strain symmetry is difficult to verify due to the unidirectional movement of the load truck).

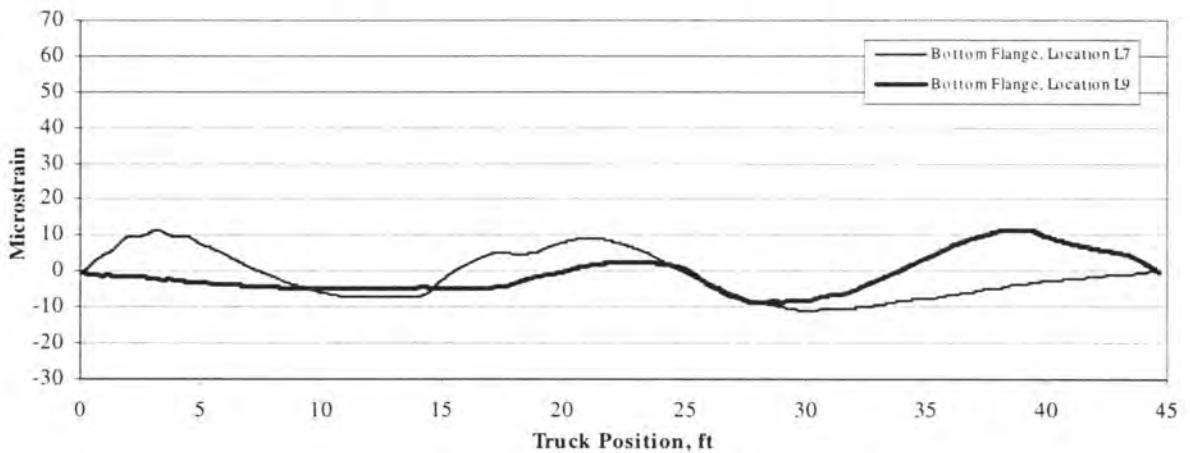
Based on the initial review of the data briefly discussed in the previous paragraph, an analytical model was created as shown in Fig. 5.25 with two elements between each girder and twelve elements in the longitudinal direction. Rotational springs were included for all girders at the centerline of the abutment bearings. As a result of the experimental data indicating composite



a. Strains near the abutment for an exterior girder at Location L15 for Path Y1.



b. Strain symmetry in the transverse direction



c. Strain symmetry in the longitudinal direction

Figure 5.24. Bridge #5: Typical experimental strains and symmetry plots.

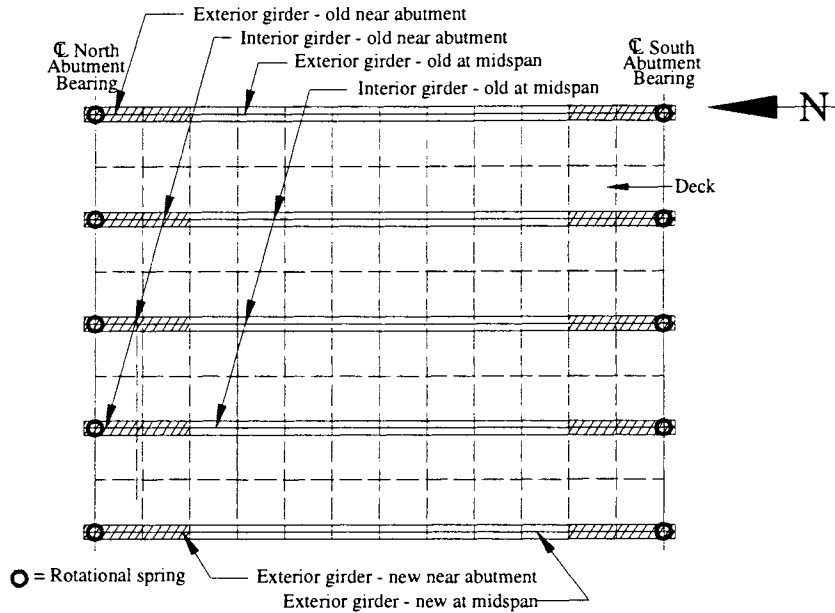


Figure 5.25. Bridge #5: Mesh of the analytical model with section property names and gage locations.

behavior at midspan, all girder sections at midspan were modeled as composite beams and all girder sections near the abutment were modeled as non-composite. In addition, the curb was included for the exterior beams at midspan to account for the edge stiffening (as indicated in the previous paragraph). The girders were modeled with beam elements, and the concrete deck was modeled with quadrilateral plate elements. Table 5.32 summarizes the optimized parameter results. These results indicate that all optimized parameters (excluding the springs) compare well with the initial parameters.

Table 5.32. Bridge #5: Adjustable parameters.

Section	Property	Units	Non-Composite	Composite	Initial	Optimized
New ext. girder near abut.	I_y	in^4	800	14,415	800	1,160
New ext. girder at midspan	I_y	in^4	800	14,415	14,415	11,720
Old ext. girder near abut.	I_y	in^4	736	13,835	736	1,160
Old ext. girder at midspan	I_y	in^4	736	13,835	13,835	11,500
Int. girder near abut.	I_y	in^4	736	3,005	736	1,255
Int. girder at midspan	I_y	in^4	736	3,005	3,005	3,595
Deck	E	ksi	N/A	N/A	3,600	4,990
Spring (rotational)	K_y	in-k/rad	N/A	N/A	0	944,000 ^a

^a Corresponds to approximately 60 % fixity.

The accuracy of the generated model is shown graphically in Fig. 5.26 and Fig 5.27 where Fig. 5.26 illustrates typical strains for the interior girders using Path Y1, and Fig. 5.26 presents typical strains for the exterior girders. Generally, all results compare well, and Table 5.33 illustrates the model accuracies for the initial and optimized models. Initially, assuming simply supported condition and initial section property values, an error of 164.5 % and a correlation coefficient of 0.79 were obtained. These values do not represent a good correlation between the measured and calculated strains, but the reason for the poor correlation is mainly due to the end restraint. The optimized model results in an error of 6.6 % and a correlation coefficient of 0.97, which verifies the good correlation between experimental and optimized analytical strains.

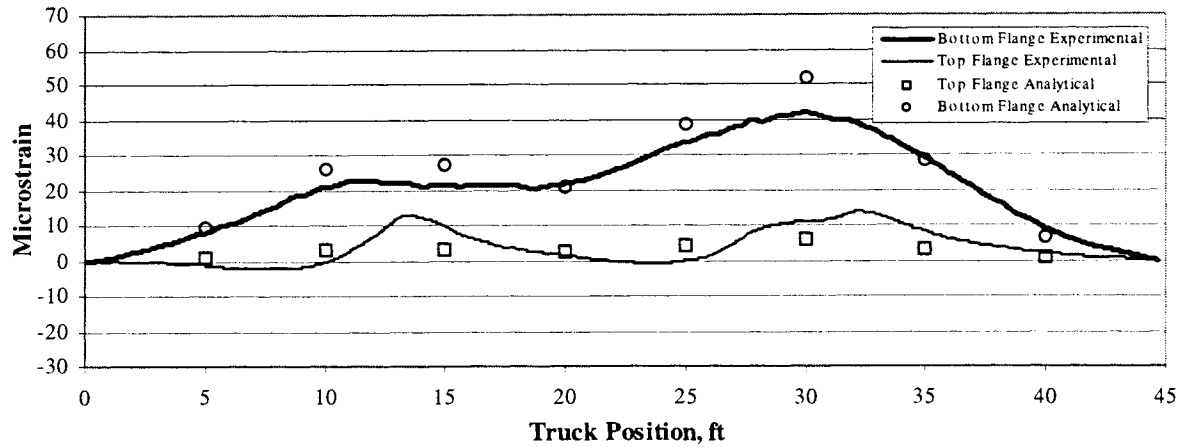
Table 5.33. Bridge #5: Model accuracy for initial and optimized model.

Statistical Term	Units	Initial	Optimized
Total error	microstrain	3,525	770
Percent Error	%	164.5	6.6
Scale Error	%	81.0	8.4
Correlation Coefficient	N/A	0.79	0.97

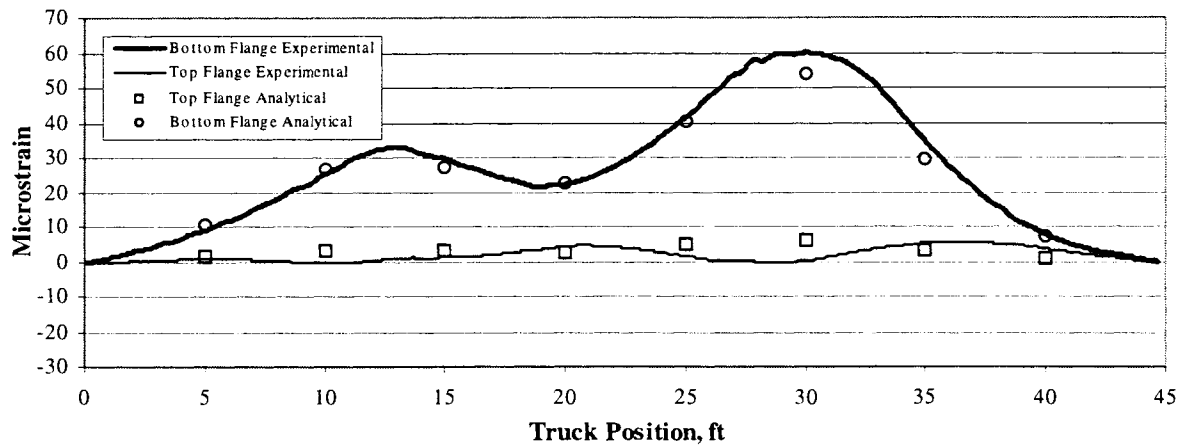
By using this optimized model with the appropriate rating trucks instead of the field truck and by applying dead load to the structure, the rating model was created. Dead load applied on the structure includes the self-weight of the girders, concrete deck including the overlay, and the concrete curb. For rating purposes, appropriate design trucks were considered:

- Paths A and B: The outer wheel line two ft from each curb.
- Path C: The driving side wheel line on the West interior girder.
- Path D: The driving side wheel line on the center girder.
- Path E: The truck placed on the bridge centerline.

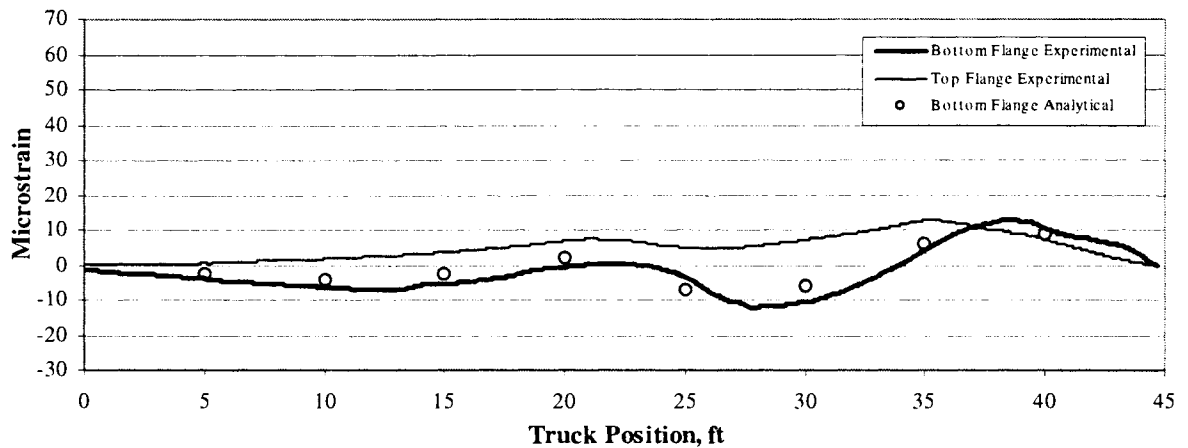
Each path was analyzed at 1 ft intervals. The bridge was designed as a single-lane bridge, so no truck path combinations were created. Individual member capacities were calculated following appropriate AASHTO Standard Specifications (4). Table 5.34 and Table 5.35 show the ratings by the LFD Method (by applying AASHTO Standard Specifications (4)) and by using the BDI Software, respectively. Table 5.36 summarizes the percent difference between inventory ratings by the LFD Method and by using the BDI Software. The critical rating condition is for flexure on the interior girder at midspan (0.87 by the LFD Method and 1.38 by the BDI Method for a difference of 92.0%).



a. Location L8.

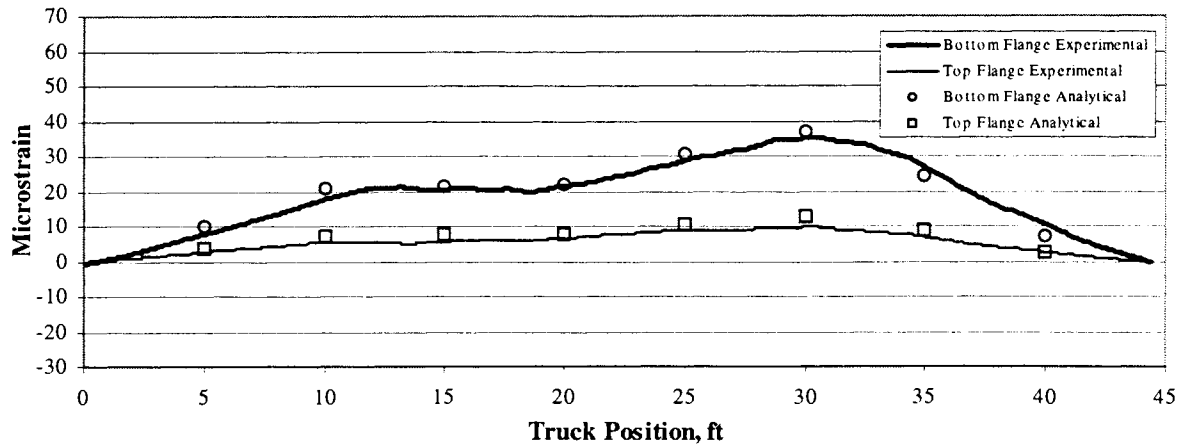


b. Location L11.

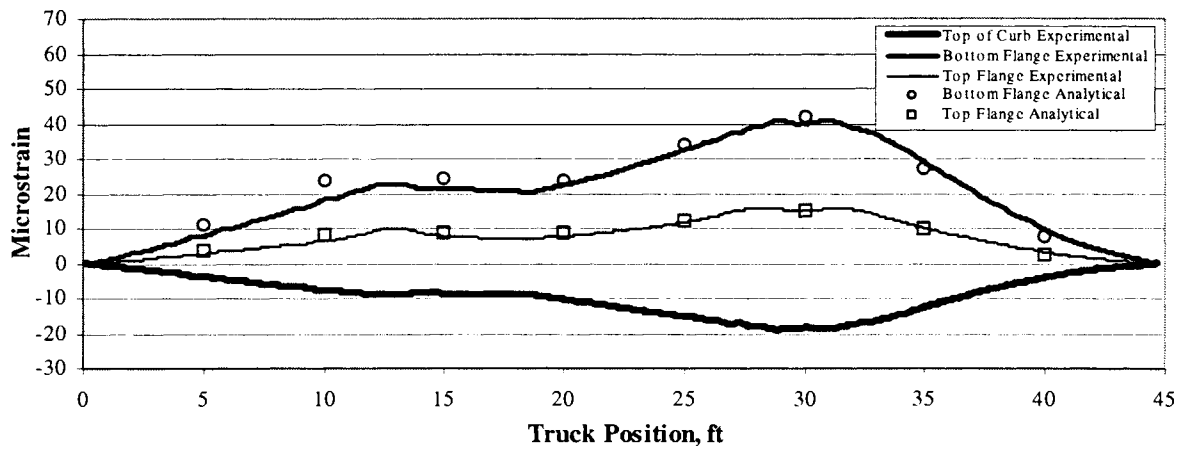


c. Location L12.

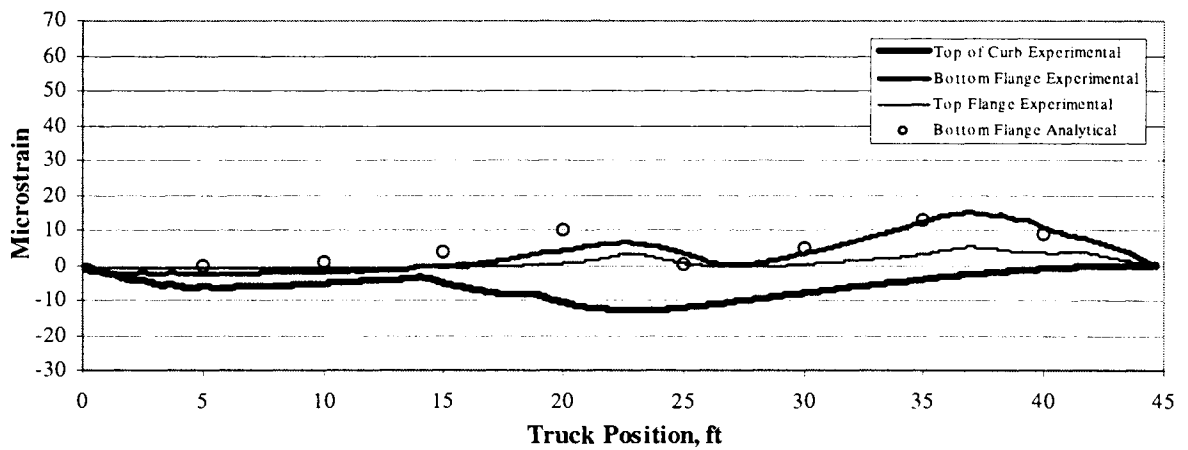
Figure 5.26. Bridge #5: Typical strain plots for interior girders for truck Path Y1.



a. Location L2 using truck Path Y2.



b. Location L14 using truck Path Y1.



c. Location L15 using truck Path Y1.

Figure 5.27. Bridge #5: Typical strain plots for the exterior girders.

Some of the BDI Software rating values were less than the LFD Method values; however, all values are above 1.0 where this occurs. It shall be pointed out that the lane loadings were investigated, but were found to be not critical (a negative percent difference indicates that the BDI rating are lower than the LFD rating).

Table 5.34. Bridge #5: Design Truck Rating Factors by the LFD Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
New exterior girder	1.35	2.25	2.90	4.85	1.35	2.25	3.77	6.29	1.50	2.50	3.81	6.36
Old exterior girder	1.51	2.53	3.51	5.86	1.51	2.53	4.59	7.60	1.68	2.81	4.61	7.69
Interior girder	0.87	1.45	2.06	3.43	0.87	1.45	2.67	4.46	0.97	1.61	2.70	4.51

Table 5.35. Bridge #5: Design Truck Rating Factors by the BDI Method^a.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
New exterior girder	1.23	2.05	3.03	5.06	1.24	2.07	3.88	6.48	1.40	2.34	4.27	7.13
Old exterior girder	1.30	2.17	3.56	5.94	1.30	2.17	4.63	7.73	1.45	2.42	4.85	8.10
Interior girder	1.67	2.79	2.97	4.96	1.68	2.80	3.59	5.99	2.03	3.39	4.04	6.74

^a Unintended composite action included.

Table 5.36. Bridge #5: Percent difference in Design Truck Rating Factors between LFD Method and BDI Software.

Section	HS-20		H-20		Type-3	
	Flexure	Shear	Flexure	Shear	Flexure	Shear
New exterior girder	-8.9	4.5	-8.1	2.9	-6.7	12.1
Old exterior girder	-13.9	1.4	-13.9	0.9	-13.7	5.2
Interior girder	92.0	44.2	93.1	34.4	109.3	49.6

5.7. BRIDGE #6

As mentioned previously, it was anticipated that the bridge would exhibit significant end restraint since there are no abutment deck expansion joints. Typical experimental data are presented in Fig 5.28, where Fig. 5.28a illustrates typical strains for Path Y2, Fig. 5.28b shows typical strains for Path Y3, and Fig. 5.28c illustrates typical strains for Path Y4. These data show that the gages on the bottom of the slab near the abutments are in tension when the truck is near; hence end restraint is not verified (note that no gages were placed on top of the slab, which makes it difficult to identify negative moments near the abutments). Experimental data illustrating symmetry is shown in Fig. 5.29, where Fig. 5.29a and Fig. 5.29b illustrates that the strains are non-symmetric in the transverse direction since the strain peaks are not of the same magnitudes, and Fig. 5.29c verifies that the strain is symmetric in the longitudinal direction since the strain magnitudes are approximately the same.

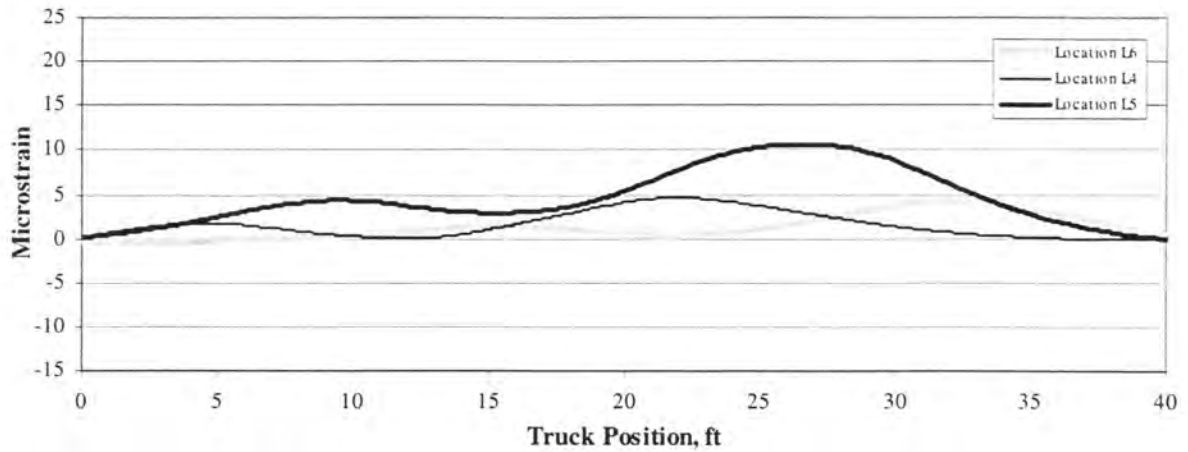
Based on the initial review of the data briefly discussed in the previous paragraph, two different sections were created on the curb (i.e., one section on the West edge and one section on the East edge) to account for the non-symmetric edge stiffness. As shown in Fig. 5.30, ten elements were created in the longitudinal direction and twenty elements were created in the transverse direction to obtain square plate elements. Rotational springs were included at the centerline of the abutment bearings on every second mesh-line to account for the end restraint. The deck was modeled with quadrilateral plate elements. Table 5.37 summarizes the optimized parameter results.

Table 5.37. Bridge #6: Adjustable parameters.

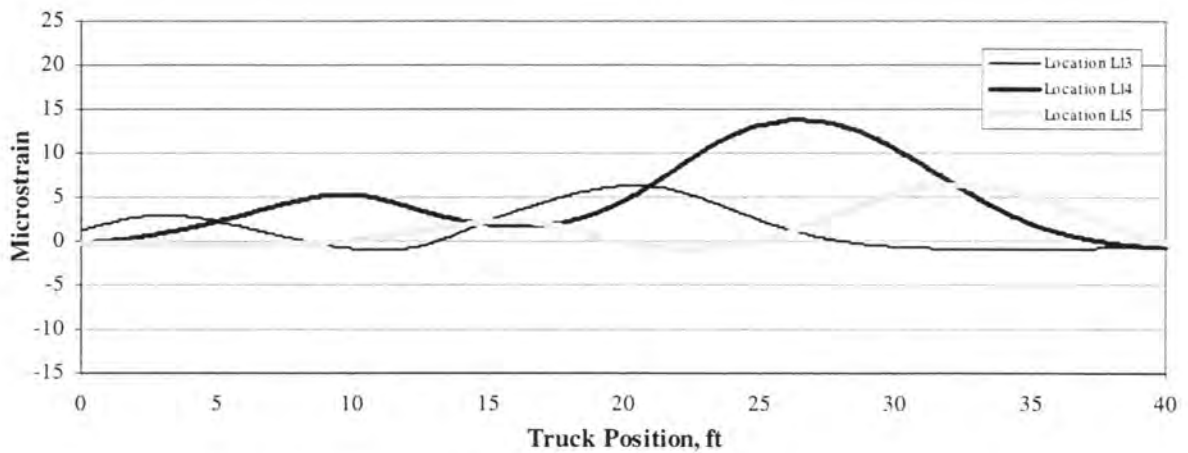
Section	Property	Units	Non-Composite	Composite	Initial	Optimized
Curb West	I_y	in^4	N/A	29,850	29,850	71,140
Curb East	I_y	in^4	N/A	29,850	29,850	5,195
Deck	E	ksi	N/A	N/A	3,600	5,985
Spring (rotational)	K_y	in-k/rad	N/A	N/A	0	534,210 ^a

^a Corresponds to approximately 7 % fixity.

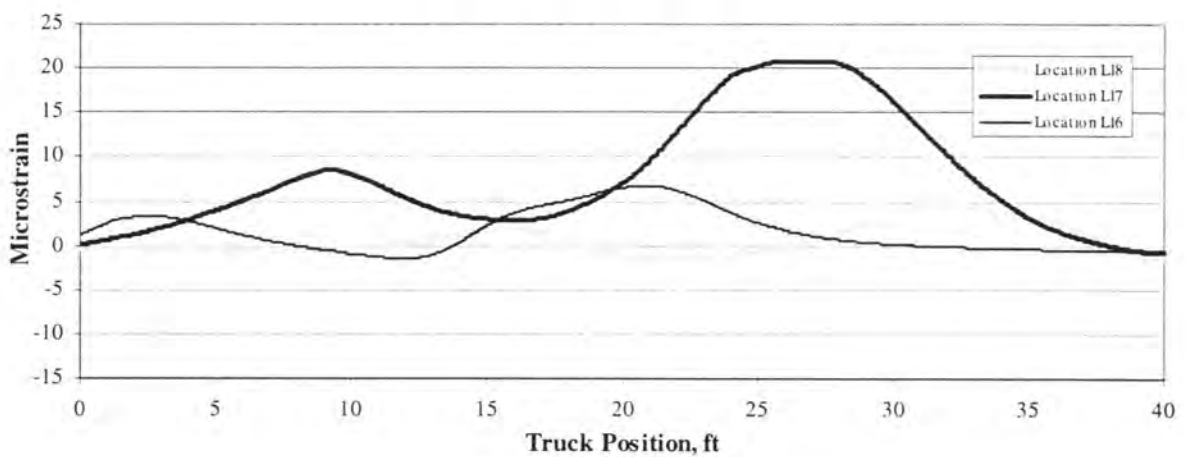
The accuracy of the generated model is shown graphically in Fig. 5.31 through Fig. 5.33 for typical data at various locations and various truck paths. All figures illustrate that the optimized analytical strains correlate relatively well with the experimental strains; however, the optimized parameters for West and East curb do not correlate very well with the initial parameters. The reason why they do not correlate that well is because it was not possible to locate the neutral axis on the East



a. Strains for Path Y2.

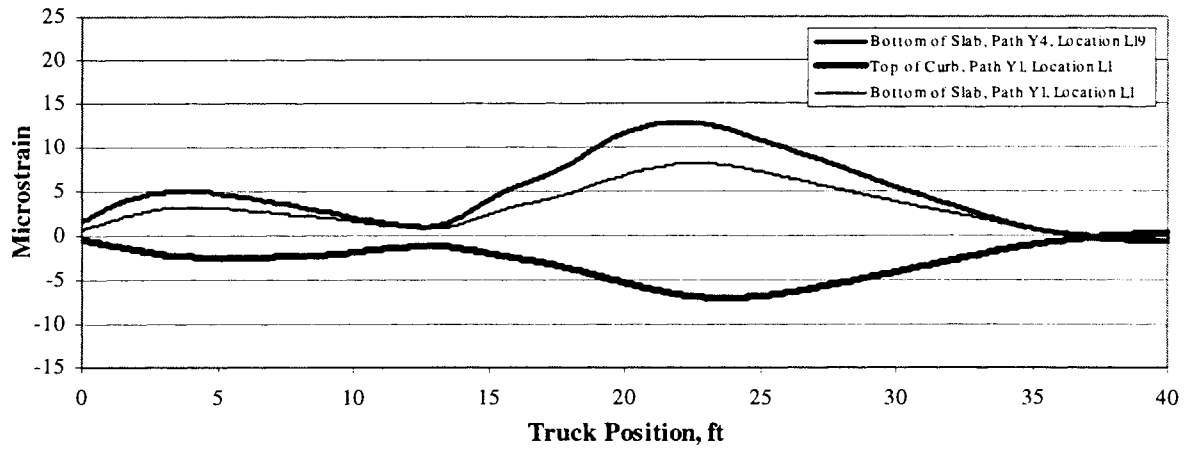


b. Strains for Path Y3.

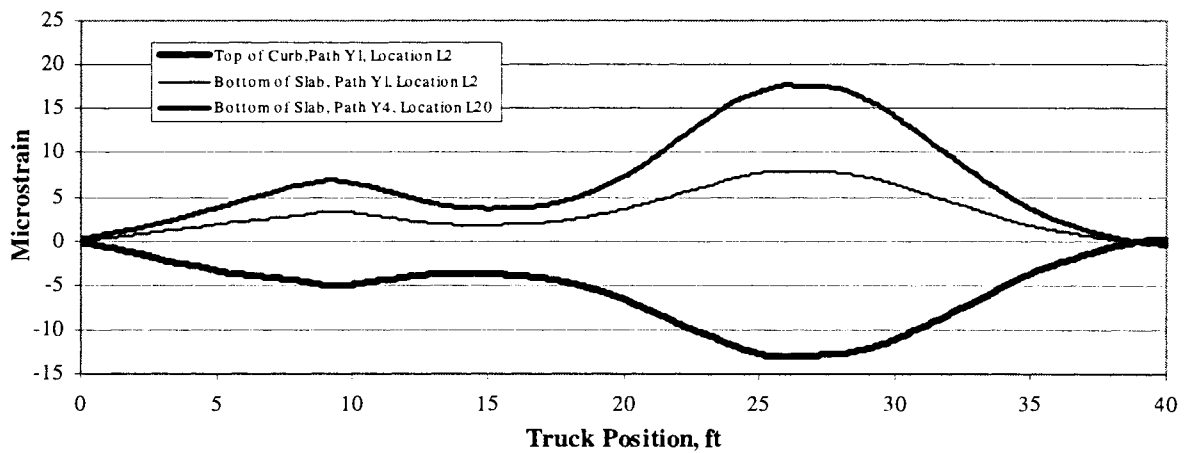


c. Strains for Path Y4.

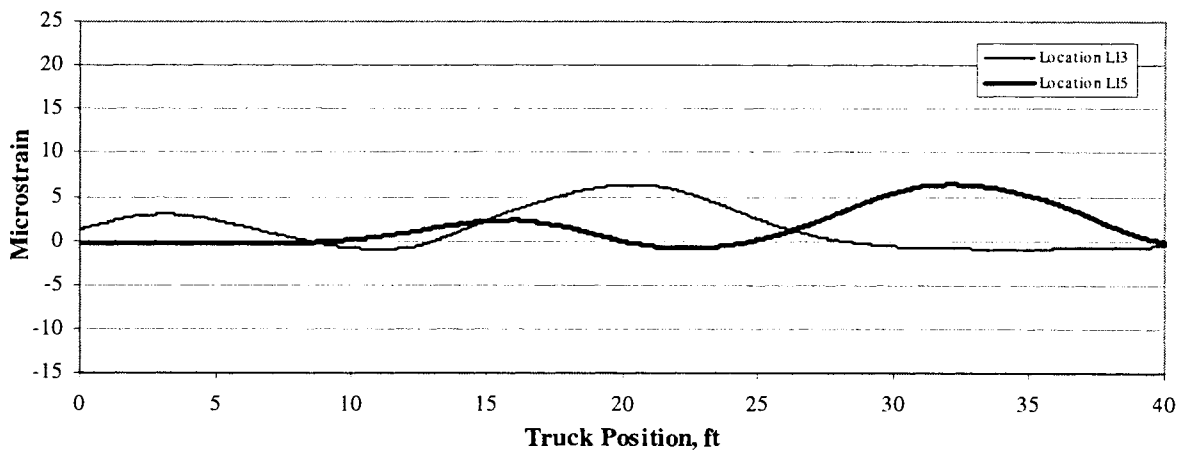
Figure 5.28. Bridge #6: Typical experimental strains.



a. Non-symmetric strains near the abutments in the transverse direction .



b. Non-symmetric strains at midspan in the transverse direction.



c. Longitudinal symmetry for Path Y3 (strains on the bottom of the slab).

Figure 5.29. Bridge #6: Experimental strains and strain symmetry.

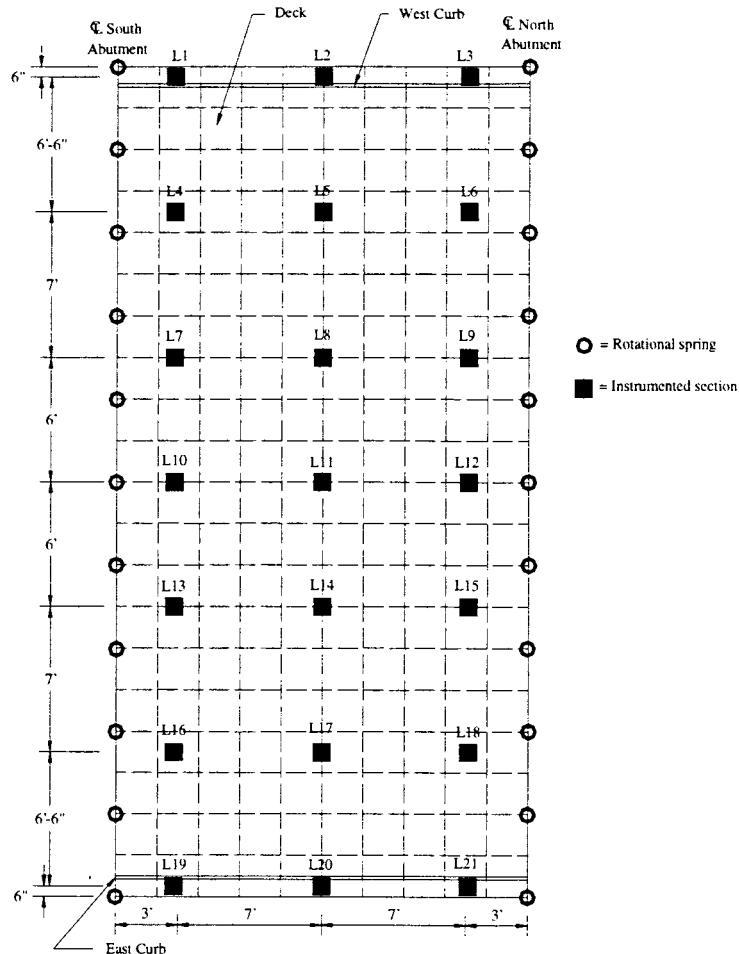
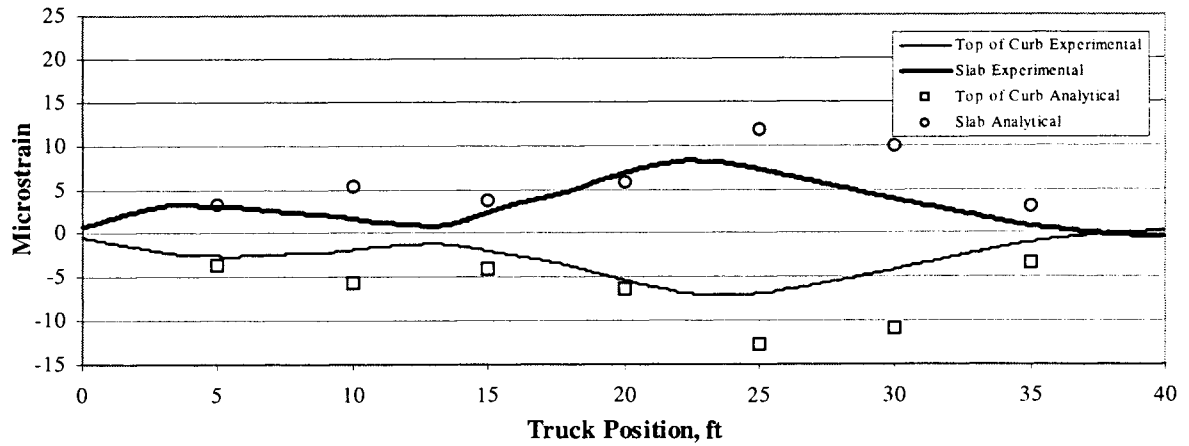
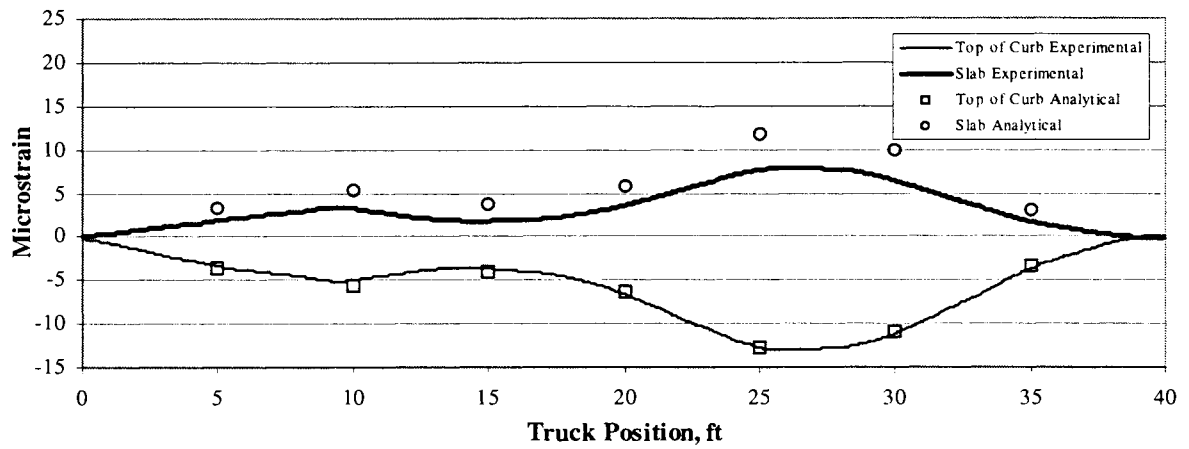


Figure 5.30. Bridge #6: Mesh of the analytical model with section property names.

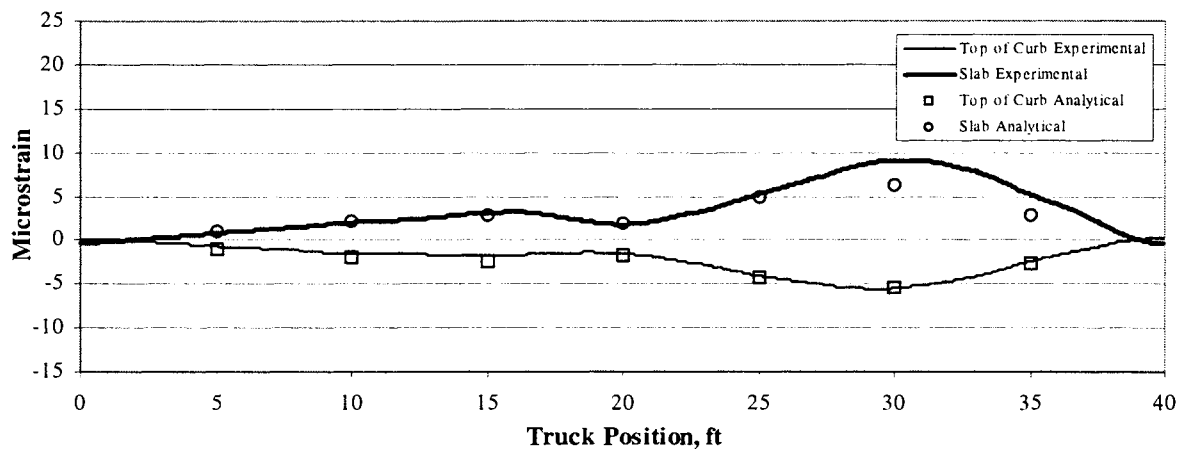
Curb without any strain data on top of the curb (strain gages on top of the curb were only installed on the West edge). Even though two different sections were created, and two different inertia values were obtained, the optimized value for the East Curb is of little use since the location of the neutral axis could not be established. However, it was necessary to include the two sections in the optimization process to obtain a reasonable analytical bridge model. Table 5.38 illustrates the model accuracy and shows that the initial error of 131.4 % and a correlation coefficient of 0.88 indicate a poor correlation between the experimental and analytical strains mostly due to non-symmetric behavior. However, the optimized model shows a final error of 9.9 % and a correlation coefficient of 0.95. These results indicate a relatively good correlation between the experimental and the optimized analytical strains (note that strains on a concrete slab are more difficult to predict than strains on a steel member).



a. Location L1.

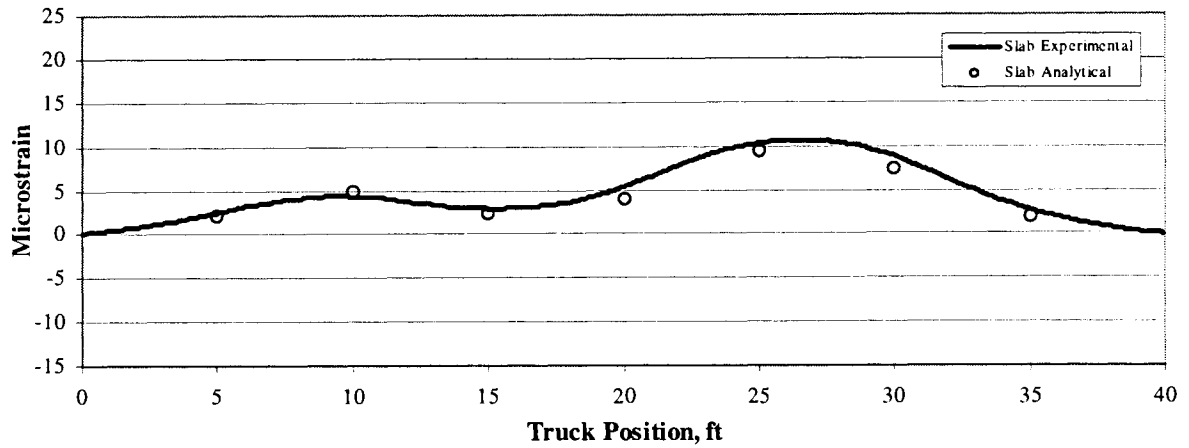


b. Location L2.

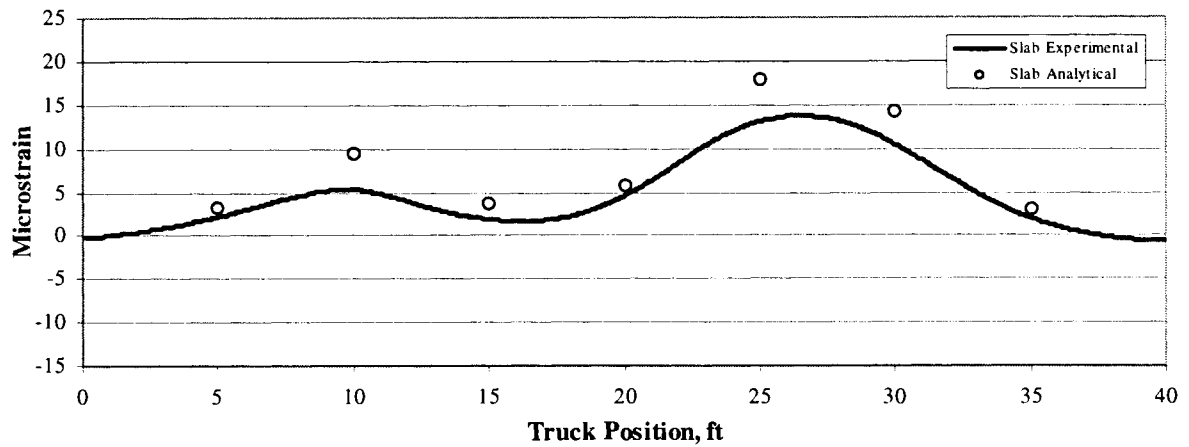


c. Location L3.

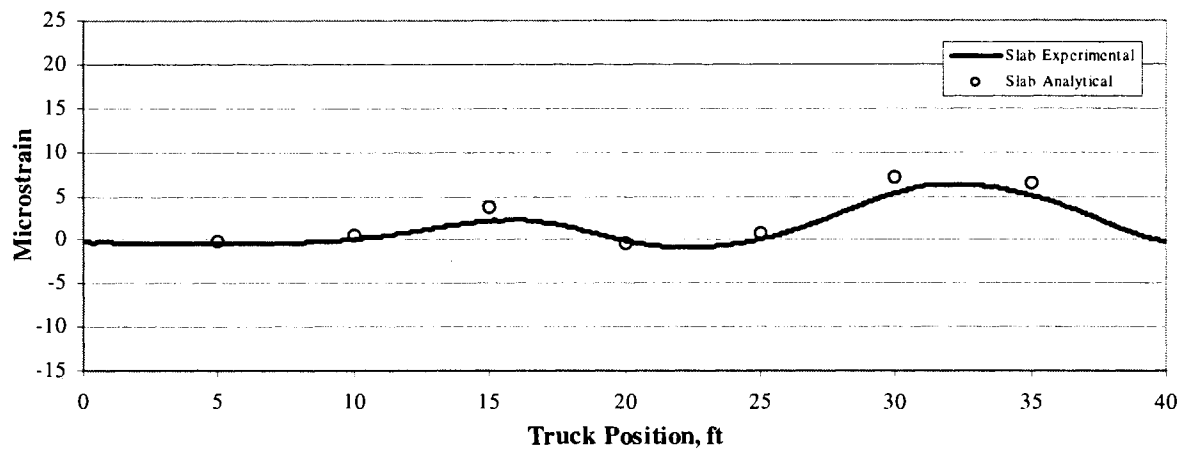
Figure 5.31. Bridge #6: Strain plots at the West Curb for truck Path Y1.



a. Location L5 for truck Path Y2.

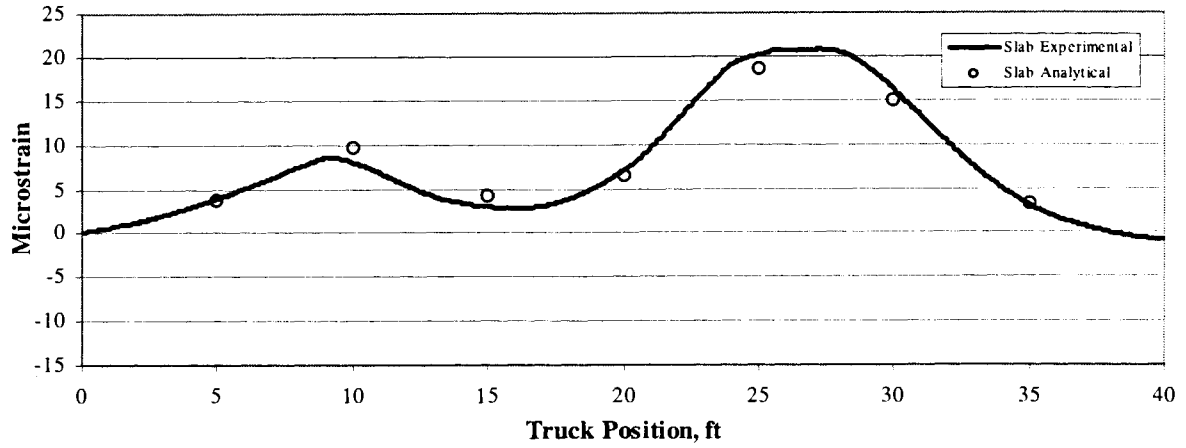


b. Location L14 for truck Path Y3.

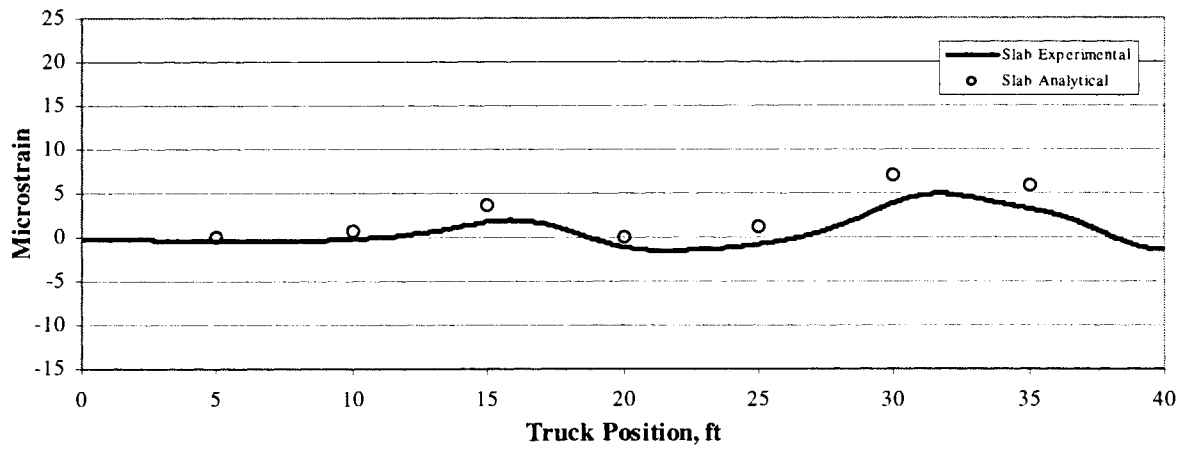


c. Location L15 for truck Path Y3.

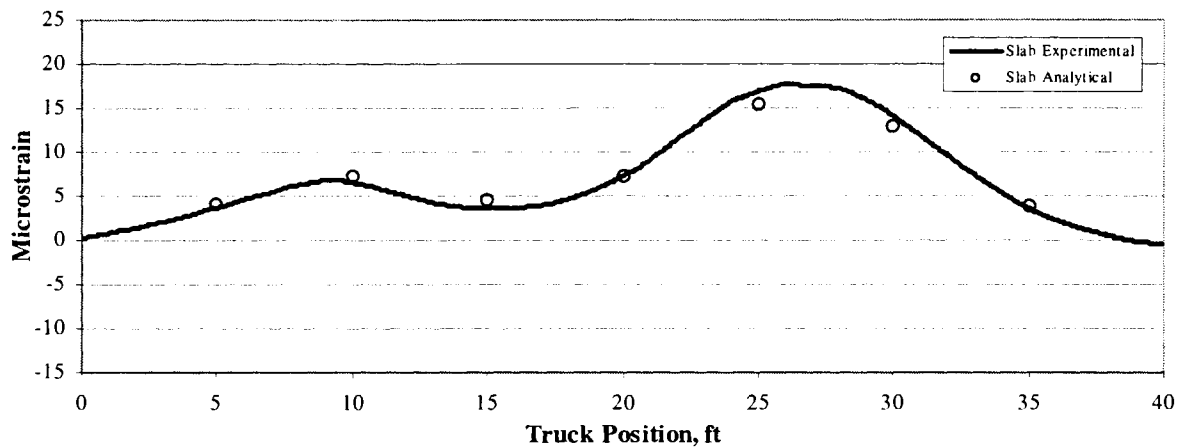
Figure 5.32. Bridge #6: Typical strains on the bottom of the slab for truck Paths Y2 and Y3.



a. Location L17.



b. Location L18.



c. Location L20.

Figure 5.33. Bridge #6: Typical strain plots at the bottom of slab for truck Path Y4.

Table 5.38. Bridge #6: Model accuracy for initial and optimized model.

Statistical Term	Units	Initial	Optimized
Total error	microstrain	1,649	450
Percent Error	%	131.4	9.9
Scale Error	%	31.6	4.9
Correlation Coefficient	N/A	0.88	0.95

By using this optimized model with the appropriate rating trucks instead of the field truck and by applying dead load to the structure, the rating model was created. Dead load applied in the analytical model includes the self-weight of the concrete slab deck and the concrete curb, and an additional 2.38 ft fill and asphalt overlay on top of the deck. For rating purposes, appropriate design trucks were considered:

- Path A: The driver side wheel line 7 ft from the East curb.
- Path B: The driver side wheel line 12 ft from the East curb.
- Path C: The driver side wheel line 17 ft from the East curb.
- Path D: The driver side wheel line 22 ft from the East curb.
- Path E: The driver side wheel line 27 ft from the East curb.
- Path F: The driver side wheel line 32 ft from the East curb.
- Path G: The driver side wheel line 1 ft from the West curb.
- Path H: The driver side wheel line 11 ft from the West curb.

Each path was analyzed at 1 ft intervals. This bridge was designed as a two-lane bridge, so truck path envelopes were created to account for two trucks being on the bridge at the same time:

- Envelope 1: Path A combined with Path C.
- Envelope 2: Path B combined with Path D.
- Envelope 3: Path C combined with Path E.
- Envelope 4: Path D combined with Path F.
- Envelope 5: Path G combined with Path H.

Individual member capacities were calculated following appropriate AASHTO Standard Specifications (4). Table 5.39 and Table 5.40 show the ratings by the LFD Method (by applying AASHTO Standard Specifications (4)) and by using the BDI Software, respectively. Table 5.41 summarizes the percent difference between inventory ratings by the LFD Method and by using the BDI Software (note: a positive percent difference indicates that the BDI rating value is greater than

the LFD rating value). The critical rating condition is 0.67 by The LFD Method and 1.55 by the BDI Software for a difference of 131.3 %. It shall be pointed out that lane loadings were investigated and were found to be not critical.

Table 5.39. Bridge #6: Design Truck Rating Factors by The LFD Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Deck	0.67	1.12	1.86	3.10	0.67	1.12	2.25	3.76	0.77	1.29	2.46	4.11

Table 5.40. Bridge #6: Design Truck Rating Factors by the BDI Method^a.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Deck	1.55	2.59	1.79	2.99	1.55	2.59	1.98	3.31	2.10	3.51	2.37	3.96

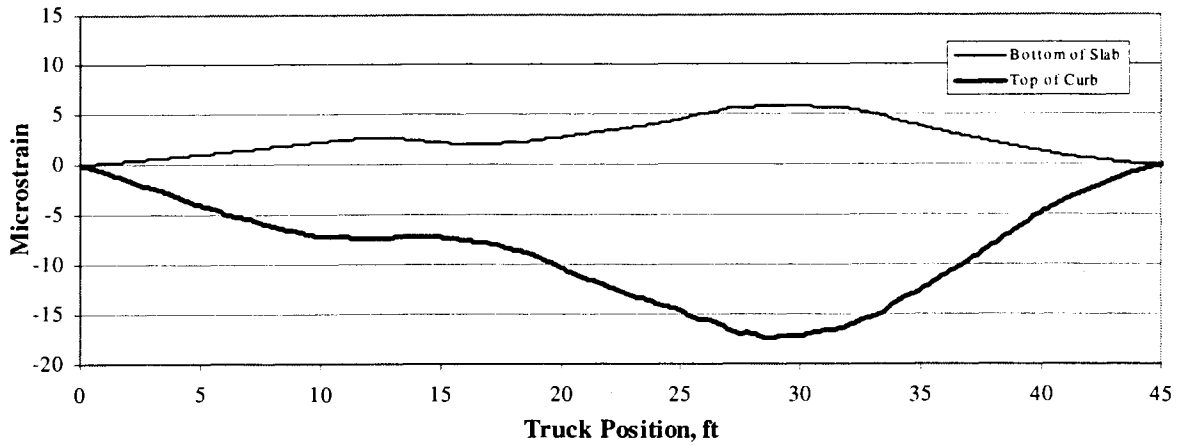
^a Edge stiffening included.

Table 5.41. Bridge #6: Percent difference in Design Truck Rating Factors between LFD Method and BDI Software.

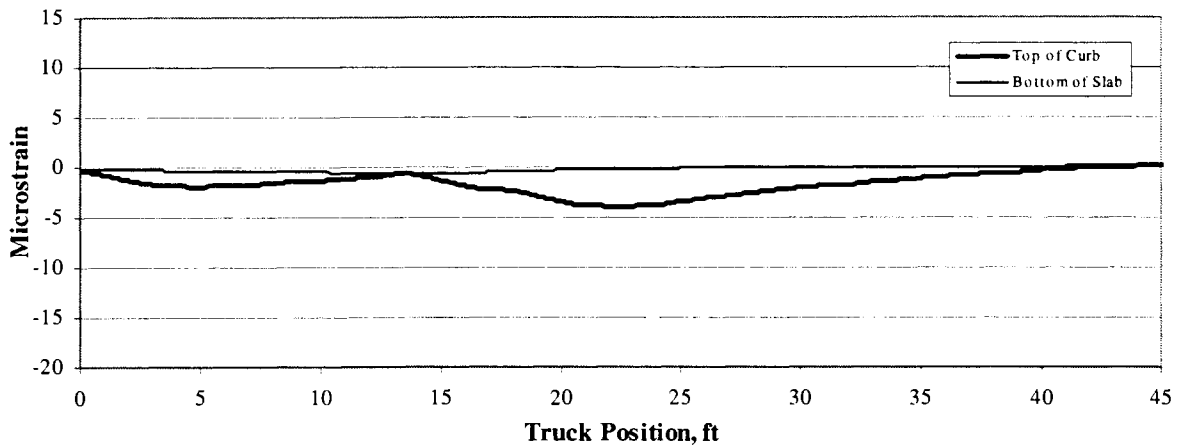
Section	HS-20		H-20		Type-3	
	Flexure	Shear	Flexure	Shear	Flexure	Shear
Deck	131.3	-3.8	131.3	-12.0	172.7	-3.7

5.8. BRIDGE #7

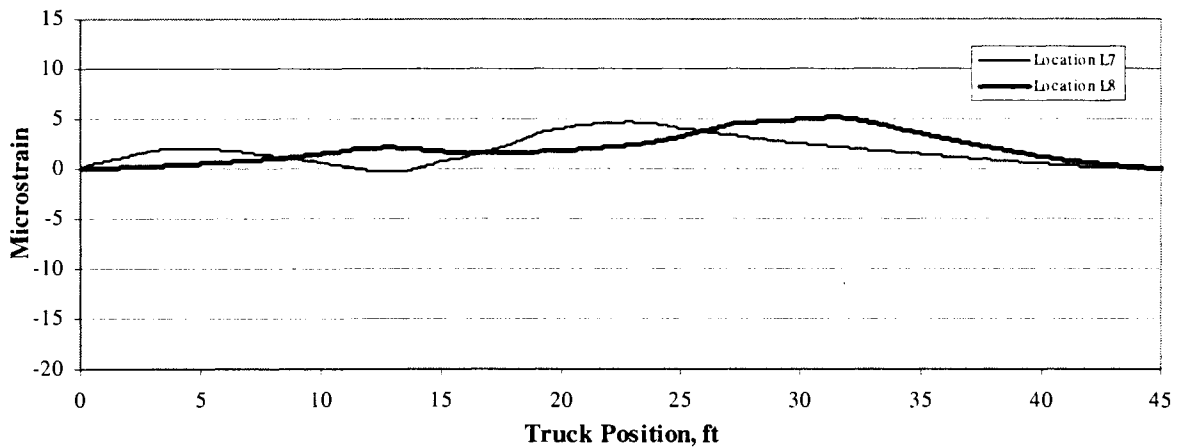
Typical experimental data are presented in Figs. 5.34 through 5.36, where Fig. 5.34a indicate that edge stiffening due to the curb occurs since the neutral axis location is above mid depth of the slab. As described previously, gages were installed near the construction joint for Path Y2 to observe the potential live load transfer across the joint. Experimental data at midspan near the construction joint is presented in Fig. 5.35, where Fig 5.35a illustrates the strains 5 ft West of the joint, the strains 1 ft West of the joint are shown in Fig. 5.35b, and the strains 1ft East of the joint are shown in Fig. 5.35c. These results indicate that the loads are not transferred linearly across the joint since, because, if the loads were transferred linearly, the strains in Fig. 5.35c should have been larger relative to the



a. Strains at midspan at Location L2.

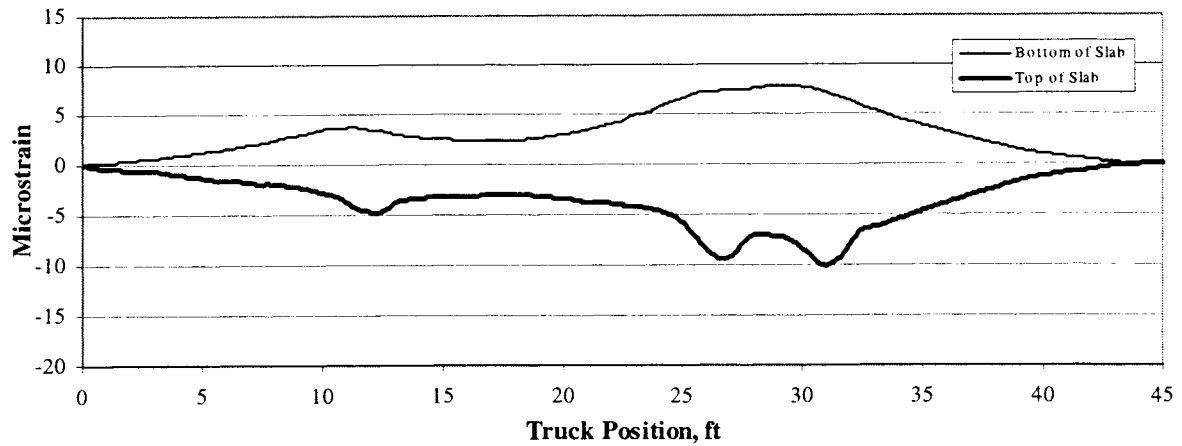


b. Strains near the abutment at Location L1.

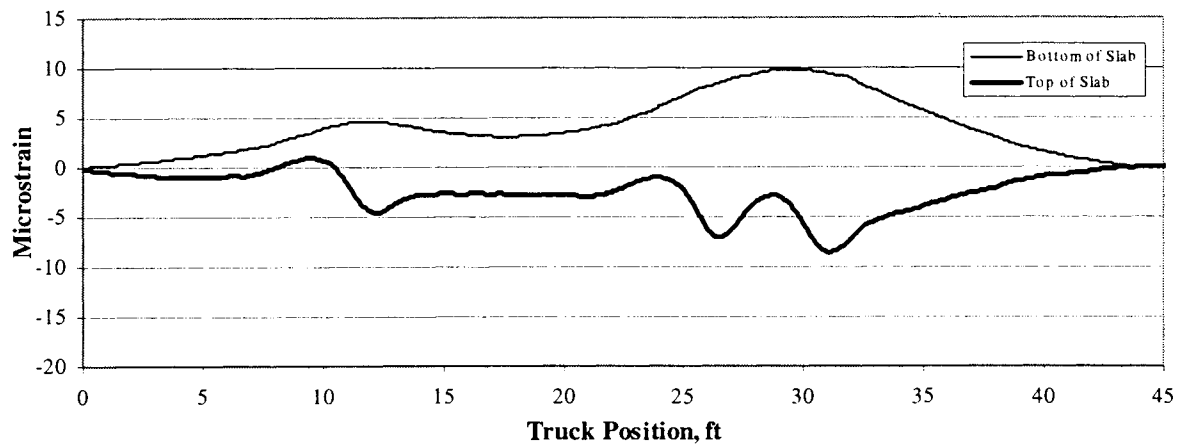


c. Strains on the bottom of the slab at locations L7 and L8.

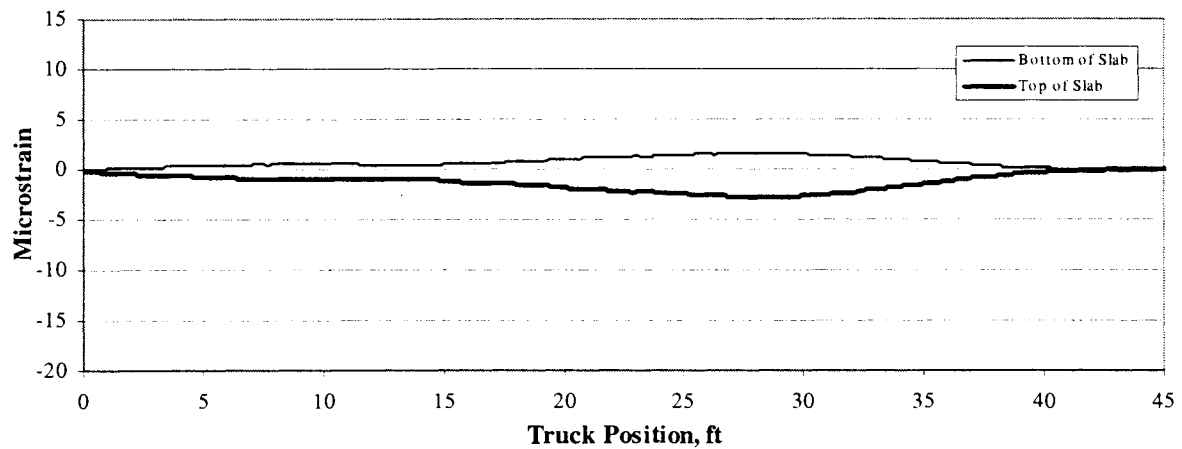
Figure 5.34. Bridge #7: Typical experimental strains for Path Y4.



a. Strains 5 ft West of construction joint at Location L14.

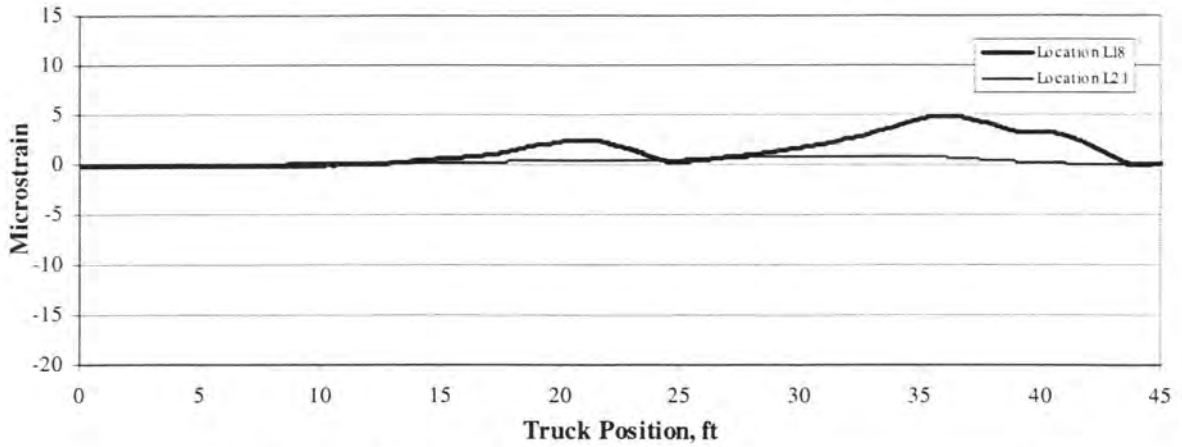


b. Strains 1 ft West of construction joint at Location L17.

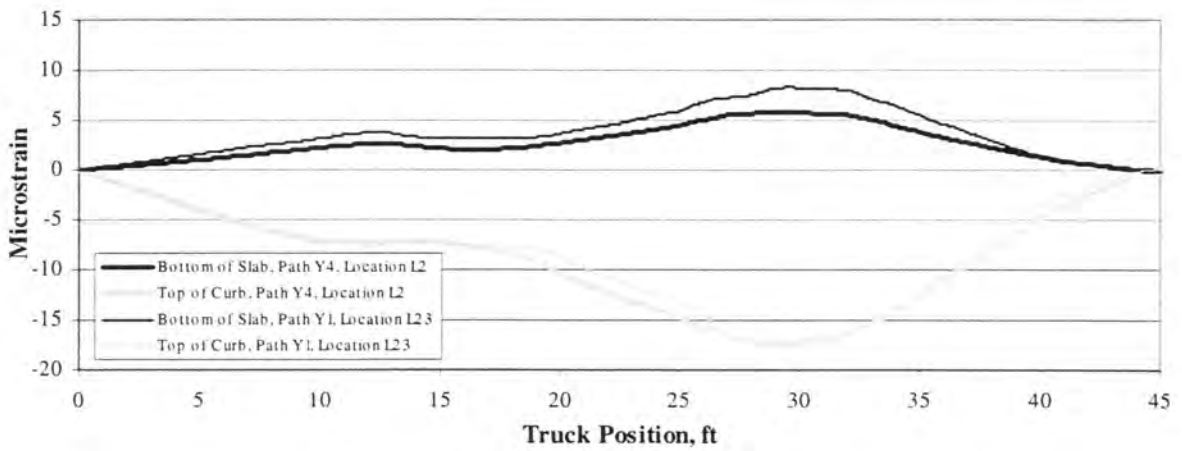


c. Strains 1 ft East of construction joint at Location L20.

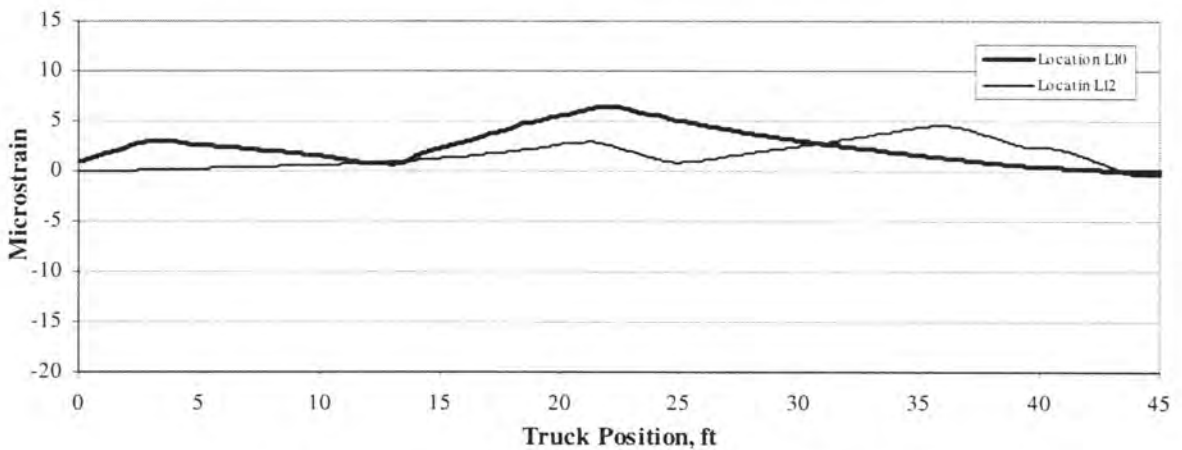
Figure 5.35. Bridge #7: Experimental strains at midspan near the construction joint for Path Y2.



a. Strains on the bottom of the slab across the construction joint for Path Y2.



b. Transverse strain symmetry.



c. Strain comparison to identify longitudinal strain symmetry.

Figure 5.36. Bridge #7: Experimental strains and strain symmetry.

strains shown in Fig. 5.35b. Figure 5.36a illustrates the strain transfer across the joint on the bottom of the slab near the abutment for Path Y2, and verifies that the strains are not linearly transferred across the joint. Further, as can be seen in Fig. 5.36b, the strains are relatively symmetric in the transverse direction since the strain magnitudes are approximately the same, and Fig. 5.36c shows that the strains are also relatively symmetric in the longitudinal direction since the strain peaks are approximately of the same magnitudes.

Based on the initial review of the data briefly discussed in the previous paragraph, the curb was included in the analytical model to account for the edge stiffening. It was not possible to take into account the fact that strains did not transfer linearly across the construction joint due to the limitations of the BDI Software, so, in the analytical model, strains will transfer linearly across the joint. As shown in Fig. 5.37, twelve elements were created in the longitudinal direction and fifteen elements were created in the transverse direction. Rotational springs were included at the centerline of the abutment bearings on every second analytical mesh-line to account for the end restraint (note: the BDI Software has a limited number of springs that can be included in the model, and, for this bridge model, the software would not run if springs were included on all mesh-lines). The deck was modeled with quadrilateral plate elements. Table 5.42 summarizes the optimized parameter results.

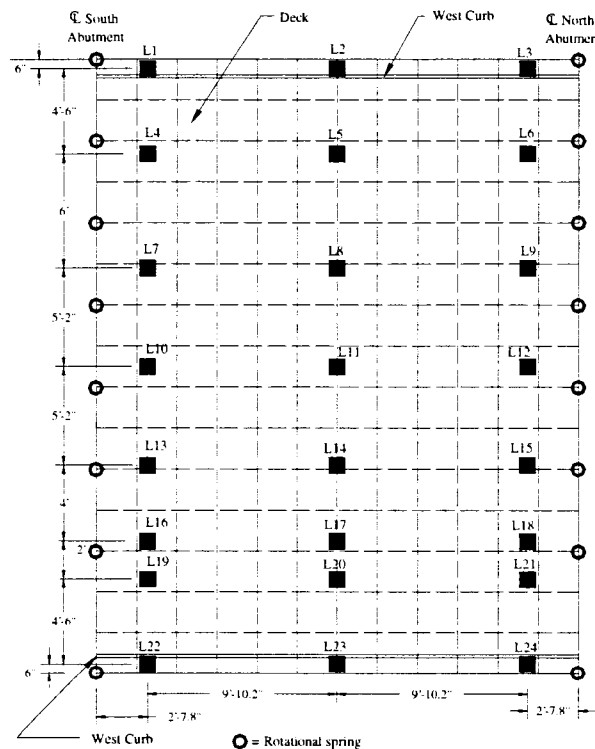


Figure 5.37. Bridge #7: Mesh of the analytical model with section property names.

Table 5.42. Bridge #7: Adjustable parameters.

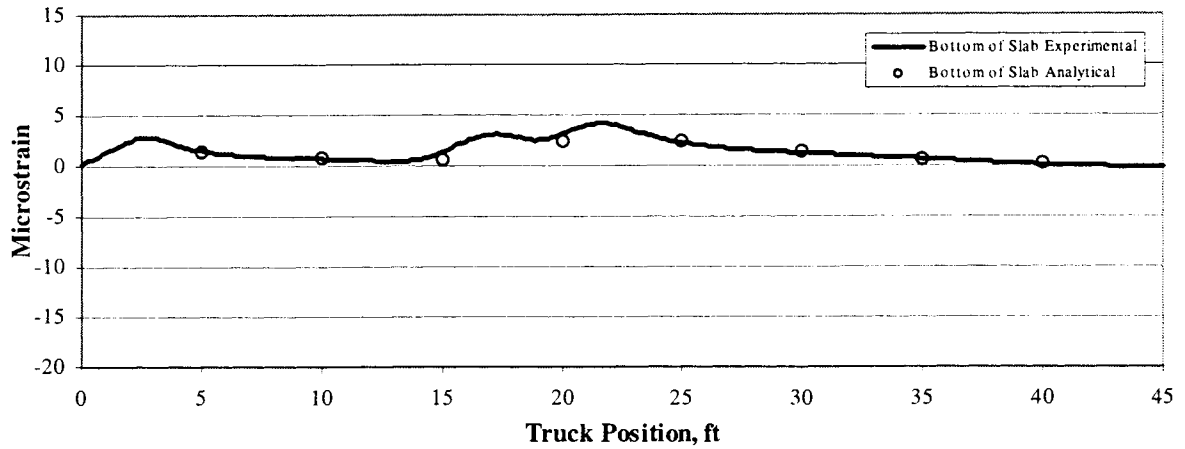
Section	Property	Units	Non-Composite	Composite	Initial	Optimized
Curb	I_y	in^4	N/A	183,460	183,460	348,700
Deck	E	ksi	N/A	N/A	3,600	3,960
Spring (rotational)	K_y	in-k/rad	N/A	N/A	0	39,670 ^a

^a Correlates to approximate 2 % fixity.

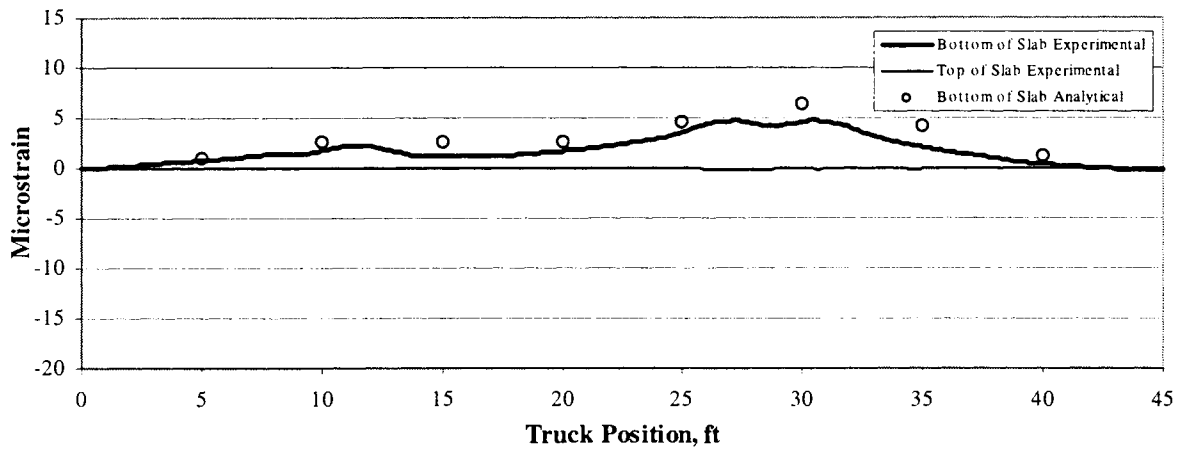
The accuracy of the generated model is shown graphically in Fig. 5.38 through Fig. 5.42 for various truck paths and at various locations. Strain plots on the East side of the construction joint for Path Y3 are illustrated in Fig. 5.38 and indicate that the experimental and analytical strains compare well. Strain plots on the West side of the construction joint for Path Y3 are presented in Fig. 5.39 and also indicates that the strains compare well; however, when comparing strains at midspan 1 ft from each side of the construction joint, the data show that the analytical strains are slightly larger than the experimental strains on the East side of the joint (Location L20, shown in Fig. 5.38b) and the analytical strains are slightly smaller than the experimental strains on the West side of the joint (Location L17, shown in Fig. 5.39b). These results verify that the analytical strains are transferred linearly across the construction joint. Further, data are presented in Fig. 5.40 and Fig. 5.41 illustrating strains at various locations on the East curb and on the West curb, respectively. Finally, Fig. 5.42 illustrates typical strains for Path Y2, where Fig. 5.42c shows both analytical and experimental strains across the construction joint and verifies that analytical strains are linearly transferred and that the experimental strains are not transferred linearly across the joint. Table 5.43 illustrates the model accuracy and shows an initial error of 22.3 %. The final optimized error is 12.5%; however, the reason of the relatively large error may be that the analytical model could not simulate the non-linear shear transfer across the construction joint.

Table 5.43. Bridge #7: Model accuracy for initial and optimized model.

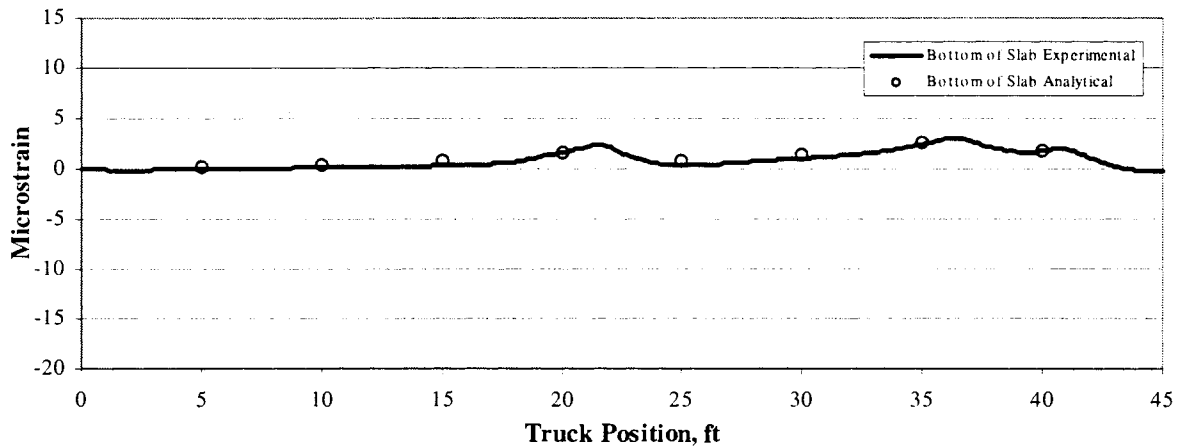
Statistical Term	Units	Initial	Optimized
Total error	microstrain	839	625
Percent Error	%	22.3	12.5
Scale Error	%	18.3	12.1
Correlation Coefficient	N/A	0.92	0.94



a. Location L19.

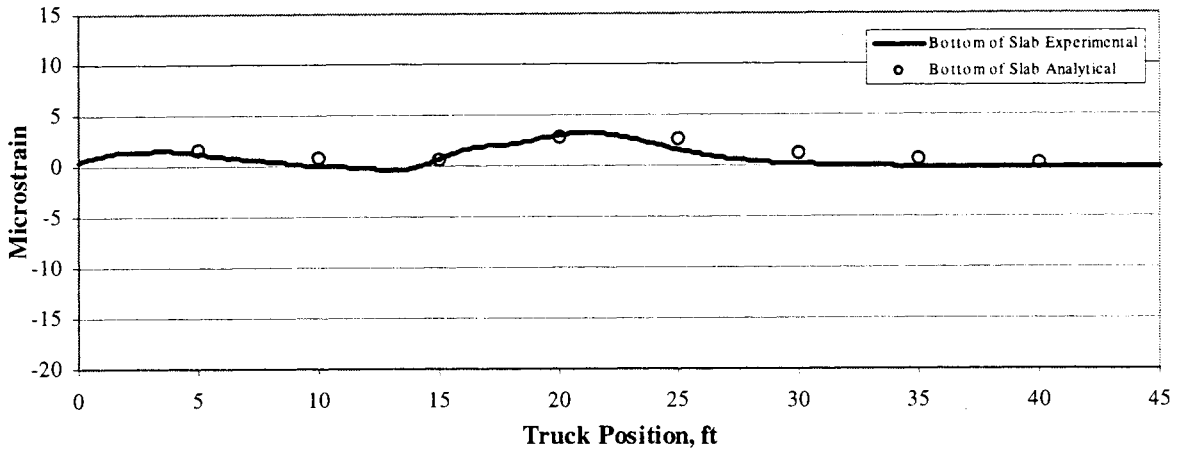


b. Location L20.

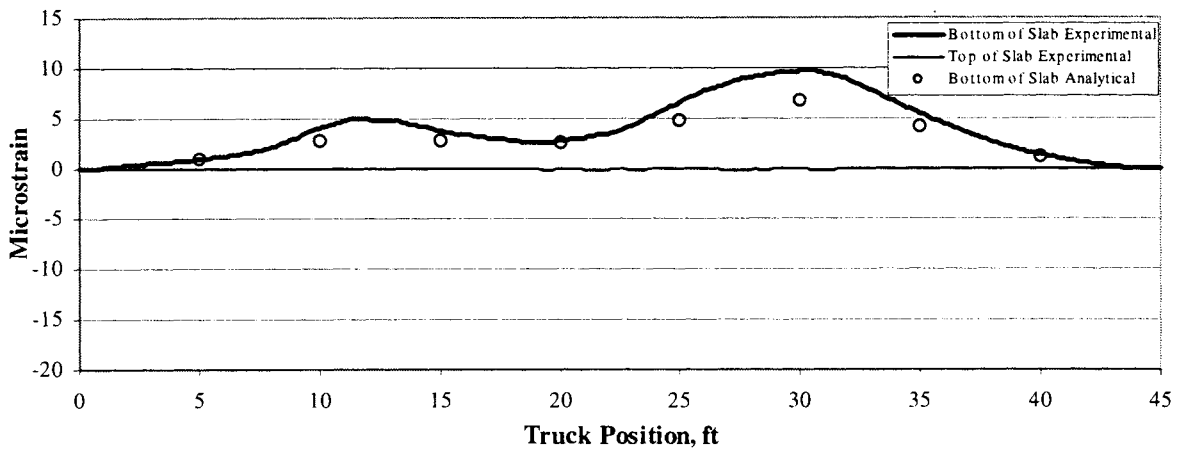


c. Location L21.

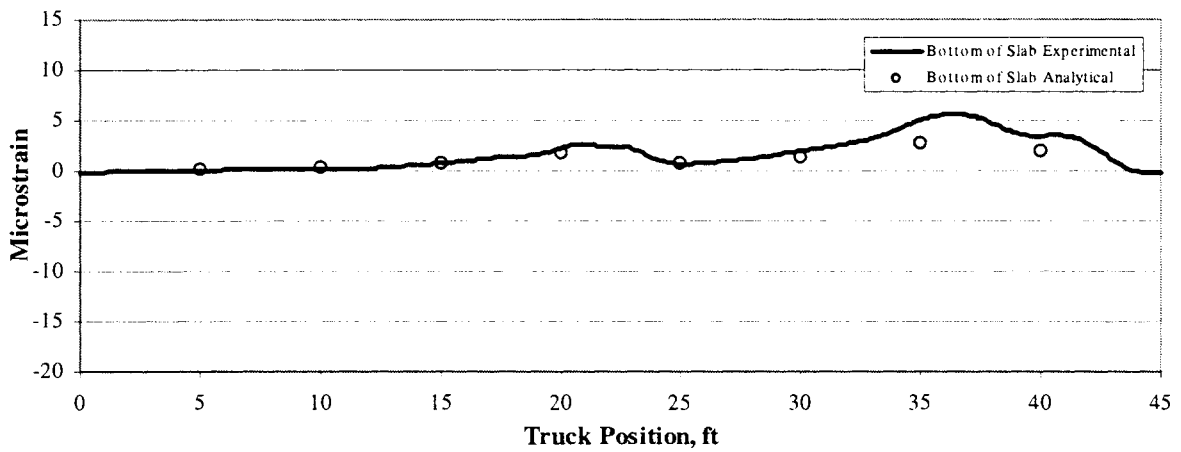
Figure 5.38. Bridge #7: Strain plots on the East side of the construction joint for truck Path Y3.



a. Location L16.

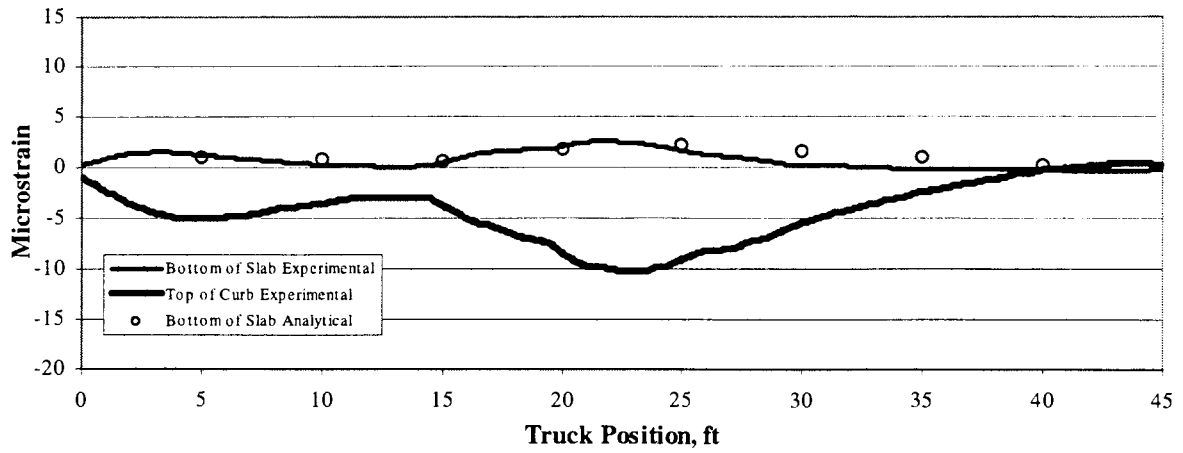


b. Location L17.

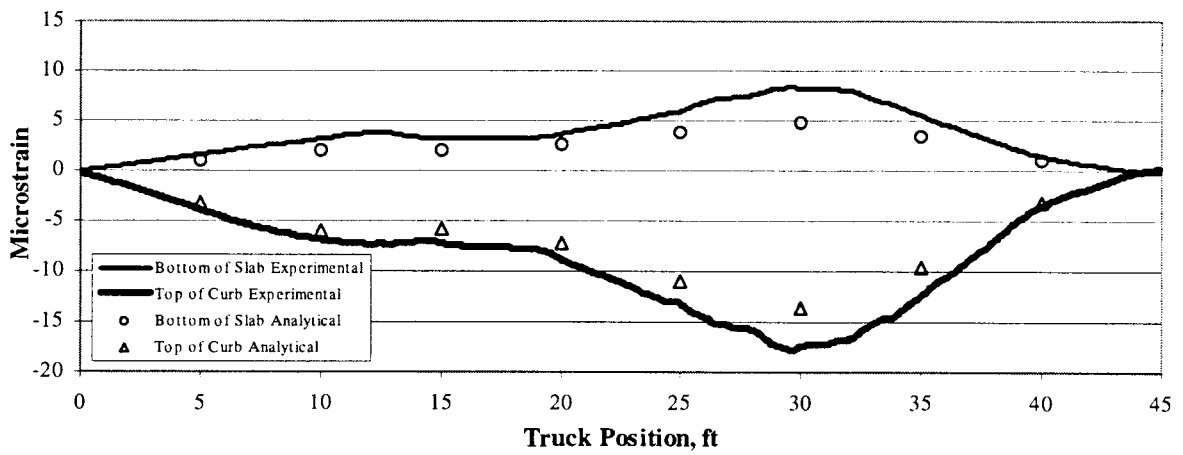


c. Location L18.

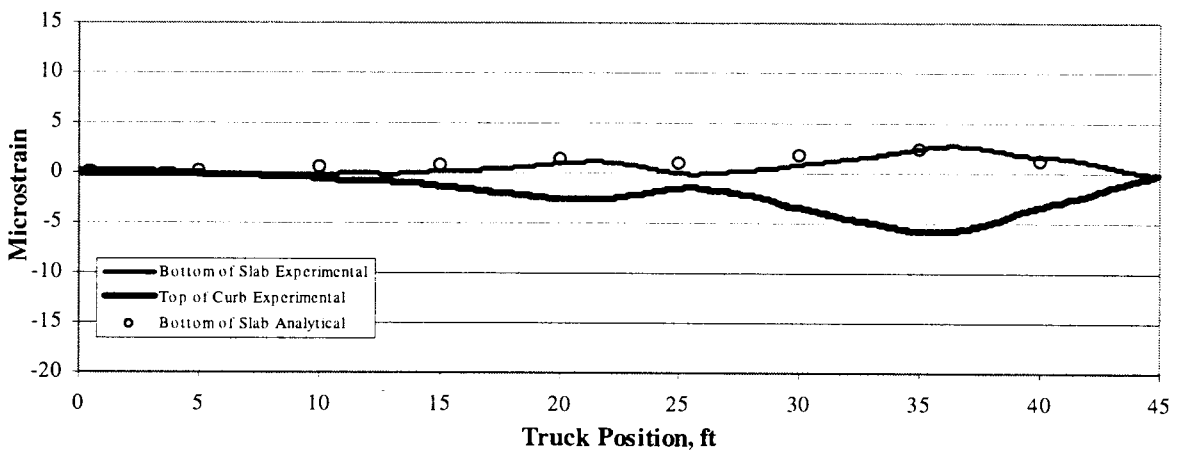
Figure 5.39. Bridge #7: Strain plots on the West side of the construction joint for truck Path Y3.



a. Location L22.

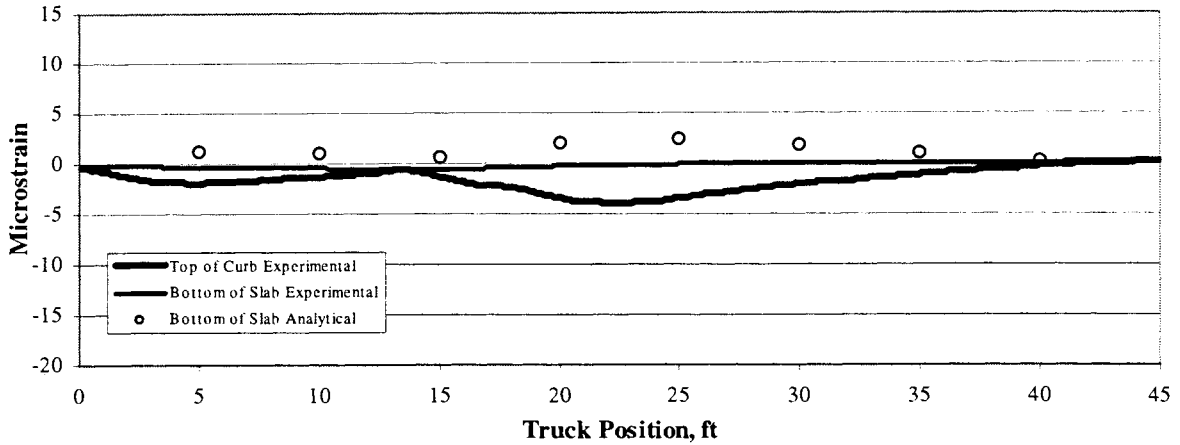


b. Location L23.

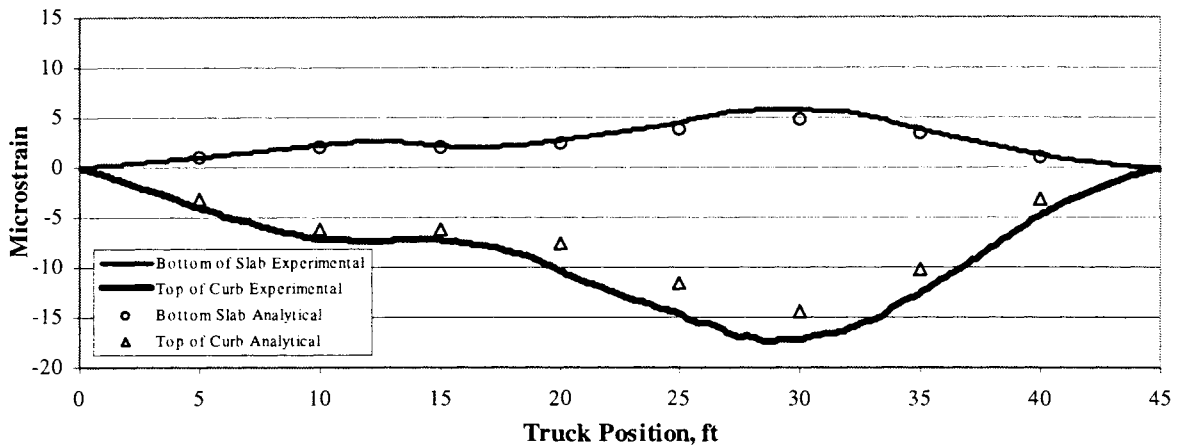


c. Location L24.

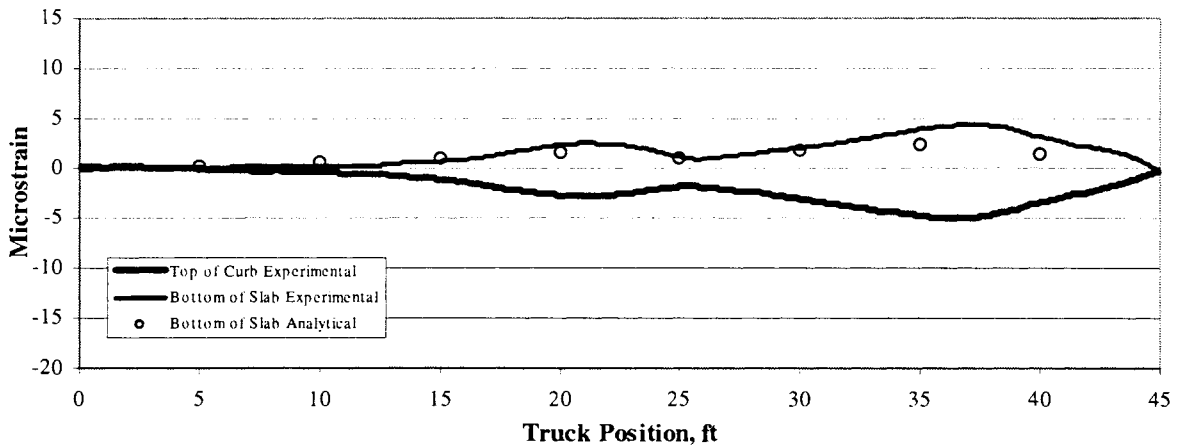
Figure 5.40. Bridge #7: Strain plots at the East curb for truck Path Y1.



a. Location L1.

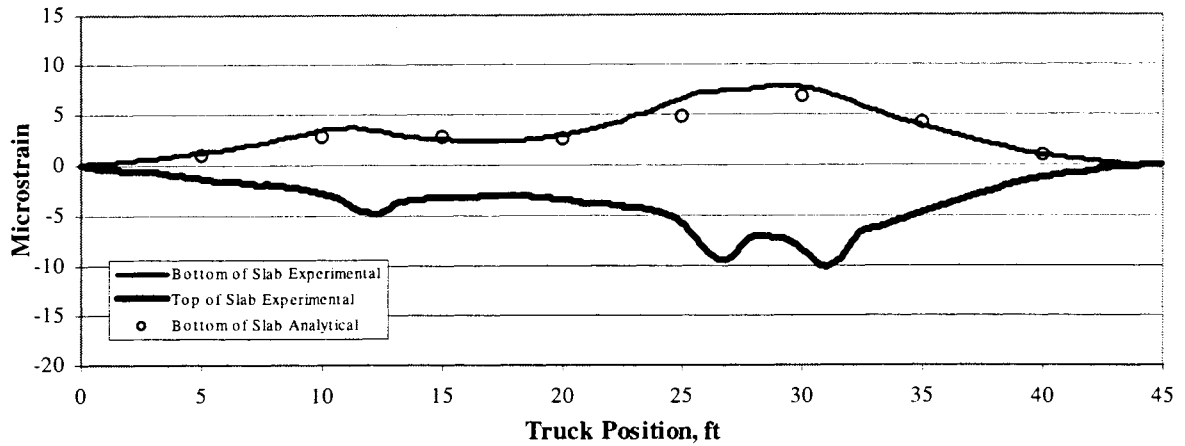


b. Location L2.

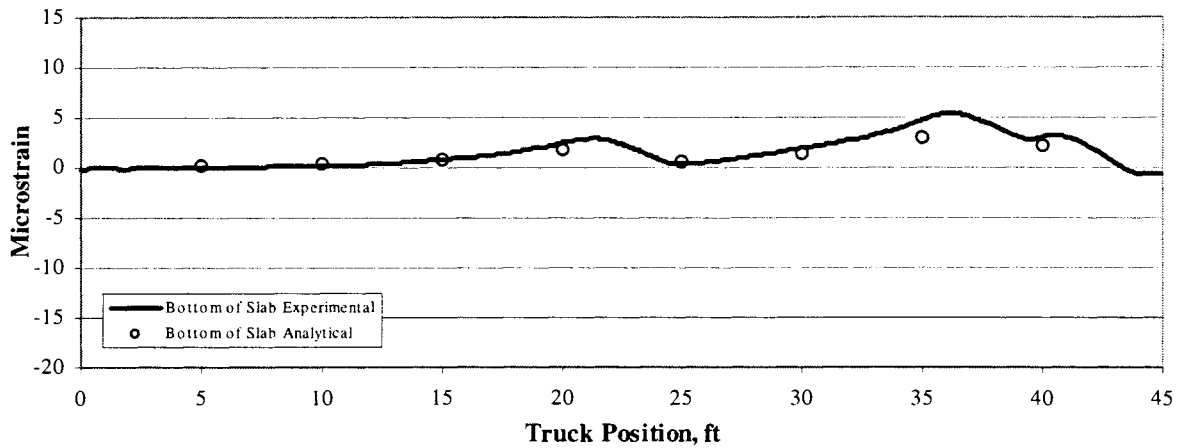


c. Location L3.

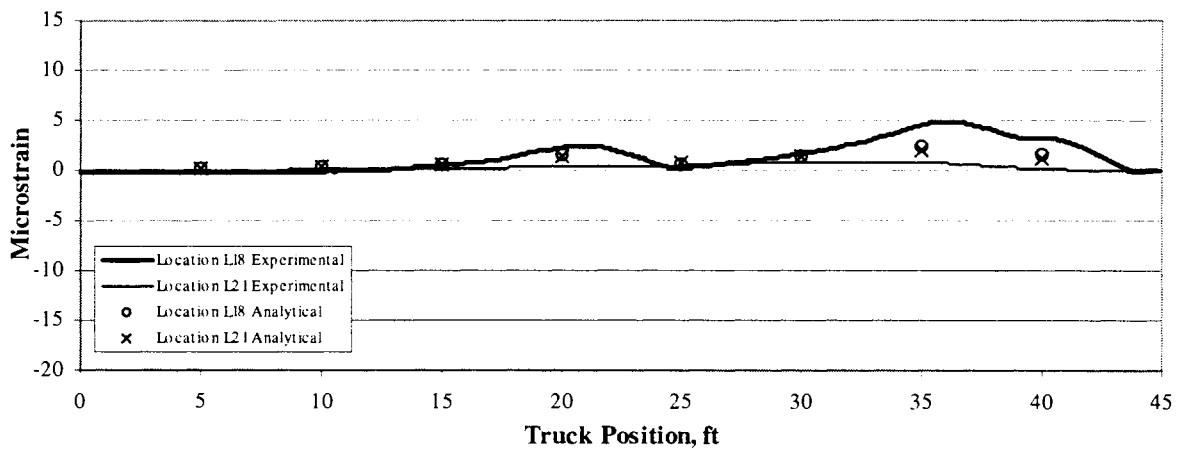
Figure 5.41. Bridge #7: Strain plots at the West Curb for truck Path Y4.



a. Location L14.



b. Location L15.



c. Strains for gages at the bottom of the slab to illustrate shear transfer.

Figure 5.42. Bridge #7: Typical strain plots for truck Path Y2.

By using this optimized model with the appropriate rating trucks and by applying dead load to the structure, the rating model was created. Dead load applied in the analytical model includes the self-weight of the concrete slab and a superimposed dead load of 126.8 lb/ft. The superimposed dead load was obtained from calculations previously performed by the bridge engineers at the Iowa DOT and accounts for the steel rail and the additional slab weight. For rating purposes, appropriate design trucks were considered:

- Path A: The driver side wheel line 7 ft from the East curb.
- Path B: The driver side wheel line 12 ft from the East curb.
- Path C: The driver side wheel line 17 ft from the East curb.
- Path D: The driver side wheel line 22 ft from the East curb.
- Path E: The driver side wheel line 1 ft from the West curb.
- Path F: The driver side wheel line 11 ft from the East curb.

Each path was analyzed at 1 ft intervals. This bridge was designed as a two-lane bridge, so truck path envelopes were created to account for two trucks applied on the structure at the same time:

- Envelope 1: Path A combined with Path C.
- Envelope 2: Path B combined with Path D.
- Envelope 3: Path E combined with Path F.

Individual member capacities were calculated following appropriate AASHTO Standard Specifications (4). Ratings by the LFD Method and by using the BDI Software are presented in Table 5.44 and Table 5.45, respectively. Table 5.46 summarizes the percent difference between inventory ratings by the LFD Method and by using the BDI Software. The critical rating condition is 0.77 by the LFD Method and 1.57 by the BDI Method for a difference of 103.9 %.

Table 5.44. Bridge #7: Design Truck Rating Factors by the LFD Method.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Deck	0.77	1.29	2.10	3.51	0.79	1.32	2.73	4.56	0.88	1.47	2.76	4.61

Table 5.45. Bridge #7: Design Truck Rating Factors by the BDI Method^a.

Section	HS-20				H-20				Type-3			
	Flexure		Shear		Flexure		Shear		Flexure		Shear	
	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.	Inv.	Ope.
Deck	1.57	2.62	1.95	3.26	1.61	2.69	2.31	3.86	1.94	3.24	2.76	4.61

^a Edge stiffening included.

Table 5.46. Bridge #7: Percent difference in Design Truck Rating Factors between LFD Method and BDI Software.

Section	HS-20		H-20		Type-3	
	Flexure	Shear	Flexure	Shear	Flexure	Shear
Deck	103.9	-7.1	103.8	-15.4	120.5	0.0

6. CONCLUSIONS AND RECOMMENDATION

The following briefly summarizes the information previously presented. In addition, conclusions and recommendations based on this work are provided.

6.1 SUMMARY

- **The model development process used herein was verified by comparison with a previously analyzed bridge.** The percent error for the model developed by BDI was 6.0 %, while the model described herein using a similar procedure was 5.7 %. Both bridge analyses had a correlation coefficient of 0.97 and had similar section properties in all but one instance.
- **The partial proof load test completed for Bridge #1 showed that the model accuracy remains approximately the same independent of the load truck used.** A limitation of this partial proof load test is that the bridge was assumed to behave with linear strains: A full truck was used to obtain the optimized model. This model using the full truckload had an error of 1.8 %, while the other truckloads used in the same model gave a 2.4 % and 5.5 % for the half-full and empty truck, respectively.
- **Bridge #2 indicated that strains can be predicted at locations without gages installed.** The optimized model percent error is approximately the same when including a limited number of gages as when including all gages (to predict strains). The optimized model with a limited number of gages had a 1.8 % error, while the percent error for the same model using gages at predicted locations gave a 2.1 %.
- **For the HS-20 load vehicle, most bridges had a flexural rating greater than that obtained using a codified approach.** The two steel girder bridges with timber decks had BDI ratings that were 47 % greater (average difference) than the LFD ratings. The three steel bridges with concrete decks tested had BDI ratings that were 57 % greater (average difference). The two concrete slab bridges had BDI ratings that were 117 % greater (average difference). The difference in the rating values for the five steel girder bridges were due to issues such as increased exterior beam stiffness due to the presence of reinforced concrete parapets and presence of unintended composite action. The rating increases for the two concrete slab bridges were credited to a more accurate analysis of a plate structure.
- **For the HS-20 load vehicle, most bridges had a shear rating greater than that obtained using a codified approach.** The two steel girder bridges with timber decks had BDI ratings that were 49 % greater (average difference) than the LFD ratings, the three steel bridges with

concrete decks tested had ratings that were 40 % greater (average difference), and the two concrete slab bridges had ratings that were –5.5 % smaller (average difference).

- **For all critical bridge sections, the BDI Software ratings were greater than the LFD Method ratings.** The critical BDI ratings (one critical rating value per bridge) varied from 0.83 to 1.57 with an average value of 1.28. The critical LFD ratings varied from 0.67 to 1.32 with an average critical value of 0.86. These results indicate that the critical BDI ratings were 48 % greater than the critical LFD ratings.
- **Strain errors (when comparing analytical with experimental strains) for all investigated bridges varied from 1.8 % to 12.5 %.** The two timber deck bridges had an average optimized strain error of 2.0 % and an average correlation coefficient of 0.99. The three steel-girder bridges had an averaged optimized strain error of 6.0 % and an average correlation coefficient of 0.97. The two concrete slab bridges had an average optimized strain error of 11.2 % and an average correlation coefficient of 0.95.
- **All BDI Software ratings for non-composite timber-deck steel-girder bridges are greater than the codified ratings.** The rating values for the BDI Software compared well with the LFD Method. For such bridges, all BDI Software rating values were greater than the LFD Method values.
- **Most BDI Software ratings for composite concrete-deck steel-girder bridges are greater than the codified ratings.** Even though some values were lesser, all critical BDI Software rating values (e.g. inventory rating values less than 1) were greater than the LFD Method values.
- **Most BDI Software ratings for concrete slab bridges are significantly greater than the codified parameters.** Even though the strains on such bridges were difficult to predict, once an optimized model has been created, all ratings for flexure were multiple times greater the codified ratings. However, the BDI Software ratings for shear were slightly smaller in magnitude than the codified ratings.
- **All operating rating values were greater than one when applying both methods.** The critical operating values were 1.37 for the BDI Method (Bridge #4) and 1.12 for the LFD Method (Bridge #6).

6.2 CONCLUSIONS

- **The sensitivity of live load moments from the BDI Software depends on selecting accurate values for the location of the neutral axis.** As shown in the sensitivity study for

Bridge #1, the live load moments varied from 1,415 K-in to 1,560 K-in when the location of the neutral axis for an interior beam at midspan was varied by 4 in. This represents an increase of 10 %. Further, the model accuracy varied from 7.3 % to 5.8 % when changing the neutral axis location as described. These results indicate that even though the model accuracy does not change significantly (i.e., “good” models can be created with multiple neutral axis locations), the live load moments may change considerably.

- **It is possible to predict strains at locations where no gages were installed.** As described previously, the optimized model with a limited number of gages resulted in a 1.8 % error, while the percent error for the same model using gages at predicted locations had a 2.1 % error.
- **Strain behavior for non-composite, timber-deck, steel-girder bridges can be predicted very accurately since the average optimized strain error was 2.0%.** Based on the results for the two timber-deck steel-girder bridges investigated, the optimized models returned strains that correlated very well with the measured strains, and behavior at non-instrumented sections can accurately be predicted.
- **Strain behavior for composite, concrete-deck, steel-girder bridges can also be accurately predicted since the average optimized strain error was 6.0%.** Based on the results for the three concrete deck steel girder bridges investigated, the optimized models correlated well with the measured strains. However, composite bridges with variable effective slab widths caused problems since it is difficult to accurately predict these widths.
- **Strain behavior in concrete slab bridges can not be as accurately predicted as in steel-girder bridges since the average optimized strain error was 11.2%.** Based on the results from the two investigated concrete slab bridges, the optimized models predicted strains that correlated relatively well with the measured strains. However, as previously discussed, a “good” model has an optimized error of less than 10%. Moreover, these two bridges were atypical regarding bridge behavior (i.e., experimental data indicated strain asymmetry, shear non-transfer, etc.), hence the load distribution was difficult to predict.

6.3. RECOMMENDATIONS

- **Use of the BDI system for load rating of bridges should be continued.** The finite element approach used in this BDI Software is more accurate than the conventional LFD Method (AASHTO Standard Specifications (4) or other conventional rating procedures), thus more accurate ratings are usually obtained when using the BDI system.

- **Diagnostic load testing results can be used to extrapolate load ratings for significantly heavier trucks.** As described previously, Bridge #1 proved that it is possible to predict strains with heavier trucks. However, this conclusion depends on linear bridge behavior, and if non-linear behavior is expected, further load testing regarding these issues are recommended to observe the bridge behavior under such circumstances.
- **The following policy and procedure recommendations have been developed for bridge load evaluation decisions:**
 - Steel-girder bridges with timber decks usually exhibit non-composite behavior and insignificant end restraint.
 - Unintended composite action may occur on steel-girder bridges with concrete decks even if they are designed as non-composite.
 - Most steel-girder bridges with concrete decks exhibit significant end restraint even if the end restraint conditions do not indicate such behavior.
- **Load evaluation results from systematic testing of a significant number of bridges of one type to other similar untested bridges may be extrapolated as follows:**
 - It is only possible to make a statement about the steel-girder bridges with timber decks since the strains in these bridges were accurately predicted: the HS-20 LFD Method rating factors will be similar to the BDI rating factors by a factor (once the LFD Method rating factor is obtained, one can calculate the BDI Method rating value by multiplying the LFD Method rating factor by a factor). This assumption applies for both flexure and shear.
- **Investigation of more conventional concrete slab bridges with the BDI system is recommended.** The two concrete slab bridges tested in this investigation (e.g. Bridge #6 and Bridge #7) do not represent “normal” behavior due to:
 - The non-symmetric behavior in the transverse direction, and the earth-fill that made it difficult to install gages on top of the slab, thus neutral axis locations were not possible to obtain (Bridge #6).
 - The construction joint that did not transfer loads linearly across the joint (Bridge #7).

REFERENCES

1. A. G. Lichtenstein & Associates, Inc., "Manual for Condition Evaluation and Load and Resistance Factor Rating of Highway Bridges," Pre-Final Draft Manual, National Cooperative Highway Research Program, March 1999.
2. American Association of State Highway and Transportation Officials, "LRFD Bridge Design Specifications," First Edition, Washington, D. C.: American Association of State Highway and Transportation Officials, 1994.
3. American Association of State Highway and Transportation Officials, "Manual for Condition Evaluation of Bridges," 1994, pp. 84-87.
4. American Association of State Highway and Transportation Officials, "Standard Specifications for Highway Bridges," 16th Edition, Washington, D. C.: American Association of State Highway and Transportation Officials, 1996.
5. American Institute of Steel Construction, "Manual of Steel Construction." American Institute of Steel Construction, Inc., Sixth Edition, 1963.
6. American Institute of Steel Construction, "Manual of Steel Construction, Load and Resistance Factor Design, Volume I," American Institute of Steel Construction, Inc., Second Edition, 1994.
7. American Institute of Steel Construction, "Steel Construction," American Institute of Steel Construction, Inc., First Edition, 1930.
8. American Institute of Steel Construction, "Steel Construction, A Manual for Architects, Engineers and Fabricators of Buildings and Other Steel Structures," American Institute of Steel Construction, Inc., Fourth Edition, 1941.
9. Bridge Diagnostics, Inc., "Load Testing and Load Rating Eight State Highway Bridges in Iowa," Report submitted to Iowa Department of Transportation, November 1999.

10. Bridge Diagnostics, Inc., "Integrated Approach to Load Rating Instruction Manual", 2001.
11. Lichtenstein, A. G., "Manual for Bridge Rating Through Load Testing.", NCHRP Project, 1998.
12. National Bridge Inventory, NBI Report, 2001.
http://www.nationalbridgeinventory.com/nbi_report_200115.htm.
13. National Bridge Inventory, NBI Report, 2001.
<http://www.nationalbridgeinventory.com/iowa.jpg>.
14. Xanthakos, P. P., Theory and design of bridges, New York: John Wiley & Sons, Inc., 1994.

ACKNOWLEDGEMENTS

The work described in this report was conducted by the Bridge Engineering Center at Iowa State University and sponsored by the Iowa Highway Research Board and Project Development Division of the Iowa Department of Transportation.

I would like to thank the Bridge Engineer at Iowa Department of Transportation, Scott Neubauer for his input in providing information of the Highway Bridges, and Dave Anthony for his input in providing information on the County Bridges.

I would also like to thank my major professors Dr. Terry J. Wipf and Dr. F. Wayne Klaiber for their guidance throughout the completion of this research project. I also thank Dr. Brent Phares and Dr. Loren W. Zachary for serving on my Program of Study Committee. Doug Wood also deserves recognition for his involvement in the field-testing throughout the project.

Special thanks are accorded to the following graduate civil engineering students for their assistance with the experimental portion of the project: A. J. Samuelson, and Brian Kempers. Special thanks are also extended to Dr. Brent Phares and Brett Commander for their assistance with the analytical portion of the project.

APPENDIX A

STATE ENGINEER'S QUESTIONNAIRE

Iowa State University's Bridge Engineering Center

2901 S. Loop Drive, Suite 3100, Ames, Iowa 50010-8632
Phone: 515-294-9501 ~ Fax: 515-294-0467



This research is sponsored by
the Iowa Highway Research Board
and the Project Development Board
of the
Iowa Department of Transportation.

Development of a Bridge Load Testing Process for Load Evaluation

Please answer all eight (8) questions in this voluntary survey to the best of your ability. Before completing the survey online, you may wish to review it and gather any information you may need.

If you have questions about the survey, please contact Dr. Brent Phares, 515-294-5879,
bphares@iastate.edu
Bridge Engineering Center
Iowa State University Research Park
2901 S. Loop Drive, Suite 3100
Ames, IA 50010.

If you experience difficulties with this web page, please contact the [webmaster](#).

Contact information

Organization:	<input type="text"/>
Questionnaire completed by:	<input type="text"/>
Position/Title:	<input type="text"/>
Address:	<input type="text"/>
City/State/Zip:	<input type="text"/>
Phone No.:	<input type="text"/>
Fax No.:	<input type="text"/>
Email Address:	<input type="text"/>

Questionnaire

1. Are you currently using nondestructive load testing, proof or diagnostic, for the purposes of rating bridges?

- ☐ a) Yes, both proof and diagnostic testing.
- ☐ b) Yes, proof testing only.
- ☐ c) Yes, diagnostic testing only.

If yes, approximately how many bridges are tested per year?

- ☐ d) No, but planning on starting a program.
- ☐ e) No, no bridge testing for rating purposes.

If no, please explain why not (this completes the questionnaire).

2. Do you have formal policies and procedures in place as to how bridge test data are used, i.e., for rating purposes or in general?

- ☐ No
- ☐ Yes

If yes, please describe your policies and procedures. (If a formal document exists, please send a copy to Brent Phares at the address above.)

3. Does your state DOT

- ☐ a) conduct the testing in-house.
- ☐ b) contract with consultants for testing.
- ☐ c) use a combination of in-house and consultant testing.

4. Is a commercial testing system used?

- ☐ No
- ☐ Yes

If yes, what system?

Do you use a commercial software program to verify field data?

- ☒ No
☐ Yes

If yes, what program?

6. For the following hypothetical bridge, how much would be budgeted for the nondestructive testing, analysis, and load rating?

Thirty-year-old, 60-ft, simply supported single span bridge carrying two-lane road (medium ADT) over a small creek, maximum height above the creek is 15 ft.

Superstructure: Steel, five-girder superstructure (rolled shapes); composite concrete deck. Substructure: Concrete abutments.

- ☒ a) Less than \$5,000
☐ b) \$5,000 to \$10,000
☐ c) \$10,000 to \$15,000
☐ d) More than \$15,000

7. When calculating ratings, do you allow to be present, but not codified, one or more of the following bridge properties? (you may select more than one)

- ☐ a) unintended composite action
☐ b) edge rail stiffness
☐ c) restraint at the abutments or piers
☐ d) other

If you selected "other," please specify.

8. Do you extrapolate the results from load testing to issue permits for overload vehicles?

- ☒ No
☐ Yes

If yes, what are your policies related to load testing and permit vehicles?

Would you like to receive a copy of the survey results?

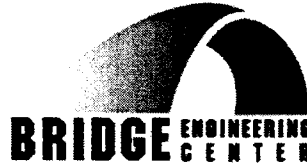
- ☐ No
☒ Yes

Thank you for completing this survey! [Submit Survey](#)

APPENDIX B

COUNTY ENGINEER'S QUESTIONNAIRE

Iowa State University's Bridge Engineering Center
2901 S Loop Drive, Suite 3100, Ames, Iowa 50010-8632
Phone: 515-294-9501 ~ Fax: 515-294-0467



Development of a Bridge Load Testing Process for Load Evaluation



Please answer all questions in this voluntary survey to the best of your ability.

This research is sponsored by the Iowa Highway Research Board and the Project Development Board of the Iowa Department of Transportation.

If you have any questions about the survey, please contact Dr. Brent Phares, 515-294-5879, fax: 515-294-0467
bphares@iastate.edu
Bridge Engineering Center
Iowa State University Research Park
2901 S. Loop Drive, Suite 3100
Ames, IA 50010

Contact Information

Organization:
Questionnaire completed by:
Position/Title:
Address:
City/State/State:
Phone No.:
Fax No.:
Email Address:

Questionnaire

- #1 **Are you currently using nondestructive load testing, proof or diagnostic, for the purposes of rating bridges?**
- a) Yes, both proof and diagnostic testing.
 - b) Yes, proof testing only.
 - c) Yes, diagnostic testing only.
If yes, approximately how many bridges are tested per year? _____
 - d) No, but planning on starting a program.
 - e) No, no bridge testing for rating purposes.

ANSWER:

If no, please comment on why not.

#2 Does your organization

- a) conduct the testing in-house.
- b) contract with consultants for testing.
- c) use a combination of in-house and consultant testing.
- d) use State DOT forces

ANSWER:

#3 For the following hypothetical bridge, what would you budget (if currently using nondestructive load testing) or be willing to budget (if not currently using nondestructive load testing) for testing, analysis, and load rating?

Thirty-year-old, 60 ft, simply supported single span bridge carrying two-lane road (medium ADT) over a small creek, maximum height above the creek is 15 ft.

Superstructure: Steel, five-girder superstructure (rolled shapes); composite concrete deck.

Substructure: Concrete abutments.

- a) Less than \$5,000
- b) \$5,000 to \$10,000
- c) \$10,000 to \$15,000
- d) More than \$15,000

ANSWER:

Would you like a copy of the survey results?

- a) No
- b) Yes

ANSWER:

Thank you for completing this survey!

APPENDIX C.

**A STEP-BY-SPEP PROCEDURE FOR BRIDGE RATING BASED ON
PHYSICAL TESTING**

Input clicker distance manually for all truck path files:

- Open the first truck path file (dat-file) in WordPad or Notepad. Scroll down to the bottom and input the correct field clicker distance.
- Repeat for all truck path files.

If two strain files for each path are created, verify that both files are approximately the same:

- Open the two files in WinGRF and compare the strains. Choose linear drift if it desired to zero the field strains at start and finish of field data information.
 - File → Load STS Data File → Open both files → Linear drift both files
- Select appropriate locations to compare strains for the two chosen files.
 - Data comparison → Strain plots
- Repeat for all truck paths

Average and filter the two strain files for each path to create one file for each path be used in the modeling process:

- For Path Y1, open the two raw field strain data files in WinGRF.
 - File → Load STS Data File → Open both files → Linear drift both files
- Average the two raw data files.
 - Data Processing → Average STS files → Save as “average_Y1” → OK
- Open the averaged file in WinGRF and decimate to smoothen out the graph.
 - File → Load STS Data File → Open “average_Y1” → Linear drift → Data Processing → Filter/Decimate → OK → Save as “filter_Y1”
- Repeat for all truck paths. All strain files used from here are the “filter_Y”-files (not the raw data files or the “average_Y”-files).

Verify strain symmetry:

- Check field strains in WinGRF for symmetric truck paths in the transverse direction to verify strain symmetry.
- Repeat for symmetric paths in the longitudinal direction.

Locate the neutral axis to determine any composite section at a selected location:

- Check field strains in WinGRF by comparing strains at top and bottom gages at the selected location. The neutral axis location should lie at the center of the web for a symmetric non-composite steel beam. A neutral axis location near the top flange is an indication of composite action for the selected section.
 - Data comparison → Neutral axis plots.

Observe if the bridge exhibits any end restraint:

- Select an appropriate truck path. Select strain locations near the abutment or near the pier (if any) and observe the presence of tension in the top flanges (if the neutral axis location lies below the top flange) and compression in the bottom flanges.

Create an analytical one-span bridge model in WinGEN by using the filtered strain file:

- Define model geometry, plan parameters, and transverse members for “Bridge #1”. Add transverse members where floor beams are located.
 - File → New Model File → Model Geometry → Beam/Slab Bridge → Enter “Bridge #1” → Define Plan Parameters → Enter parameters → OK → Span Length/Beam Spacing → Enter Parameters → Transverse Members → Add transverse members → Done
- Add spring locations:
 - Define Plan Parameters → Enter parameters → OK → Span Length/Beam Spacing → Enter Parameters → Spring Locations → Add Springs → All done
- Create a W27x84 steel cross-section:
 - Model Parameters → Define X-section → AISC Steel Sections → W33–W27 → W27x84 → OK
- For any cross-sections not defined in the software, the user must define the sections:
 - Model Parameters → Define X-sections → Create New Cross-section → User defined → Add Quadrilateral → Enter parameters → OK
- Assign the W27x84 to the model:
 - Model Parameters → Assign X-sections → “Select group” → Assign Group → Assign by dragging over the desired elements, and right-click when done → OK
- Repeat for all cross-sections, such as concrete slab deck, rotational spring, curb dimensions, and user defined sections.
- Apply Boundary Conditions so that bridge is simply supported:
 - Model Parameters → Boundary Conditions → Check displacement boxes in X- Y- and Z-direction → Assign BC → OK
- Define field truck:
 - Load Definition → Define Truck → OK
- Define Truck Paths:
 - Load Definition → Define Truck Paths → Add Path → “Enter parameters” → Apply → OK
- Retrieve field test strain data and apply to model:

- Model Parameters → Retrieve STS Data → Check “Linear Varying Offset” → STS Data File → Select “filter_Y1” → Apply secondary gage factors if strain gages other than standard has been used → Apply → OK
- Repeat for all truck paths.
- Enter optimization parameters:
 - Model Parameters → Optimization Parameters → New Variable → W27x84 → Select “Iy” → Set lower limit to 80 % of non-composite value and upper limit to 120 % of composite value → OK → OK
- Repeat for all desired parameters.
- Select analysis options for optimization:
 - Analysis → SAC Options → Check “STS Data Comparison” and “Parameter Optimization” → OK
- Save both model file and analysis file:
 - File → Save Model File As → “Model”
 - File → Save SAC File as → “Model”
- Two files have now been created. The model file is named Model.mod, and the analysis file needed to run SAC is named Model.inp.

Run the input analysis file using WinSAC:

- File → Open → “Model”
- SAC will perform iterations and change the user defined optimization parameters in order to reach the smallest strain difference between the analytical and experimental strains.

View input/output/strain/property files in SAC:

- View data → Input/Output/Strains/Properties

Create a new model in WinGen and update the optimized properties to use for HS-20 truck rating:

- The updated optimized model will be named Updated.mod.
 - File → Open Model File → “Model” → File → Save Model File As → “Updated” → Model Parameters → Define X-sections → Update (optimized) parameters → “Model” → Done → File → Save Model File As → “Updated” → OK
- However, the optimization box needs to be checked off.
 - Analysis → SAC options → Check off “Parameter optimization” → File → Save Model File → File → Save SAC File As → “Updated”

Run updated analysis file in SAC to verify that the model accuracy is the same:

- File → Open → “Updated”

Use the updated file and apply dead load in WinGEN:

- Load Definition → Dead Load → Self Weight → Check box so that program will apply the self weight of the user defined parameters → OK
- Additional dead load, such as gravel/dirt/asphalt overlay and rail must be added.

Apply HS-20 Design Truck to model in WinGEN:

- Load truck dimensions from the library if there is one. If not, create a new truck as previously described.
 - Load Definition → Define Truck → Library → Library File → HS-20 → OK
 - Load Definition → Define Truck Paths → Truck (library) → HS-20 → OK → Apply → Adjust Parameters so that the truck will be in critical position with appropriate longitudinal intervals → Apply → OK
- Apply additional truck paths with appropriate transverse intervals.

Apply rating factors in WinGEN:

- For LFD Method, the Dead Load Factor is 1.3, the Live Load Factor is 2.17, and the impact is 0.3 (use AASHTO Standard Specifications for more exact impact factor).
 - Rating → Load Factors → “LFD” → 1.3 → 2.17 → 0.3 → Save Method → OK

Enter Capacities for W27x84 in WinGEN:

- Rating → Capacities → Enter “LFD” → New Method → Select W27x84 → Enter capacities as desired → Apply → OK
- Repeat for all desired section parameters.

Input truck path envelopes in WinGEN if the bridge is designed for two or more trucks:

- Rating → Combine Truck Paths → Add Combination → Select appropriate design truck paths → Apply → OK
- Apply additional truck path envelopes if necessary.

Save rating option in WinGEN:

- Analysis → SAC options → Check “Perform Load Rating” → OK
- File → Save Model File As → “Rating”
- File → Save SAC File As → “Rating”

Run analysis file in WinSAC to perform load rating:

- File → Open → “Rating”

Extract Live Load Moments by exploring the output file in SAC:

- View Data → Output

Repeat for other rating truck vehicles as desired (e.g. H-20, Type-3, etc.)

APPENDIX D

RATING EVALUATION BY LFD METHOD

g

D.1. RATING FOR BRIDGE #1Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{wood}} = 50 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of wood deck and curb} \quad 3.3.6$$

$$w_{\text{asphalt}} = 9 \frac{\text{lb}}{\text{ft}^2} \quad \text{Weight of a one-inch thick asphalt plank on top of the wood deck} \quad 3.3.6$$

$$w_{\text{gravel}} = 100 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of gravel overlay on top of asphalt} \quad 3.3.6$$

$$F_y = 30\text{ksi} \quad \text{Steel strength from Steel Construction Manual, 1930, p.18}$$

Interior GirderInput:

$$A_{\text{tf}} = 8.27\text{in} \times 0.685\text{in} \quad \text{Area of top flange} \quad A_{\text{tf}} = 5.665 \text{in}^2$$

$$A_w = 19.76\text{in} \times 0.43\text{in} \quad \text{Area of web} \quad A_w = 8.497 \text{in}^2$$

$$A_{\text{bf}} = 8.27\text{in} \times 0.685\text{in} \quad \text{Area of bottom flange} \quad A_{\text{bf}} = 5.665 \text{in}^2$$

$$t_{\text{tf}} = 0.685\text{in} \quad \text{Thickness of top flange}$$

$$b_w = 19.76\text{in} \quad \text{Width of web}$$

$$t_w = 0.43\text{in} \quad \text{Thickness of web}$$

$$t_{\text{bf}} = 0.685\text{in} \quad \text{Thickness of bottom flange}$$

Section Properties:

$$L = 43.67\text{ft} \quad \text{Design span of beam}$$

$$t_s = 4\text{in} \quad \text{Thickness of wood deck}$$

$$A_b = A_{\text{tf}} + A_w + A_{\text{bf}} \quad A_b = 19.827 \text{in}^2$$

$$d = t_{\text{tf}} + b_w + t_{\text{bf}} \quad \text{Total depth of steel} \quad d = 21.13 \text{in}$$

$$D = b_w \quad \text{Clear distance between flanges} \quad D = 19.76 \text{in}$$

Loads For Lane Loading:

$$P_s = 26k \quad \text{Point Load for Shear for Lane Loading} \quad \text{fig. 3.7.6.b}$$

$$P_m = 18k \quad \text{Point Load for Moment for Lane Loading}$$

$$\omega = 0.64 \frac{k}{\text{ft}} \quad \text{Uniform Load for Lane Loading}$$

Live Load Distribution Factor for Design Trucks:

$$S_b = 30.25\text{in} \quad \text{Average stringer spacing in ft} \quad S_b = 2.521\text{ ft} \quad \text{table 3.23.1}$$

$$DF = \frac{S_b}{4.5\text{ft}} \quad DF = 0.56$$

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.296 \quad 3.8.2.1$$

Maximum Live Load Moments:

Lane Load $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear fig. 3.7.6.b
 Uniform Load of 0.64 k/ft over the whole span
 All values are lane loads, therefore divide lane loads by 2
 so that lane loads are compatible with truck loads

$$\text{Uniform load:} \quad M1_{\text{Lane}} = \frac{\omega \times L^2}{8} \quad M1_{\text{Lane}} = 152.566 \text{ ftk}$$

$$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L \quad V1_{\text{Lane}} = 13.974 \text{ k}$$

$$\text{Point Load:} \quad M2_{\text{Lane}} = \frac{P_m \times L}{4} \quad M2_{\text{Lane}} = 196.515 \text{ ftk}$$

$$V2_{\text{Lane}} = P_s \quad V2_{\text{Lane}} = 26 \text{ k}$$

$$M_{LL} = \frac{1}{2} (M1_{\text{Lane}} + M2_{\text{Lane}}) \quad M_{LL} = 174.54 \text{ ftk}$$

$$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF \quad M_{LL_I_Lane} = 126.759 \text{ ftk}$$

$$V_{LL} = \frac{1}{2} (V1_{\text{Lane}} + V2_{\text{Lane}}) \quad V_{LL} = 19.987 \text{ k}$$

$$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF \quad V_{LL_I_Lane} = 14.516 \text{ k}$$

HS-20 Max moment occur when middle axle is placed at 24.1 ft from the end. Max shear occur for rear axle at the end.

$$P_1 = 16\text{k}$$

$$P_2 = 4\text{k}$$

$$x = 24.1 \text{ ft}$$

$$x = 24.1 \text{ ft}$$

$$M_{LL} = \frac{36\text{k} \times (L - x) \times (x - 4.67\text{ft})}{L} - 56\text{ftk}$$

$$M_{LL} = 257.461 \text{ ftk}$$

$$M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_HS20} = 186.979 \text{ ftk}$$

$$V_{LL} = P_1 + \frac{L - 14\text{ft}}{L} \times P_1 + \frac{L - 28\text{ft}}{L} \times P_2$$

$$V_{LL} = 28.306 \text{ k}$$

$$V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_HS20} = 20.557 \text{ k}$$

H-20	Max moment occur when middle axle is placed at 23.2 ft from the end. Max shear occur for rear axle at the end.	$P_1 = 16k$ $P_2 = 4k$
	$x = 23.2ft$	$x = 23.2 ft$
	$M_{LL} = \frac{20k \times (L - x) \times (x - 2.8ft)}{L}$	$M_{LL} = 191.247 ftk$
	$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$	$M_{LL_I_H20} = 138.892 ftk$
	$V_{LL} = P_1 + \frac{L - 14ft}{L} \times P_2$	$V_{LL} = 18.718 k$
	$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$	$V_{LL_I_H20} = 13.594 k$
Type 3	Max moment occur when middle axle is 23.5 ft from the end. Max shear occur for rear axle at the end.	$P_1 = 8.5k$ $P_2 = 8k$
	$x = 23.5ft$	$x = 23.5 ft$
	$M_{LL} = 25k \times (x - 3.44ft) \times \frac{L - x}{L} - 34ftk$	$M_{LL} = 197.629 ftk$
	$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$	$M_{LL_I_Type3} = 143.527 ftk$
	$V_{LL} = P_1 + \frac{L - 4ft}{L} \times P_1 + \frac{L - 19ft}{L} \times P_2$	$V_{LL} = 20.741 k$
	$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$	$V_{LL_I_Type3} = 15.063 k$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb, overlay and channel equally distributed to all girders/stringers.

Steel:	$w_b = w_{steel} \times A_b$	$w_b = 67.45 \frac{lb}{ft}$
Wood deck:	$w_w = w_{wood} \times t_s \times S_b$	$w_w = 42.014 \frac{lb}{ft}$
Rail:	Total volume of rail on each side of roadway based on field measurements was found to be 6570 in ³ . The uniform load is distributed equally over the eight girders.	
	$w_r = w_{steel} \times \frac{6570in^3}{L \times 8}$	$w_r = 5.331 \frac{lb}{ft}$
Curb:	Total volume of wood-curb on each side of the roadway based on field measurements was found to be 44278 in ³ . The uniform load is distributed equally over the eight girders.	
	$w_c = w_{wood} \times \frac{44278in^3}{L \times 8}$	$w_c = 3.667 \frac{lb}{ft}$
Overlay:	$w_o = w_{asphalt} \times S_b + w_{gravel} \times 3in \times S_b$	$w_o = 85.708 \frac{lb}{ft}$

$$\text{Channel: } w_{ch} = w_{steel} \times 6.47 \text{ in}^2 \times 4 \times \frac{S_b}{L} \quad w_{ch} = 5.082 \frac{\text{lb}}{\text{ft}}$$

Total Dead Load = sum w

$$DL = w_b + w_w + w_f + w_c + w_o + w_{ch} \quad DL = 0.209 \frac{\text{k}}{\text{ft}}$$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8} \quad M_{DL} = 49.883 \text{ ft-k}$$

$$V_{DL} = \frac{1}{2} \times DL \times L \quad V_{DL} = 4.569 \text{ k}$$

Capacities:

$$C = A_b \times F_y \quad C = 594.801 \text{ k} \quad (10-124)$$

$$AF_{tf} = A_{tf} \times F_y \quad \text{Top flange} \quad AF_{tf} = 169.948 \text{ k}$$

$$AF_w = A_w \times F_y \quad \text{Web above welded plate} \quad AF_w = 254.904 \text{ k}$$

$$AF_{bf} = AF_{tf} \quad \text{Bottom flange} \quad AF_{bf} = 169.948 \text{ k}$$

$$y = t_{bf} + \frac{b_w}{2} \quad \text{Distance from bottom of steel to PNA} \quad y = 10.565 \text{ in}$$

$$D_{cp} = \frac{b_w}{2} \quad \text{Depth of web in compression at PNA} \quad D_{cp} = 9.88 \text{ in}$$

Check compact:

$$b = \frac{8.27 \text{ in} - 0.43 \text{ in}}{2} \quad \text{Width of projecting flange element} \quad b = 3.92 \text{ in}$$

$$\frac{b}{t_w} \leq \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \frac{b}{t_w} = 9.116 \quad \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 11.865 \quad \text{OK!} \quad (10-93)$$

$$\frac{D}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \frac{D}{t_w} = 45.953 \quad \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 111.024 \quad \text{OK!} \quad (10-93)$$

Since not both of the two criteria above exceed 75% of limit => don't check (10-95)

$$M_n = F_y \times Z \quad (10-92)$$

$$y = 10.565 \text{ in} \quad \text{Distance from bottom of steel to PNA} \quad y = 10.565 \text{ in}$$

$$y_{bf} = y - \frac{0.685 \text{ in}}{2} \quad \text{Distance from PNA to C.G bottom flange} \quad y_{bf} = 10.223 \text{ in}$$

$$y_w = \frac{1}{2} \times \frac{D}{2} \quad \text{Distance from PNA to C.G web above PNA} \quad y_w = 4.94 \text{ in}$$

$$A_{tf} = 5.665 \text{ in}^2$$

Area of top flange

$$A_{tf} = 5.665 \text{ in}^2$$

$$A_w = 8.497 \text{ in}^2$$

Area of the whole web both above and below PNA

$$A_w = 8.497 \text{ in}^2$$

$$Z = 2 \times y_{bf} \times A_{tf} + 2 \times y_w \times \frac{A_w}{2}$$

Plastic section modulus

$$Z = 157.794 \text{ in}^3$$

$$M_n = F_y \times Z$$

$$M_n = 394.485 \text{ ft-k}$$

$$M_n = 4.734 \times 10^3 \text{ in} \times k$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$K = 5$$

For unstiffened beams and girders

$$D = 19.76 \text{ in}$$

Clear distance between flanges

$$t_w = 0.43 \text{ in}$$

Web thickness

$$\frac{D}{t_w} = 45.953$$

$$\frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 77.46$$

 \Rightarrow

$$C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 147.844 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p$$

$$V_n = 147.844 \text{ k} \quad (10-113)$$

Rating:

$$\text{Inventory:} \quad A_1 = 1.3 \quad A_{2i} = 2.17$$

$$\text{Operating:} \quad A_1 = 1.3 \quad A_{2o} = 1.3$$

$$\text{Lane Flexure: Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$$

$$RF = 1.198$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$$

$$RF = 2$$

$$\text{Shear: Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$$

$$RF = 4.505$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$$

$$RF = 7.52$$

$$\text{HS-20 Flexure: Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$$

$$RF = 0.812$$

		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	$RF = 1.356$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	$RF = 3.181$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	$RF = 5.31$
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	$RF = 1.094$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	$RF = 1.826$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	$RF = 4.811$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	$RF = 8.03$
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	$RF = 1.058$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	$RF = 1.767$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	$RF = 4.341$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	$RF = 7.247$

LOADS EXTRACTED FROM THE BDI-SOFTWARE

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 489.3 \text{ in} \times \text{k}$
			Live load	$M_{LL} = 1245 \text{ in} \times \text{k}$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 1.614 \times 10^3 \text{ in} \times \text{k}$
	Shear	Inventory	Dead load	$V_{DL_HS20} = 3.84 \text{ k}$
			Live load	$V_{LL} = 12.86 \text{ k}$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 16.672 \text{ k}$
H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 504.7 \text{ in} \times \text{k}$
			Live load	$M_{LL} = 962.3 \text{ in} \times \text{k}$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 1.248 \times 10^3 \text{ in} \times \text{k}$

Type-3	Shear	Inventory	Dead load	$V_{DL_H20} = 3.84k$
			Live load	$V_{LL} = 9.68k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 12.55k$
	Flexure	Inventory	Dead load	$M_{DL_Type3} = 504.3in \times k$
			Live load	$M_{LL} = 917.6in \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 1.19 \times 10^3 in \times k$
	Shear	Inventory	Dead load	$V_{DL_Type3} = 3.84k$
			Live load	$V_{LL} = 9.24k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 11.979k$

BDI Ratings:

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.17
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 1.953
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 3.949
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 6.591
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.506
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 2.514
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 5.246
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 8.756
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.58
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 2.637
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 5.495
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 9.173

Exterior GirderLive Load Distribution Factor:

overhang = 12in

Overhang of wood deck

$$S_b = \frac{S_b}{2} + \text{overhang}$$

1/2 stringer spacing + overhang

$$S_b = 2.26 \text{ ft}$$

table 3.23.1

$$DF_1 = \frac{S_b}{4.5 \text{ ft}}$$

$$DF_1 = 0.502$$

3.23.2.3.1.5

Find new DF for treating the exterior stringer as a simple beam

3.23.2.3.1.2

$$DF_2 = \frac{2.521 \text{ ft} - 2 \text{ ft}}{2.521 \text{ ft}}$$

$$DF_2 = 0.207$$

Use maximum distribution factor

$$DF = \max \left(\left(\begin{array}{c} DF_1 \\ DF_2 \end{array} \right) \right)$$

$$DF = 0.502$$

Maximum Live Load Moments:

Lane Load

 $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear

fig. 3.7.6.b

Uniform Load of 0.64 k/ft over the whole span

All values are lane loads, therefore divide lane loads by 2 so that lane loads are compatible with truck loads

$$\text{Uniform load: } M1_{\text{Lane}} = \frac{\omega \times L^2}{8}$$

$$M1_{\text{Lane}} = 152.566 \text{ ftk}$$

$$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L$$

$$V1_{\text{Lane}} = 13.974 \text{ k}$$

$$\text{Point Load: } M2_{\text{Lane}} = \frac{P_m \times L}{4}$$

$$M2_{\text{Lane}} = 196.515 \text{ ftk}$$

$$V2_{\text{Lane}} = P_s$$

$$V2_{\text{Lane}} = 26 \text{ k}$$

$$M_{LL} = \frac{1}{2} (M1_{\text{Lane}} + M2_{\text{Lane}})$$

$$M_{LL} = 174.54 \text{ ftk}$$

$$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_Lane} = 113.664 \text{ ftk}$$

$$V_{LL} = \frac{1}{2} (V1_{\text{Lane}} + V2_{\text{Lane}})$$

$$V_{LL} = 19.987 \text{ k}$$

$$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_Lane} = 13.016 \text{ k}$$

HS-20

Max moment occur when middle axle is placed at 24.1 ft from the end. Max shear occur for rear axle at the end.

$$P_1 = 16 \text{ k}$$

$$P_2 = 4 \text{ k}$$

$$x = 24.1 \text{ ft}$$

$$x = 24.1 \text{ ft}$$

$$M_{LL} = \frac{36 \text{ k} \times (L - x) \times (x - 4.67 \text{ ft})}{L} - 56 \text{ ftk}$$

$$M_{LL} = 257.461 \text{ ftk}$$

$$M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_HS20} = 167.663 \text{ ftk}$$

	$V_{LL} = P_1 + \frac{L - 14\text{ft}}{L} \times P_1 + \frac{L - 28\text{ft}}{L} \times P_2$	$V_{LL} = 28.306 \text{ k}$
	$V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$	$V_{LL_I_HS20} = 18.433 \text{ k}$
H-20	Max moment occur when middle axle is placed at 23.2 ft from the end. Max shear occur for rear axle at the end.	$P_1 = 16\text{k}$
	$x = 23.2\text{ft}$	$P_2 = 4\text{k}$
	$M_{LL} = \frac{20\text{k} \times (L - x) \times (x - 2.8\text{ft})}{L}$	$x = 23.2\text{ft}$
	$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$	$M_{LL} = 191.247 \text{ ftk}$
	$V_{LL} = P_1 + \frac{L - 14\text{ft}}{L} \times P_2$	$M_{LL_I_H20} = 124.544 \text{ ftk}$
	$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$	$V_{LL} = 18.718 \text{ k}$
Type 3	Max moment occur when middle axle is 23.5 ft from the end. Max shear occur for rear axle at the end.	$V_{LL_I_H20} = 12.189 \text{ k}$
	$x = 23.5\text{ft}$	$P_1 = 8.5\text{k}$
	$M_{LL} = 25\text{k} \times (x - 3.44\text{ft}) \times \frac{L - x}{L} - 34\text{ftk}$	$P_2 = 8\text{k}$
	$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$	$x = 23.5\text{ft}$
	$V_{LL} = P_1 + \frac{L - 4\text{ft}}{L} \times P_1 + \frac{L - 19\text{ft}}{L} \times P_2$	$M_{LL} = 197.629 \text{ ftk}$
	$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$	$M_{LL_I_Type3} = 128.7 \text{ ftk}$
		$V_{LL} = 20.741 \text{ k}$
		$V_{LL_I_Type3} = 13.507 \text{ k}$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb, overlay and channel equally distributed to all girders/stringers.

Steel:	$w_b = w_{\text{steel}} \times A_b$	$w_b = 67.45 \frac{\text{lb}}{\text{ft}}$
Wood deck:	$w_w = w_{\text{wood}} \times t_s \times S_b$	$w_w = 37.674 \frac{\text{lb}}{\text{ft}}$
Rail:	Total volume of rail on each side of roadway based on field measurements was found to be 6570 in ³ . The uniform load is distributed equally over the two exterior girders.	
	$w_r = w_{\text{steel}} \times \frac{6570\text{in}^3}{L \times 2}$	$w_r = 21.326 \frac{\text{lb}}{\text{ft}}$
Curb:	Total volume of wood-curb on each side of the roadway based on field measurements was found to be 44278 in ³ . The uniform load is distributed over the exterior girder.	

$$w_c = w_{\text{wood}} \times \frac{44278 \text{ in}^3}{L \times 2}$$

$$w_c = 14.669 \frac{\text{lb}}{\text{ft}}$$

$$\text{Overlay: } w_o = w_{\text{asphalt}} \times S_b + w_{\text{gravel}} \times 3 \text{ in} \times S_b$$

$$w_o = 76.854 \frac{\text{lb}}{\text{ft}}$$

$$\text{Channel: } w_{\text{ch}} = w_{\text{steel}} \times 6.47 \text{ in}^2 \times 4 \times \frac{S_b}{L}$$

$$w_{\text{ch}} = 4.557 \frac{\text{lb}}{\text{ft}}$$

Total Dead Load = sum w

$$DL = w_b + w_w + w_r + w_c + w_o + w_{\text{ch}}$$

$$DL = 0.223 \frac{\text{k}}{\text{ft}}$$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8}$$

$$M_{DL} = 53.048 \text{ ft-k}$$

$$V_{DL} = \frac{1}{2} \times DL \times L$$

$$V_{DL} = 4.859 \text{ k}$$

Capacities:

The capacities are the same as for the interior girders since the steel sections are the same.

$$M_n = 394.485 \text{ ft-k}$$

$$M_n = 4.734 \times 10^3 \text{ in} \times \text{k}$$

$$V_p = 147.844 \text{ k} \quad (10-115)$$

Rating:

$$\text{Inventory: } A_1 = 1.3$$

$$A_{2i} = 2.17$$

$$\text{Operating: } A_1 = 1.3$$

$$A_{2o} = 1.3$$

$$\text{Lane Flexure: Inventory: } RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL-I_Lane}}$$

$$RF = 1.32$$

$$\text{Operating: } RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL-I_Lane}}$$

$$RF = 2.203$$

$$\text{Shear: Inventory: } RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL-I_Lane}}$$

$$RF = 5.011$$

$$\text{Operating: } RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL-I_Lane}}$$

$$RF = 8.364$$

$$\text{HS-20 Flexure: Inventory: } RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL-I_HS20}}$$

$$RF = 0.895$$

$$\text{Operating: } RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL-I_HS20}}$$

$$RF = 1.493$$

$$\text{Shear: Inventory: } RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL-I_HS20}}$$

$$RF = 3.538$$

		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_HS20}}$	RF = 5.906
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.204
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_H20}}$	RF = 2.011
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 5.351
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_H20}}$	RF = 8.931
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.166
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_Type3}}$	RF = 1.946
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 4.829
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_Type3}}$	RF = 8.06

LOADS EXTRACTED FROM THE BDI-SOFTWARE

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 488.3 \text{ in} \times k$
			Live load	$M_{LL} = 1102 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 1.429 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_HS20} = 3.55 k$
			Live load	$V_{LL} = 8.49 k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 11.007 k$
H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 488.3 \text{ in} \times k$
			Live load	$M_{LL} = 801.8 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 1.039 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_H20} = 3.55 k$
			Live load	$V_{LL} = 5.4 k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 7.001 k$
Type-3	Flexure	Inventory	Dead load	$M_{DL_Type3} = 488.3 \text{ in} \times k$

		Live load	$M_{LL} = 832.4 \text{ in} \times \text{k}$
		$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 1.079 \times 10^3 \text{ in} \times \text{k}$
Shear	Inventory	Dead load	$V_{DL_Type3} = 3.55 \text{ k}$
		Live load	$V_{LL} = 6.15 \text{ k}$
		$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 7.973 \text{ k}$

BDI Ratings:

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.322
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 2.207
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 5.997
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 10.01
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.817
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 3.033
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 9.428
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 15.738
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.75
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 2.922
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 8.278
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 13.819

D.2. RATING FOR BRIDGE #2Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3}$	Weight of steel	
$w_{\text{wood}} = 50 \frac{\text{lb}}{\text{ft}^3}$	Weight of wood deck and curb	3.3.6
$w_{\text{gravel}} = 100 \frac{\text{lb}}{\text{ft}^3}$	Weight of gravel overlay on top of asphalt	3.3.6
$F_y = 30\text{ksi}$	Steel strength from Steel Construction Manual, 1930, p.18	

Interior GirderInput:

$A_{\text{tf}} = 8.5\text{in} \times 0.5\text{in}$	Area of top flange	$A_{\text{tf}} = 4.25 \text{ in}^2$
$A_w = 20\text{in} \times 0.5\text{in}$	Area of web	$A_w = 10 \text{ in}^2$
$A_{\text{bf}} = 8.5\text{in} \times 0.5\text{in}$	Area of bottom flange	$A_{\text{bf}} = 4.25 \text{ in}^2$
$t_{\text{tf}} = 0.5\text{in}$	Thickness of top flange	
$b_w = 20\text{in}$	Width of web	
$t_w = 0.5\text{in}$	Thickness of web	
$t_{\text{bf}} = 0.5\text{in}$	Thickness of bottom flange	

Section Properties:

$L = 37.83\text{ft}$	Design span of beam	
$t_s = 4\text{in}$	Thickness of wood deck	
$A_b = A_{\text{tf}} + A_w + A_{\text{bf}}$		$A_b = 18.5 \text{ in}^2$
$d = t_{\text{tf}} + b_w + t_{\text{bf}}$	Total depth of steel	$d = 21 \text{ in}$
$D = b_w$	Clear distance between flanges	$D = 20 \text{ in}$

Loads For Lane Loading:

$P_s = 26k$	Point Load for Shear for Lane Loading	fig. 3.7.6.b
$P_m = 18k$	Point Load for Moment for Lane Loading	
$\omega = 0.64 \frac{k}{\text{ft}}$	Uniform Load for Lane Loading	

Live Load Distribution Factor for Design Trucks:

$S_b = 2\text{ft} + 6.375\text{in}$	Average stringer spacing in ft	$S_b = 2.531 \text{ ft}$	table 3.23.1
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$$DF = \frac{S_b}{4.5\text{ft}}$$

$$DF = 0.563$$

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.3 \quad 3.8.2.1$$

Maximum Live Load Moments:

Lane Load $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear fig. 3.7.6.b

Uniform Load of 0.64 k/ft over the whole span
All values are lane loads; therefore divide loads by 2
so that the lane loads are compatible with truck loads

$$\text{Uniform load:} \quad M1_{\text{Lane}} = \frac{\omega \times L^2}{8} \quad M1_{\text{Lane}} = 114.489 \text{ ftk}$$

$$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L \quad V1_{\text{Lane}} = 12.106 \text{ k}$$

$$\text{Point Load:} \quad M2_{\text{Lane}} = \frac{P_m \times L}{4} \quad M2_{\text{Lane}} = 170.235 \text{ ftk}$$

$$V2_{\text{Lane}} = P_s \quad V2_{\text{Lane}} = 26 \text{ k}$$

$$M_{LL} = \frac{1}{2}(M1_{\text{Lane}} + M2_{\text{Lane}}) \quad M_{LL} = 142.362 \text{ ftk}$$

$$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF \quad M_{LL_I_Lane} = 104.102 \text{ ftk}$$

$$V_{LL} = \frac{1}{2}(V1_{\text{Lane}} + V2_{\text{Lane}}) \quad V_{LL} = 19.053 \text{ k}$$

$$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF \quad V_{LL_I_Lane} = 13.932 \text{ k}$$

HS-20 Max moment occur when middle axle is placed at 21.2 ft from the end. Max shear occur for rear axle at the end.

$$P_1 = 16\text{k}$$

$$P_2 = 4\text{k}$$

$$x = 21.2\text{ft}$$

$$x = 21.2\text{ft}$$

$$M_{LL} = \frac{36\text{k} \times (L - x) \times (x - 4.67\text{ft})}{L} - 56\text{ftk}$$

$$M_{LL} = 205.596 \text{ ftk}$$

$$M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_HS20} = 150.342 \text{ ftk}$$

$$V_{LL} = P_1 + \frac{L - 14\text{ft}}{L} \times P_1 + \frac{L - 28\text{ft}}{L} \times P_2$$

$$V_{LL} = 27.118 \text{ k}$$

$$V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_HS20} = 19.83 \text{ k}$$

H-20 Max moment occur when middle axle is placed at 20.3 ft from the end. Max shear occur for rear axle at the end.

$$P_1 = 16\text{k}$$

$$P_2 = 4\text{k}$$

$$x = 20.3\text{ft}$$

$$x = 20.3\text{ft}$$

	$M_{LL} = \frac{20k \times (L - x) \times (x - 2.8ft)}{L}$	$M_{LL} = 162.186 \text{ ftk}$
	$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$	$M_{LL_I_H20} = 118.599 \text{ ftk}$
	$V_{LL} = P_1 + \frac{L - 14ft}{L} \times P_2$	$V_{LL} = 18.52 \text{ k}$
	$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$	$V_{LL_I_H20} = 13.543 \text{ k}$
Type 3	Max moment occur when middle axle is 20.6 ft from the end. Max shear occur for rear axle at the end.	$P_1 = 8.5k$
	$x = 20.6ft$	$P_2 = 8k$
	$M_{LL} = 25k \times (x - 3.44ft) \times \frac{L - x}{L} - 34ftk$	$x = 20.6 \text{ ft}$
	$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$	$M_{LL} = 161.392 \text{ ftk}$
	$V_{LL} = P_1 + \frac{L - 4ft}{L} \times P_1 + \frac{L - 19ft}{L} \times P_2$	$M_{LL_I_Type3} = 118.018 \text{ ftk}$
	$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$	$V_{LL} = 20.083 \text{ k}$
		$V_{LL_I_Type3} = 14.686 \text{ k}$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb, overlay and channel equally distributed to all girders/stringers.

Steel:	$w_b = w_{\text{steel}} \times A_b$	$w_b = 62.937 \frac{\text{lb}}{\text{ft}}$
Wood deck:	$w_w = w_{\text{wood}} \times t_s \times S_b$	$w_w = 42.187 \frac{\text{lb}}{\text{ft}}$
Rail:	Total volume of rail on both sides of roadway based on field measurements was found to be 6701 in ³ . The uniform load is distributed equally over the eight girders.	
	$w_r = w_{\text{steel}} \times \frac{6701 \text{ in}^3}{L \times 8}$	$w_r = 6.277 \frac{\text{lb}}{\text{ft}}$
Curb:	Total volume of wood-curb on both sides of the roadway based on field measurements was found to be 81720 in ³ . The uniform load is distributed equally over the eight girders.	
	$w_c = w_{\text{wood}} \times \frac{81720 \text{ in}^3}{L \times 8}$	$w_c = 7.813 \frac{\text{lb}}{\text{ft}}$
Overlay:	$w_o = w_{\text{gravel}} \times 3 \text{ in} \times S_b$	$w_o = 63.281 \frac{\text{lb}}{\text{ft}}$
Channel:	$w_{ch} = w_{\text{steel}} \times 6.47 \text{ in}^2 \times 4 \times \frac{S_b}{L}$	$w_{ch} = 5.891 \frac{\text{lb}}{\text{ft}}$
Total Dead Load = sum w		
$DL = w_b + w_w + w_r + w_c + w_o + w_{ch}$		$DL = 0.188 \frac{\text{k}}{\text{ft}}$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8}$$

$$M_{DL} = 33.7 \text{ ft-k}$$

$$V_{DL} = \frac{1}{2} \times DL \times L$$

$$V_{DL} = 3.563 \text{ k}$$

Capacities:

$$C = A_b \times F_y$$

$$C = 555 \text{ k} \quad (10-124)$$

$$AF_{tf} = A_{tf} \times F_y$$

Top flange

$$AF_{tf} = 127.5 \text{ k}$$

$$AF_w = A_w \times F_y$$

Web above welded plate

$$AF_w = 300 \text{ k}$$

$$AF_{bf} = AF_{tf}$$

Bottom flange

$$AF_{bf} = 127.5 \text{ k}$$

$$y = t_{bf} + \frac{b_w}{2}$$

Distance from bottom of steel to NA

$$y = 10.5 \text{ in}$$

$$D_{cp} = \frac{b_w}{2}$$

Depth of web in compression at NA

$$D_{cp} = 10 \text{ in}$$

Check compact:

$$b = \frac{8.5 \text{ in} - 0.5 \text{ in}}{2}$$

Width of projecting flange element

$$b = 4 \text{ in}$$

$$\frac{b}{t_w} \leq \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$\frac{b}{t_w} = 8$$

$$\frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 11.865$$

$$\text{OK!} \quad (10-93)$$

$$\frac{D}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$\frac{D}{t_w} = 40$$

$$\frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 111.024$$

$$\text{OK!} \quad (10-93)$$

Since not both of the two criteria above exceed 75% of limit => don't check (10-95)

$$M_n = F_y \times Z$$

$$(10-92)$$

$$y = 10.5 \text{ in}$$

Distance from bottom of steel to PNA

$$y = 10.5 \text{ in}$$

$$y_{bf} = y - \frac{0.5 \text{ in}}{2}$$

Distance from PNA to C.G bottom flange

$$y_{bf} = 10.25 \text{ in}$$

$$y_w = \frac{1}{2} \times \frac{D}{2}$$

Distance from NA to C.G web above NA

$$y_w = 5 \text{ in}$$

$$A_{tf} = 4.25 \text{ in}^2$$

Area of top flange

$$A_{tf} = 4.25 \text{ in}^2$$

$$A_w = 10 \text{ in}^2$$

Area of the whole web both above and below PNA

$$A_w = 10 \text{ in}^2$$

$$Z = 2 \times y_{bf} \times A_{tf} + 2 \times y_w \times \frac{A_w}{2}$$

Plastic section modulus

$$Z = 137.125 \text{ in}^3$$

$$M_n = F_y \times Z$$

$$M_n = 342.813 \text{ ft-k}$$

$$M_n = 4.114 \times 10^3 \text{ in} \times k$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$K = 5$$

For unstiffened beams and girders

$$D = 20 \text{ in}$$

Clear distance between flanges

$$t_w = 0.5 \text{ in}$$

Web thickness

$$\frac{D}{t_w} = 40$$

$$\frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 77.46$$

 \Rightarrow

$$C = 1.0$$

(10-116)

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 174 \text{ k}$$

(10-115)

$$V_n = C \times V_p$$

$$V_n = 174 \text{ k}$$

(10-113)

Rating:

$$\text{Inventory:} \quad A_1 = 1.3 \quad A_{2i} = 2.17$$

$$\text{Operating:} \quad A_1 = 1.3 \quad A_{2o} = 1.3$$

$$\text{Lane} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}} \quad RF = 1.324$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}} \quad RF = 2.209$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}} \quad RF = 5.602$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}} \quad RF = 9.351$$

$$\text{HS-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}} \quad RF = 0.917$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}} \quad RF = 1.53$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}} \quad RF = 3.936$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}} \quad RF = 6.57$$

$$\text{H-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}} \quad RF = 1.162$$

Type-3	Flexure:	Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_H20}}$	RF = 1.939
		Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 5.763
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_H20}}$	RF = 9.62
		Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.168
	Shear:	Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_Type3}}$	RF = 1.949
		Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 5.315
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_Type3}}$	RF = 8.871
		Inventory:		

LOADS EXTRACTED FROM THE BDI-SOFTWARE

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 326.1 \text{ in} \times k$
			Live load	$M_{LL} = 1001 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 1.301 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_HS20} = 2.99k$
			Live load	$V_{LL} = 12.63k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 16.419 k$
H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 336.3 \text{ in} \times k$
			Live load	$M_{LL} = 824.6 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 1.072 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_H20} = 2.99k$
			Live load	$V_{LL} = 9.91k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 12.883 k$
Type-3	Flexure	Inventory	Dead load	$M_{DL_Type3} = 336.3 \text{ in} \times k$
			Live load	$M_{LL} = 746.2 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 970.06 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_Type3} = 2.99k$
			Live load	$V_{LL} = 9.10k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 11.83 k$

BDI Ratings:

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.307
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 2.181
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 4.775
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 7.97
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.581
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 2.638
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 6.085
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 10.157
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.747
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 2.915
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 6.627
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 11.061

Exterior GirderLive Load Distribution Factor:

overhang = 12in

Overhang of wood deck

$$S_b = \frac{S_b}{2} + \text{overhang}$$

Average stringer spacing in ft

$$S_b = 2.266 \text{ ft}$$

table 3.23.1

$$DF_1 = \frac{S_b}{4.5 \text{ ft}}$$

$$DF_1 = 0.503$$

3.23.2.3.1.5

Find new DF for treating the exterior stringer as a simple beam

3.23.2.3.1.2

$$DF_2 = \frac{2 \text{ ft} + 6.375 \text{ in} - 2 \text{ ft}}{2 \text{ ft} + 6.375 \text{ in}}$$

$$DF_2 = 0.21$$

Use maximum distribution factor

$$DF = \max \left(\left(\frac{DF_1}{DF_2} \right) \right)$$

$$DF = 0.503$$

Maximum Live Load Moments:

Lane Load	<p>$P_m=18k$ for moment, $P_s=26k$ for shear</p> <p>Uniform Load of 0.64 k/ft over the whole span</p> <p>All values are lane loads, therefore divide lane loads by 2 so that lane loads are compatible with truck loads</p>	fig. 3.7.6.b
Uniform load:	$M1_{Lane} = \frac{\omega \times L^2}{8}$ $V1_{Lane} = \frac{1}{2} \times \omega \times L$	$M1_{Lane} = 114.489 \text{ ftk}$ $V1_{Lane} = 12.106 \text{ k}$
Point Load:	$M2_{Lane} = \frac{P_m \times L}{4}$ $V2_{Lane} = P_s$	$M2_{Lane} = 170.235 \text{ ftk}$ $V2_{Lane} = 26 \text{ k}$
	$M_{LL} = \frac{1}{2} (M1_{Lane} + M2_{Lane})$	$M_{LL} = 142.362 \text{ ftk}$
	$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF$	$M_{LL_I_Lane} = 93.178 \text{ ftk}$
	$V_{LL} = \frac{1}{2} (V1_{Lane} + V2_{Lane})$	$V_{LL} = 19.053 \text{ k}$
	$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF$	$V_{LL_I_Lane} = 12.47 \text{ k}$
HS-20	<p>Max moment occur when middle axle is placed 21.2 ft from midspan. Max shear occur for rear axle at one end.</p> <p>$x = 21.2 \text{ ft}$</p> $M_{LL} = \frac{36k \times (L - x) \times (x - 4.67 \text{ ft})}{L} - 56 \text{ ftk}$ $M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$ $V_{LL} = P_1 + \frac{L - 14 \text{ ft}}{L} \times P_1 + \frac{L - 28 \text{ ft}}{L} \times P_2$ $V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$	<p>$P_1 = 16k$</p> <p>$P_2 = 8k$</p> <p>$x = 21.2 \text{ ft}$</p> <p>$M_{LL} = 205.596 \text{ ftk}$</p> <p>$M_{LL_I_HS20} = 134.566 \text{ ftk}$</p> <p>$V_{LL} = 28.158 \text{ k}$</p> <p>$V_{LL_I_HS20} = 18.43 \text{ k}$</p>
H-20	<p>Max moment occur when middle axle is placed 20.3 ft from midspan. Max shear occur for rear axle at one end.</p> <p>$x = 20.3 \text{ ft}$</p> $M_{LL} = \frac{20k \times (L - x) \times (x - 2.8 \text{ ft})}{L}$ $M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$	<p>$P_1 = 16k$</p> <p>$P_2 = 4k$</p> <p>$x = 20.3 \text{ ft}$</p> <p>$M_{LL} = 162.186 \text{ ftk}$</p> <p>$M_{LL_I_H20} = 106.153 \text{ ftk}$</p>

$$V_{LL} = P_1 + \frac{L - 14\text{ft}}{L} \times P_2$$

$$V_{LL} = 18.52 \text{ k}$$

$$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_H20} = 12.121 \text{ k}$$

Type 3 Max moment occur when middle axle is placed 20.6 ft from midspan. Max shear occur for rear axle at the end.

$$P_1 = 8.5 \text{ k}$$

$$P_2 = 8 \text{ k}$$

$$x = 20.6 \text{ ft}$$

$$x = 20.6 \text{ ft}$$

$$M_{LL} = 25 \text{ k} \times (x - 3.44 \text{ ft}) \times \frac{L - x}{L} - 34 \text{ ft k}$$

$$M_{LL} = 161.392 \text{ ft k}$$

$$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_Type3} = 105.633 \text{ ft k}$$

$$V_{LL} = P_1 + \frac{L - 4\text{ft}}{L} \times P_1 + \frac{L - 4\text{ft} - 15\text{ft}}{L} \times P_2$$

$$V_{LL} = 20.083 \text{ k}$$

$$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_Type3} = 13.145 \text{ k}$$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb, overlay and channel equally distributed to all girders/stringers.

Steel: $w_b = w_{\text{steel}} \times A_b$

$$w_b = 62.937 \frac{\text{lb}}{\text{ft}}$$

Wood deck: $w_w = w_{\text{wood}} \times t_s \times S_b$

$$w_w = 37.76 \frac{\text{lb}}{\text{ft}}$$

Rail: Total volume of rail on each side of roadway based on field measurements was found to be 6701 in³. The uniform load is distributed equally over the two exterior girders.

$$w_r = w_{\text{steel}} \times \frac{6570 \text{ in}^3}{L \times 2}$$

$$w_r = 24.618 \frac{\text{lb}}{\text{ft}}$$

Curb: Total volume of wood-curb on each side of the roadway based on field measurements was found to be 81720 in³. The uniform load is distributed over the exterior girder.

$$w_c = w_{\text{wood}} \times \frac{81720 \text{ in}^3}{L \times 2}$$

$$w_c = 31.253 \frac{\text{lb}}{\text{ft}}$$

Overlay: $w_o = w_{\text{gravel}} \times 3 \text{ in} \times S_b$

$$w_o = 56.641 \frac{\text{lb}}{\text{ft}}$$

Channel: $w_{ch} = w_{\text{steel}} \times 6.47 \text{ in}^2 \times 4 \times \frac{S_b}{L}$

$$w_{ch} = 5.273 \frac{\text{lb}}{\text{ft}}$$

Total Dead Load = sum w

$$DL = w_b + w_w + w_r + w_c + w_o + w_{ch}$$

$$DL = 0.218 \frac{\text{k}}{\text{ft}}$$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8}$$

$$M_{DL} = 39.084 \text{ ft k}$$

$$V_{DL} = \frac{1}{2} \times DL \times L$$

$$V_{DL} = 4.133 \text{ k}$$

Capacities:

The capacities are the same as for the interior girders since the steel sections are the same.

$$M_n = 342.813 \text{ ft-k}$$

$$M_n = 4.114 \times 10^3 \text{ in} \times \text{k}$$

$$V_p = 174 \text{ k} \quad (10-115)$$

Rating:

$$\text{Inventory:} \quad A_1 = 1.3 \quad A_{2i} = 2.17$$

$$\text{Operating:} \quad A_1 = 1.3 \quad A_{2o} = 1.3$$

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 1.444
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 2.411
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 6.231
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 10.402
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 1.669
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 4.217
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 7.038
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.268
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 2.116
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 6.411
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 10.701

Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.274
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 2.126
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 5.912
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 9.868

LOADS EXTRACTED FROM THE BDI-SOFTWARE

HS-20	Flexure	Inventory	Dead load per inch-strip	$M_{DL_HS20} = 326 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 850.7 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 1.106 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_HS20} = 2.92k$
			Live load per inch-strip	$V_{LL} = 7.93k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 10.309k$
H-20	Flexure	Inventory	Dead load per inch-strip	$M_{DL_H20} = 336.1 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 661 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 859.3 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_H20} = 2.92k$
			Live load per inch-strip	$V_{LL} = 5.22k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 6.786k$
Type-3	Flexure	Inventory	Dead load per inch-strip	$M_{DL_Type3} = 336.1 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 653.6 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 849.68 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_Type3} = 2.92k$
			Live load per inch-strip	$V_{LL} = 5.82k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 7.566k$

BDI Ratings:

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.538
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 2.567

	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 7.608
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 12.7
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.972
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 3.291
H-20	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 11.558
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 19.294
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.994
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 3.329
Type-3	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 10.367
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 17.305

D.3. RATING FOR BRIDGE #3

RATING FOR MAIN GIRDER

Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of concrete}$$

$$f_c = 3\text{ksi} \quad \text{Concrete strength}$$

$$F_y = 33\text{ksi} \quad \text{Steel strength}$$

Input:

$$A_{tf} = 15.66\text{in} \times 1.378\text{in} \quad \text{Area of top flange} \quad A_{tf} = 21.579 \text{in}^2$$

$$A_{wl} = 6.31\text{in} \times 0.84\text{in} \quad \text{Area of top of web above welded plate} \quad A_{wl} = 5.3 \text{in}^2$$

$$A_p = 26\text{in} \times 0.875\text{in} \quad \text{Area of welded plate} \quad A_p = 22.75 \text{in}^2$$

$A_{w2} = 6.31 \text{ in} \times 0.84 \text{ in}$	Area of bottom of web below welded plate	$A_{w2} = 5.3 \text{ in}^2$
$A_{c1} = 14 \text{ in} \times 1 \text{ in}$	Area of first cover plate	$A_{c1} = 14 \text{ in}^2$
$A_{c2} = 12 \text{ in} \times 0.625 \text{ in}$	Area of second cover plate	$A_{c2} = 7.5 \text{ in}^2$
$A_{ha} = 2 \times 8 \text{ in} \times 1 \text{ in}$	Area of horizontal part of angle	$A_{ha} = 16 \text{ in}^2$
$A_{va} = 2 \times 1 \text{ in} \times 3 \text{ in}$	Area of vertical part of angles	$A_{va} = 6 \text{ in}^2$
$t_{tf} = 1.378 \text{ in}$	Thickness of top flange	
$b_{w1} = 6.31 \text{ in}$	Width of web above welded plate	
$b_p = 26 \text{ in}$	Width of welded plate	
$b_{w2} = 6.31 \text{ in}$	Width of web below welded plate	
$t_{bf} = 1.378 \text{ in}$	Thickness of bottom flange	
$t_{c1} = 1 \text{ in}$	Thickness of first cover	
$t_{c2} = 0.625 \text{ in}$	Thickness of second cover	

Loads for Lane Loading

$P_s = 26 \text{ k}$	Point Load for Shear for Lane Loading	fig. 3.7.6.b
$P_m = 18 \text{ k}$	Point Load for Moment for Lane Loading	
$\omega = 0.64 \frac{\text{k}}{\text{ft}}$	Uniform Load for Lane Loading	

Girder second cover

Live Load Distribution Factor for Design Trucks per wheel line:

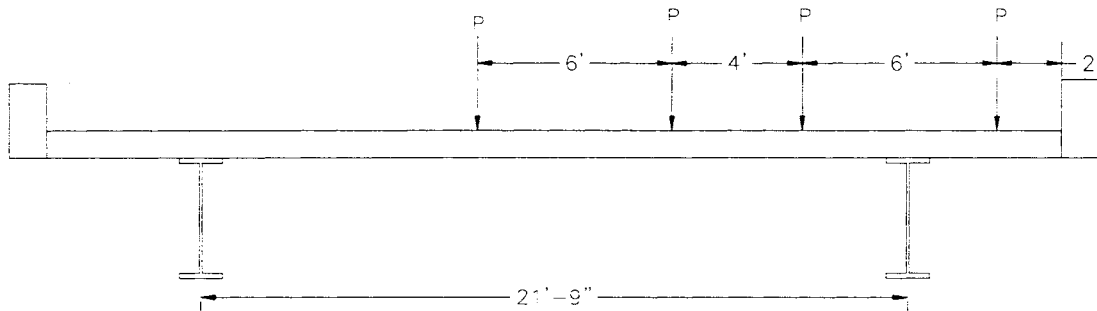


Figure D.1. Live Load Distribution Factor for girder.

$$DF = \frac{94.5 + (94.5 + 72) + (94.5 + 72 + 48) + (94.5 + 72 + 48 + 72)}{261} \quad DF = 2.92$$

Distribution factor for Lane Load per lane:

Since roadway width is 30 ft and the distance between the girders is 21.75 ft, two lane design lanes are distributed such that one lane is adjacent to the curb. 3.6.2
3.6.3

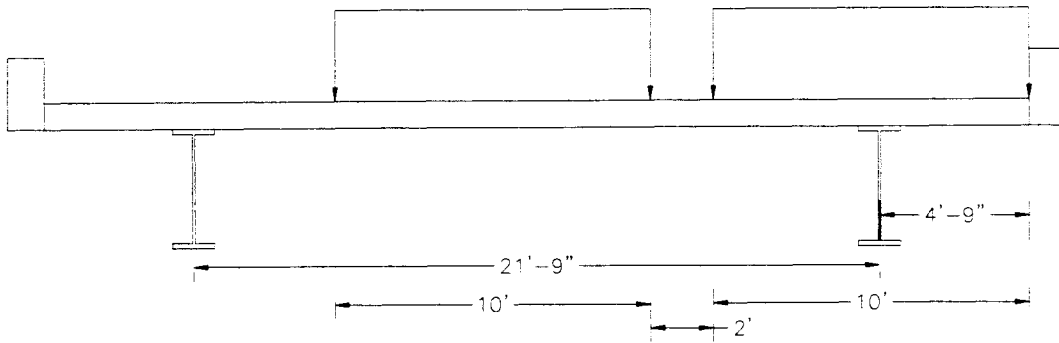


Figure D.2. Distribution factor for Lane Load.

$$DF_{\text{Lane}} = \frac{21.5\text{ft} + 9.5\text{ft}}{21.75\text{ft}}$$

$$DF_{\text{Lane}} = 1.425$$

Section Properties:

$$I_0 = 82797\text{in}^4 \quad \text{Moment of inertia for elastic section (from Excel)}$$

$$Ecc = 18.56\text{in} \quad \text{Distance from c.g. slab to c.g elastic composit section (from Excel)}$$

$$L = 70\text{ft} \quad \text{Span of beam}$$

$$t_s = 8\text{in} \quad \text{Thickness of concrete slab}$$

$$A_b = A_{tf} + A_{w1} + A_p + A_{w2} + A_{ha} + A_{va} + A_{tf} + A_{c1} + A_{c2} \quad A_b = 120.01\text{in}^2$$

$$d = t_{tf} + b_{w1} + b_p + b_{w2} + t_{bf} + t_{c1} + t_{c2} \quad \text{Total depth of steel} \quad d = 43.001\text{in}$$

$$D = b_{w1} + b_p + b_{w2} \quad \text{Clear distance between flanges} \quad D = 38.62\text{in}$$

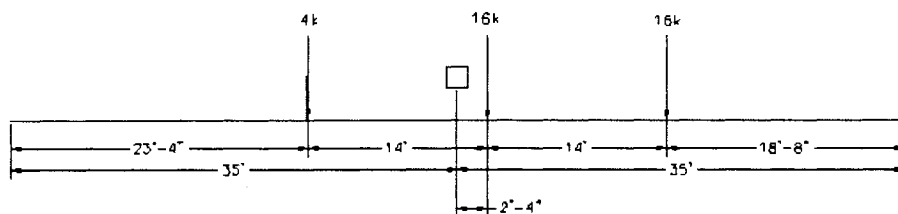


Figure D.3. Location of HS-20 truck for maximum moment.

$$CG = \frac{4k \times (-14\text{ft}) + 16k \times 0\text{ft} + 16k \times 14\text{ft}}{4k + 16k + 16k}$$

$$CG = 4.667\text{ft}$$

$$CG_{\text{shift}} = \frac{CG}{2}$$

$$CG_{\text{shift}} = 2.333\text{ft}$$

CG is center of gravity of truck when the center wheel load (16 k/wheel line) is placed at midspan.
CG_{shift} is the shift in truck position to obtain maximum live load moment.

$x_m = 35\text{ft} + (2\text{ft} + 4\text{in})$ Distance from edge of beam to calculate maximum live load moment

$$x_m = 37.333\text{ ft}$$

$x_s = 48.5\text{ft}$ Distance from edge of beam to calculate maximum live load shear

$$x_s = 48.5\text{ ft}$$

$$b_{\text{eff}} = \min \left(\left(\frac{1}{4} \times L \right), \left(21.75\text{ft} \right), \left(12 \times t_s \right) \right)$$

$$b_{\text{eff}} = 96\text{ in} \quad 10.38.3.1$$

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.256 \quad 3.8.2.1$$

Maximum Live Load Moments:

$$\text{Moment:} \quad \frac{L - x_m}{L} = 0.467 \quad \text{Shear:} \quad \frac{L - x_s}{L} = 0.307 \quad [3] \text{ p.84-87}$$

Lane $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear
Uniform Load of 0.64 k/ft over the whole span

fig. 3.7.6.b

$$\text{Uniform load:} \quad M1_{\text{Lane}} = \frac{\omega \times L^2}{8}$$

$$M1_{\text{Lane}} = 392\text{ ftk}$$

$$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L \times \left(2 \times \frac{x_s}{L} - 1 \right)$$

$$V1_{\text{Lane}} = 8.64\text{ k}$$

$$\text{Point Load:} \quad M2_{\text{Lane}} = \frac{P_m \times L}{4}$$

$$M2_{\text{Lane}} = 315\text{ ftk}$$

$$V2_{\text{Lane}} = P_s \times \frac{x_s}{L}$$

$$V2_{\text{Lane}} = 18.014\text{ k}$$

All values are lane loads.

$$M_{LL} = M1_{\text{Lane}} + M2_{\text{Lane}}$$

$$M_{LL} = 707\text{ ftk}$$

$$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF_{\text{Lane}}$$

$$M_{LL_I_Lane} = 1.266 \times 10^3\text{ ftk}$$

$$V_{LL} = V1_{\text{Lane}} + V2_{\text{Lane}}$$

$$V_{LL} = 26.654\text{ k}$$

$$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF_{\text{Lane}}$$

$$V_{LL_I_Lane} = 47.731\text{ k}$$

$$\text{HS-20} \quad M_{\text{HS20}} = \frac{36\text{k} \times (L - x_m) \times (x_m - 4.67\text{ft})}{L} - 56\text{ftk}$$

$$M_{\text{HS20}} = 492.744\text{ ftk}$$

$$M_{LL_I_HS20} = M_{\text{HS20}} \times (1 + I) \times DF$$

$$M_{LL_I_HS20} = 1.807 \times 10^3\text{ ftk}$$

$$V_{\text{HS20}} = \frac{36\text{k} \times (x_s - 9.33\text{ft})}{L}$$

$$V_{\text{HS20}} = 20.145\text{ k}$$

$$V_{LL_I_HS20} = V_{\text{HS20}} \times (1 + I) \times DF$$

$$V_{LL_I_HS20} = 73.893\text{ k}$$

$$\text{H-20} \quad M_{\text{H20}} = \frac{20\text{k} \times (L - x_m) \times (x_m - 2.8\text{ft})}{L}$$

$$M_{\text{H20}} = 322.311\text{ ftk}$$

$$M_{LL_I_H20} = M_{H20} \times (1 + I) \times DF$$

$$M_{LL_I_H20} = 1.182 \times 10^3 \text{ ftk}$$

$$V_{H20} = \frac{20k \times (x_s - 2.8\text{ft})}{L}$$

$$V_{H20} = 13.057 \text{ k}$$

$$V_{LL_I_H20} = V_{H20} \times (1 + I) \times DF$$

$$V_{LL_I_H20} = 47.895 \text{ k}$$

$$\text{Type 3 } M_{\text{Type3}} = (25k) \times (x_m - 3.44\text{ft}) \times \frac{L - x_m}{L} - 34\text{ftk}$$

$$M_{\text{Type3}} = 361.422 \text{ ftk}$$

$$M_{LL_I_Type3} = M_{\text{Type3}} \times (1 + I) \times DF$$

$$M_{LL_I_Type3} = 1.326 \times 10^3 \text{ ftk}$$

$$V_{\text{Type3}} = \frac{25k \times (x_s - 7.44\text{ft})}{L}$$

$$V_{\text{Type3}} = 14.664 \text{ k}$$

$$V_{LL_I_Type3} = V_{\text{Type3}} \times (1 + I) \times DF$$

$$V_{LL_I_Type3} = 53.791 \text{ k}$$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb and parapet equally distributed to all girders/stringers.

$$\text{Steel: } w_b = w_{\text{steel}} \times A_b$$

$$w_b = 0.408 \frac{\text{k}}{\text{ft}}$$

$$\text{Stringers: } w_{st} = w_{\text{steel}} 12.49\text{in}^2 \times \frac{4}{2}$$

$$w_{st} = 0.085 \frac{\text{k}}{\text{ft}}$$

$$\text{Floorbeams: } w_f = w_{\text{steel}} \times \frac{29.18\text{in}^2 + 32.92\text{in}^2}{2} \times \frac{21.75\text{ft}}{2} \times \frac{4}{70\text{ft}}$$

$$w_f = 0.066 \frac{\text{k}}{\text{ft}}$$

$$\text{Slab: } w_s = w_{\text{concrete}} \times t_s \times \left[\frac{21.75\text{ft}}{2} + (4\text{ft} + 7.5\text{in}) \right]$$

$$w_s = 1.55 \frac{\text{k}}{\text{ft}}$$

$$\text{Curb: } w_c = w_{\text{concrete}} \times 10\text{in} \times 23\text{in}$$

$$w_c = 0.24 \frac{\text{k}}{\text{ft}}$$

$$\text{Parapet: } w_p = w_{\text{concrete}} \times 27\text{in} \times 5\text{in}$$

$$w_p = 0.141 \frac{\text{k}}{\text{ft}}$$

$$\text{Overlay: } w_o = w_{\text{concrete}} \times \frac{30\text{ft}}{2} \times 1.89\text{in}$$

$$w_o = 0.354 \frac{\text{k}}{\text{ft}}$$

Total Dead Load = sum w + add 5%

$$DL = (w_b + w_{st} + w_f + w_s + w_c + w_p + w_o) \times 1.05$$

$$DL = 2.986 \frac{\text{k}}{\text{ft}}$$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8}$$

$$M_{DL} = 1.829 \times 10^3 \text{ ftk}$$

$$V_{DL} = \frac{1}{2} \times DL \times L \times \left(2 \times \frac{x_s}{L} - 1 \right)$$

$$V_{DL} = 40.306 \text{ k}$$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s$$

$$C_1 = 1.958 \times 10^3 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y$$

$$C_2 = 3.96 \times 10^3 \text{ k} \quad (10-124)$$

$$C = \min \left(\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} \right)$$

Compressive force in slab

$$C = 1.958 \times 10^3 \text{ k}$$

$$a = \frac{C}{0.85 \times f_c \times b_{\text{eff}}}$$

Depth of concrete stressblock

$$a = 8 \text{ in} \quad (10-125)$$

Since Eq. (10-123) controls \Rightarrow steel has compression

$$C_{prime} = \frac{C_2 - C}{2}$$

Compressive force in steel

$$C_{prime} = 1.001 \times 10^3 \text{ k}$$

$$AF_{tf} = A_{tf} \times F_y$$

top flange

$$AF_{tf} = 712.123 \text{ k}$$

$$AF_{w1} = A_{w1} \times F_y$$

web above welded plate

$$AF_{w1} = 174.913 \text{ k}$$

$$AF_p = A_p \times F_y$$

welded plate

$$AF_p = 750.75 \text{ k}$$

$$AF_{w2} = AF_{w1}$$

web below welded plate

$$AF_{w2} = 174.913 \text{ k}$$

$$AF_{ha} = A_{ha} \times F_y$$

horizontal part of angle

$$AF_{ha} = 528 \text{ k}$$

$$AF_{va} = A_{va} \times F_y$$

vertical part of angle

$$AF_{va} = 198 \text{ k}$$

$$AF_{bf} = AF_{tf}$$

bottom flange

$$AF_{bf} = 712.123 \text{ k}$$

$$AF_{c1} = A_{c1} \times F_y$$

first cover

$$AF_{c1} = 462 \text{ k}$$

$$AF_{c2} = A_{c2} \times F_y$$

second cover

$$AF_{c2} = 247.5 \text{ k}$$

Since $C_{prime} > AF_{tf} + AF_{w1} \Rightarrow$
y lies in welded plate section

$$t_{tf} = 1.378 \text{ in}$$

Thickness of top flange

$$b_{w1} = 6.31 \text{ in}$$

Width of web above welded plate

$$b_p = 26 \text{ in}$$

Depth of welded plate

$$y = t_{tf} + b_{w1} + \frac{C_{prime} - (AF_{tf} + AF_{w1})}{AF_p} \times b_p$$

$$y = 11.633 \text{ in}$$

y is distance from bottom of
slab down to plastic NA.

Check compact:

$$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

(10-129)

$$D_{cp} = y - t_{tf}$$

Depth of web in compression at
the plastic moment

$$D_{cp} = 10.255 \text{ in}$$

$$t_w = 0.84 \text{ in}$$

Thickness of web

$$\frac{2 \times D_{cp}}{t_w} = 24.418$$

$$\frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 105.858$$

OK!

Check (10-129a):

$$\frac{D_p}{D_{prime}} \leq 5$$

(10-129a)

$$D_p = y + t_s$$

Distance from top of slab to PNA

$$D_p = 19.633 \text{ in}$$

$$D_{prime} = 0.9 \times \frac{d + t_s}{7.5}$$

$$D_{prime} = 6.12 \text{ in}$$

$$\frac{D_p}{D_{prime}} = 3.208$$

OK!

$$\text{Since } D_{prime} < D_p < 5D_{prime} \Rightarrow$$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad (10-129c)$$

Slab:	$C = 1.958 \times 10^3 \text{ k}$	$d_c = \left \frac{t_s}{2} + y \right $	$d_c = 15.633 \text{ in}$
Top flange:	$AF_{tf} = 712.123 \text{ k}$	$d_{tf} = \left y - \frac{t_{tf}}{2} \right $	$d_{tf} = 10.944 \text{ in}$
Web above welded plate:	$AF_{w1} = 174.913 \text{ k}$	$d_{w1} = \left y - t_{tf} - \frac{b_{w1}}{2} \right $	$d_{w1} = 7.1 \text{ in}$
Welded plate:	$AF_p = 750.75 \text{ k}$	$d_p = \left y - t_{tf} - b_{w1} - \frac{b_p}{2} \right $	$d_p = 9.055 \text{ in}$
Web below welded plate:	$AF_{w2} = 174.913 \text{ k}$	$d_{w2} = \left y - t_{tf} - b_{w1} - b_p - \frac{b_{w1}}{2} \right $	$d_{w2} = 25.21 \text{ in}$
Horizontal part of angle:	$AF_{ha} = 528 \text{ k}$	$d_{ha} = \left d - y - 2.125 \text{ in} - \frac{1 \text{ in}}{2} \right $	$d_{ha} = 28.743 \text{ in}$
Vertical part of angle:	$AF_{va} = 198 \text{ k}$	$d_{va} = \left d - y - 3.125 \text{ in} - \frac{3 \text{ in}}{2} \right $	$d_{va} = 26.743 \text{ in}$
Bottom flange:	$AF_{bf} = 712.123 \text{ k}$	$d_{bf} = \left d - y - t_{c2} - t_{c1} - \frac{t_{tf}}{2} \right $	$d_{bf} = 29.054 \text{ in}$
First cover:	$AF_{c1} = 462 \text{ k}$	$d_{c1} = \left d - y - t_{c2} - \frac{t_{c1}}{2} \right $	$d_{c1} = 30.243 \text{ in}$
Second cover:	$AF_{c2} = 247.5 \text{ k}$	$d_{c2} = \left d - y - \frac{t_{c2}}{2} \right $	$d_{c2} = 31.055 \text{ in}$

$$M_{p1} = C \times d_c + AF_{tf} \times d_{tf} + AF_{w1} \times d_{w1} + AF_p \times d_p + AF_{w2} \times d_{w2} + AF_{bf} \times d_{bf}$$

$$M_{p2} = AF_{ha} \times d_{ha} + AF_{va} \times d_{va} + AF_{c1} \times d_{c1} + AF_{c2} \times d_{c2}$$

$$M_p = M_{p1} + M_{p2} \quad M_p = 9.473 \times 10^3 \text{ ft-k}$$

Yield moment:

$$I_g = 8.28 \times 10^4 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - Ecc \quad \text{Distance from bottom of steel to elastic NA} \quad Y = 28.441 \text{ in}$$

$$M_y = F_y \times \frac{I_g}{Y} \quad M_y = 8.006 \times 10^3 \text{ ft-k}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad M_n = 8 \times 10^3 \text{ ft-k}$$

$$M_n = 9.6 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

K = 5 For unstiffened beams and girders

D = 38.62 in Clear distance between flanges

 $t_w = 0.84$ in Web thickness

$$\frac{D}{t_w} = 45.976 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 620.917 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 620.917 \text{ k} \quad (10-113)$$

Rating:Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$ Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 2.047
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 3.416

	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 5.489
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 9.162

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.434
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 2.393

	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 3.546
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 5.918

H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.192
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	

		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 3.658
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 5.47
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 9.131
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.955
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 3.263
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 4.871
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 8.13

Girder first cover

Section Properties:

$A_{c2} = 0 \text{ in}^2$	Remove area for second cover	
$t_{c2} = 0 \text{ in}$	Remove second cover	
$I_g = 76633 \text{ in}^4$	Moment of inertia for elastic section (from Excel)	
$Ecc = 17.49 \text{ in}$	Distance from c.g. slab to c.g elastic composit section (from Excel)	
$L = 70 \text{ ft}$	Span of beam	
$t_s = 8 \text{ in}$	Thickness of concrete slab	
$DF = 2.92$	Distribution factor for a wheel line	
$x_m = 48.5 \text{ ft}$	Distance from edge of beam to calculate maximum live load moment	
$x_s = 57.5 \text{ ft}$	Distance from edge of beam to calculate maximum live load shear	
$A_b = A_{tf} + A_{w1} + A_p + A_{w2} + A_{ha} + A_{va} + A_{tf} + A_{c1} + A_{c2}$		$A_b = 112.51 \text{ in}^2$
$d = t_{tf} + b_{w1} + b_p + b_{w2} + t_{bf} + t_{c1} + t_{c2}$		$d = 42.376 \text{ in}$
	d is total depth of steel	
$D = b_{w1} + b_p + b_{w2}$		$D = 38.62 \text{ in}$
	D is clear distance between flanges	

$$b_{eff} = \min \left(\left(\frac{1}{4} \times L \right), \left(21.75 \text{ ft} \right), \left(12 \times t_s \right) \right) \quad b_{eff} = 96 \text{ in} \quad 10.38.3.1$$

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.256 \quad 3.8.2.1$$

Maximum Live Load Moments:

$$\text{Moment:} \quad \frac{L - x_m}{L} = 0.307 \quad \text{Shear:} \quad \frac{L - x_s}{L} = 0.179 \quad [3] \text{ p.84-87}$$

Lane $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear
Uniform Load of 0.64 k/ft over the whole span fig. 3.7.6.b

$$\text{Uniform load:} \quad M1_{\text{Lane}} = \frac{1}{2} \times \omega \times L \times \left(x_m - \frac{x_m^2}{L} \right) \quad M1_{\text{Lane}} = 333.68 \text{ ftk}$$

$$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L \times \left(2 \times \frac{x_s}{L} - 1 \right) \quad V1_{\text{Lane}} = 14.4 \text{ k}$$

$$\text{Point Load:} \quad M2_{\text{Lane}} = \frac{L - x_m}{L} \times P_m \times x_m \quad M2_{\text{Lane}} = 268.136 \text{ ftk}$$

$$V2_{\text{Lane}} = P_s \times \frac{x_s}{L} \quad V2_{\text{Lane}} = 21.357 \text{ k}$$

All values are lane loads

$$M_{LL} = M1_{\text{Lane}} + M2_{\text{Lane}} \quad M_{LL} = 601.816 \text{ ftk}$$

$$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF_{\text{Lane}} \quad M_{LL_I_Lane} = 1.078 \times 10^3 \text{ ftk}$$

$$V_{LL} = V1_{\text{Lane}} + V2_{\text{Lane}} \quad V_{LL} = 35.757 \text{ k}$$

$$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF_{\text{Lane}} \quad V_{LL_I_Lane} = 64.032 \text{ k}$$

$$\text{HS-20} \quad M_{\text{HS20}} = \frac{36\text{k} \times (L - x_m) \times (x_m - 9.33\text{ft})}{L} \quad M_{\text{HS20}} = 433.108 \text{ ftk}$$

$$M_{LL_I_HS20} = M_{\text{HS20}} \times (1 + I) \times DF \quad M_{LL_I_HS20} = 1.589 \times 10^3 \text{ ftk}$$

$$V_{\text{HS20}} = \frac{36\text{k} \times (x_s - 9.33\text{ft})}{L} \quad V_{\text{HS20}} = 24.773 \text{ k}$$

$$V_{LL_I_HS20} = V_{\text{HS20}} \times (1 + I) \times DF \quad V_{LL_I_HS20} = 90.871 \text{ k}$$

$$\text{H-20} \quad M_{\text{H20}} = \frac{20\text{k} \times (L - x_m) \times (x_m - 2.8\text{ft})}{L} \quad M_{\text{H20}} = 280.729 \text{ ftk}$$

$$M_{LL_I_H20} = M_{\text{H20}} \times (1 + I) \times DF \quad M_{LL_I_H20} = 1.03 \times 10^3 \text{ ftk}$$

$$V_{\text{H20}} = \frac{20\text{k} \times (x_s - 2.8\text{ft})}{L} \quad V_{\text{H20}} = 15.629 \text{ k}$$

$$V_{LL_I_H20} = V_{\text{H20}} \times (1 + I) \times DF \quad V_{LL_I_H20} = 57.328 \text{ k}$$

$$\text{Type 3} \quad M_{\text{Type3}} = (25\text{k}) \times (x_m - 7.44\text{ft}) \times \frac{L - x_m}{L} \quad M_{\text{Type3}} = 315.282 \text{ ftk}$$

$$M_{LL_I_Type3} = M_{\text{Type3}} \times (1 + I) \times DF \quad M_{LL_I_Type3} = 1.156 \times 10^3 \text{ ftk}$$

$$V_{\text{Type3}} = \frac{25k \times (x_s - 7.44\text{ft})}{L}$$

$$V_{\text{LL_I_Type3}} = V_{\text{Type3}} \times (1 + I) \times \text{DF}$$

$$V_{\text{Type3}} = 17.879 \text{ k}$$

$$V_{\text{LL_I_Type3}} = 65.581 \text{ k}$$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s$$

$$C_1 = 1.958 \times 10^3 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y$$

$$C_2 = 3.713 \times 10^3 \text{ k} \quad (10-124)$$

$$C = \min \left(\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} \right)$$

Compressive force in slab

$$C = 1.958 \times 10^3 \text{ k}$$

$$a = \frac{C}{0.85 \times f_c \times b_{\text{eff}}}$$

Depth of concrete stressblock

$$a = 8 \text{ in} \quad (10-125)$$

Since Eq. (10-123) controls =>
steel has compression

$$C_{\text{prime}} = \frac{C_2 - C}{2}$$

Compressive force in steel

$$C_{\text{prime}} = 877.211 \text{ k}$$

$$AF_{\text{tf}} = A_{\text{tf}} \times F_y$$

top flange

$$AF_{\text{tf}} = 712.123 \text{ k}$$

$$AF_{\text{w1}} = A_{\text{w1}} \times F_y$$

web above welded plate

$$AF_{\text{w1}} = 174.913 \text{ k}$$

$$AF_{\text{p}} = A_{\text{p}} \times F_y$$

welded plate

$$AF_{\text{p}} = 750.75 \text{ k}$$

$$AF_{\text{w2}} = AF_{\text{w1}}$$

web below welded plate

$$AF_{\text{w2}} = 174.913 \text{ k}$$

$$AF_{\text{ha}} = A_{\text{ha}} \times F_y$$

horizontal part of angle

$$AF_{\text{ha}} = 528 \text{ k}$$

$$AF_{\text{va}} = A_{\text{va}} \times F_y$$

vertical part of angle

$$AF_{\text{va}} = 198 \text{ k}$$

$$AF_{\text{bf}} = AF_{\text{tf}}$$

bottom flange

$$AF_{\text{bf}} = 712.123 \text{ k}$$

$$AF_{\text{c1}} = A_{\text{c1}} \times F_y$$

first cover

$$AF_{\text{c1}} = 462 \text{ k}$$

$$AF_{\text{c2}} = A_{\text{c2}} \times F_y$$

second cover

$$AF_{\text{c2}} = 0 \text{ k}$$

Since $C_{\text{prime}} > AF_{\text{tf}} \Rightarrow y$ lies in
web above welded plate section

$$t_{\text{tf}} = 1.378 \text{ in}$$

Thickness of top flange

$$b_{\text{w1}} = 6.31 \text{ in}$$

Width of web above welded plate

$$b_{\text{p}} = 26 \text{ in}$$

Depth of welded plate

$$y = t_{\text{tf}} + \frac{C_{\text{prime}} - AF_{\text{tf}}}{AF_{\text{w1}}} \times b_{\text{w1}}$$

$$y = 7.334 \text{ in}$$

y is distance from bottom of
slab down to plastic NA

Check compact:

$$\frac{2 \times D_{\text{cp}}}{t_{\text{w}}} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

(10-129)

$$D_{\text{cp}} = y - t_{\text{tf}}$$

Depth of web in compression at
the plastic moment

$$D_{\text{cp}} = 5.956 \text{ in}$$

$$t_w = 0.84 \text{ in} \quad \text{Thickness of web}$$

$$\frac{2 \times D_{cp}}{t_w} = 14.18 \quad \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 105.858 \quad \text{OK!}$$

Check (10-129a):

$$\frac{D_p}{D_{prime}} \leq 5 \quad (10-129a)$$

$$D_p = y + t_s \quad \text{Distance from top of slab to PNA} \quad D_p = 15.334 \text{ in}$$

$$D_{prime} = 0.9 \times \frac{d + t_s}{7.5} \quad D_{prime} = 6.045 \text{ in}$$

$$\frac{D_p}{D_{prime}} = 2.537 \quad \text{OK!}$$

Since $D_{prime} < D_p < 5D_{prime} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad (10-129c)$$

$$\text{Slab:} \quad C = 1.958 \times 10^3 \text{ k} \quad d_c = \left| \frac{t_s}{2} + y \right| \quad d_c = 11.334 \text{ in}$$

$$\text{Top flange:} \quad AF_{tf} = 712.123 \text{ k} \quad d_{tf} = \left| y - \frac{t_{tf}}{2} \right| \quad d_{tf} = 6.645 \text{ in}$$

$$\text{Web above welded plate:} \quad AF_{w1} = 174.913 \text{ k} \quad d_{w1} = \left| y - t_{tf} - \frac{b_{w1}}{2} \right| \quad d_{w1} = 2.801 \text{ in}$$

$$\text{Welded plate:} \quad AF_p = 750.75 \text{ k} \quad d_p = \left| y - t_{tf} - b_{w1} - \frac{b_p}{2} \right| \quad d_p = 13.354 \text{ in}$$

$$\text{Web below welded plate:} \quad AF_{w2} = 174.913 \text{ k} \quad d_{w2} = \left| y - t_{tf} - b_{w1} - b_p - \frac{b_{w1}}{2} \right| \quad d_{w2} = 29.509 \text{ in}$$

$$\text{Horizontal part of angle:} \quad AF_{ha} = 528 \text{ k} \quad d_{ha} = \left| d - y - 2.125 \text{ in} - \frac{1 \text{ in}}{2} \right| \quad d_{ha} = 32.417 \text{ in}$$

$$\text{Vertical part of angle:} \quad AF_{va} = 198 \text{ k} \quad d_{va} = \left| d - y - 3.125 \text{ in} - \frac{3 \text{ in}}{2} \right| \quad d_{va} = 30.417 \text{ in}$$

$$\text{Bottom flange:} \quad AF_{bf} = 712.123 \text{ k} \quad d_{bf} = \left| d - y - t_{c2} - t_{c1} - \frac{t_{tf}}{2} \right| \quad d_{bf} = 33.353 \text{ in}$$

$$\text{First cover:} \quad AF_{c1} = 462 \text{ k} \quad d_{c1} = \left| d - y - t_{c2} - \frac{t_{c1}}{2} \right| \quad d_{c1} = 34.542 \text{ in}$$

$$\text{Second cover:} \quad AF_{c2} = 0 \text{ k} \quad d_{c2} = \left| d - y - \frac{t_{c2}}{2} \right| \quad d_{c2} = 35.042 \text{ in}$$

$$M_{p1} = C \times d_c + AF_{tf} \times d_{tf} + AF_{w1} \times d_{w1} + AF_p \times d_p + AF_{w2} \times d_{w2} + AF_{bf} \times d_{bf}$$

$$M_{p2} = AF_{ha} \times d_{ha} + AF_{va} \times d_{va} + AF_{c1} \times d_{c1} + AF_{c2} \times d_{c2}$$

$$M_p = M_{p1} + M_{p2}$$

$$M_p = 8.788 \times 10^3 \text{ ft-k}$$

Yield moment:

$$I_o = 7.663 \times 10^4 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - \text{Ecc} \quad \text{Distance from bottom of steel to elastic NA}$$

$$Y = 28.886 \text{ in}$$

$$M_y = F_y \times \frac{I_o}{Y}$$

$$M_y = 7.296 \times 10^3 \text{ ft-k}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{\text{prime}}}$$

$$M_n = 7.794 \times 10^3 \text{ ft-k}$$

$$M_n = 9.353 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$K = 5 \quad \text{For unstiffened beams and girders}$$

$$D = 38.62 \text{ in} \quad \text{Clear distance between flanges}$$

$$t_w = 0.84 \text{ in} \quad \text{Web thickness}$$

$$\frac{D}{t_w} = 45.976 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 620.917 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 620.917 \text{ k} \quad (10-113)$$

Rating:

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 2.316
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 3.866
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	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 4.092
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		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 6.83
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HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.571
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 2.623
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H-20	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 2.883
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 4.813
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.424
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 4.046
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 4.57
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 7.628
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 2.158
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 3.603
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 3.995
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 6.668

Girder no coverSection Properties:

$A_{c1} = 0 \text{ in}^2$	Remove area for first cover (second cover already removed)	
$t_{c1} = 0 \text{ in}$	Remove first cover (second cover already removed)	
$I_9 = 64488 \text{ in}^4$	Moment of inertia for elastic section (from Excel)	
$Ecc = 15.33 \text{ in}$	Distance from c.g. slab to c.g elastic composit section (from Excel)	
$L = 70 \text{ ft}$	Span of beam	
$t_s = 8 \text{ in}$	Thickness of concrete slab	
$DF = 2.92$	Distribution factor for a wheel line	
$x_m = 57.5 \text{ ft}$	Distance from edge of beam to calculate maximum live load moment	
$x_s = 65 \text{ ft}$	Distance from edge of beam to calculate maximum live load shear	
$A_b = A_{tf} + A_{w1} + A_p + A_{w2} + A_{ha} + A_{va} + A_{tf} + A_{c1} + A_{c2}$		$A_b = 98.51 \text{ in}^2$
$d = t_{tf} + b_{w1} + b_p + b_{w2} + t_{bf} + t_{c1} + t_{c2}$		$d = 41.376 \text{ in}$
	d is total depth of steel	
$D = b_{w1} + b_p + b_{w2}$		$D = 38.62 \text{ in}$

D is clear distance between flanges

$$b_{\text{eff}} = \min \left(\left(\frac{1}{4} \times L \right), \left(21.75 \text{ ft} \right), \left(12 \times t_s \right) \right) \quad b_{\text{eff}} = 96 \text{ in} \quad 10.3.3.1$$

Girder Loads:

$$I = \begin{cases} \frac{50 \text{ ft}}{L + 125 \text{ ft}} & \text{if } \frac{50 \text{ ft}}{L + 125 \text{ ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.256 \quad 3.8.2.1$$

Maximum Live Load Moments:

$$\text{Moment: } \frac{L - x_m}{L} = 0.179 \quad \text{Shear: } \frac{L - x_s}{L} = 0.071 \quad [3] \text{ p.84-87}$$

Lane $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear
Uniform Load of 0.64 k/ft over the whole span fig. 3.7.6.b

$$\begin{aligned} \text{Uniform load: } M1_{\text{Lane}} &= \frac{1}{2} \times \omega \times L \times \left(x_m - \frac{x_m^2}{L} \right) & M1_{\text{Lane}} &= 230 \text{ ftk} \\ V1_{\text{Lane}} &= \frac{1}{2} \times \omega \times L \times \left(2 \times \frac{x_s}{L} - 1 \right) & V1_{\text{Lane}} &= 19.2 \text{ k} \\ \text{Point Load: } M2_{\text{Lane}} &= \frac{L - x_m}{L} \times P_m \times x_m & M2_{\text{Lane}} &= 184.821 \text{ ftk} \\ V2_{\text{Lane}} &= P_s \times \frac{x_s}{L} & V2_{\text{Lane}} &= 24.143 \text{ k} \end{aligned}$$

All values are lane loads.

$$\begin{aligned} M_{\text{LL}} &= M1_{\text{Lane}} + M2_{\text{Lane}} & M_{\text{LL}} &= 414.821 \text{ ftk} \\ M_{\text{LL}_I\text{Lane}} &= M_{\text{LL}} \times (1 + I) \times DF_{\text{Lane}} & M_{\text{LL}_I\text{Lane}} &= 742.84 \text{ ftk} \\ V_{\text{LL}} &= V1_{\text{Lane}} + V2_{\text{Lane}} & V_{\text{LL}} &= 43.343 \text{ k} \\ V_{\text{LL}_I\text{Lane}} &= V_{\text{LL}} \times (1 + I) \times DF_{\text{Lane}} & V_{\text{LL}_I\text{Lane}} &= 77.616 \text{ k} \end{aligned}$$

$$\begin{aligned} \text{HS-20 } M_{\text{HS20}} &= \frac{36 \text{ k} \times (L - x_m) \times (x_m - 9.33 \text{ ft})}{L} & M_{\text{HS20}} &= 309.664 \text{ ftk} \\ M_{\text{LL}_I\text{HS20}} &= M_{\text{HS20}} \times (1 + I) \times DF & M_{\text{LL}_I\text{HS20}} &= 1.136 \times 10^3 \text{ ftk} \\ V_{\text{HS20}} &= \frac{36 \text{ k} \times (x_s - 9.33 \text{ ft})}{L} & V_{\text{HS20}} &= 28.63 \text{ k} \\ V_{\text{LL}_I\text{HS20}} &= V_{\text{HS20}} \times (1 + I) \times DF & V_{\text{LL}_I\text{HS20}} &= 105.02 \text{ k} \\ \text{H-20 } M_{\text{H20}} &= \frac{20 \text{ k} \times (L - x_m) \times (x_m - 2.8 \text{ ft})}{L} & M_{\text{H20}} &= 195.357 \text{ ftk} \\ M_{\text{LL}_I\text{H20}} &= M_{\text{H20}} \times (1 + I) \times DF & M_{\text{LL}_I\text{H20}} &= 716.597 \text{ ftk} \end{aligned}$$

$$V_{H20} = \frac{20k \times (x_s - 2.8ft)}{L} \quad V_{H20} = 17.771 \text{ k}$$

$$V_{LL_I_H20} = V_{H20} \times (1 + I) \times DF \quad V_{LL_I_H20} = 65.188 \text{ k}$$

$$\text{Type 3} \quad M_{Type3} = (25k) \times (x_m - 7.44ft) \times \frac{L - x_m}{L} \quad M_{Type3} = 223.482 \text{ ftk}$$

$$M_{LL_I_Type3} = M_{Type3} \times (1 + I) \times DF \quad M_{LL_I_Type3} = 819.764 \text{ ftk}$$

$$V_{Type3} = \frac{25k \times (x_s - 7.44ft)}{L} \quad V_{Type3} = 20.557 \text{ k}$$

$$V_{LL_I_Type3} = V_{Type3} \times (1 + I) \times DF \quad V_{LL_I_Type3} = 75.406 \text{ k}$$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{eff} \times t_s \quad \text{Slab} \quad C_1 = 1.958 \times 10^3 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y \quad \text{Steel} \quad C_2 = 3.251 \times 10^3 \text{ k} \quad (10-124)$$

$$C = \min \left(\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} \right) \quad \text{Compressive force in slab} \quad C = 1.958 \times 10^3 \text{ k}$$

$$a = \frac{C}{0.85 \times f_c \times b_{eff}} \quad \text{Depth of concrete stressblock} \quad a = 8 \text{ in} \quad (10-125)$$

Since Eq. (10-123) controls =>
steel has compression

$$C_{prime} = \frac{C_2 - C}{2} \quad \text{Compressive force in steel} \quad C_{prime} = 646.211 \text{ k}$$

$$AF_{tf} = A_{tf} \times F_y \quad \text{top flange} \quad AF_{tf} = 712.123 \text{ k}$$

$$AF_{w1} = A_{w1} \times F_y \quad \text{web above welded plate} \quad AF_{w1} = 174.913 \text{ k}$$

$$AF_p = A_p \times F_y \quad \text{welded plate} \quad AF_p = 750.75 \text{ k}$$

$$AF_{w2} = AF_{w1} \quad \text{web below welded plate} \quad AF_{w2} = 174.913 \text{ k}$$

$$AF_{ha} = A_{ha} \times F_y \quad \text{horizontal part of angle} \quad AF_{ha} = 528 \text{ k}$$

$$AF_{va} = A_{va} \times F_y \quad \text{vertical part of angle} \quad AF_{va} = 198 \text{ k}$$

$$AF_{bf} = AF_{tf} \quad \text{bottom flange} \quad AF_{bf} = 712.123 \text{ k}$$

$$AF_{c1} = A_{c1} \times F_y \quad \text{first cover} \quad AF_{c1} = 0 \text{ k}$$

$$AF_{c2} = A_{c2} \times F_y \quad \text{second cover} \quad AF_{c2} = 0 \text{ k}$$

Since $C_{prime} < AF_{tf} \Rightarrow$
y lies in the top flange

$$t_{tf} = 1.378 \text{ in} \quad \text{Thickness of top flange}$$

$$y = \frac{C_{prime}}{AF_{tf}} \times t_{tf} \quad y \text{ is distance from bottom of slab down to plastic NA} \quad y = 1.25 \text{ in}$$

Check compact:

$$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \begin{array}{l} D_{cp} \text{ is depth of web in compression} \\ \text{at the plastic moment} \end{array} \quad (10-129)$$

Since plastic neutral axis lies in top flange => OK!

Check (10-129a):

$$\frac{D_p}{D_{prime}} \leq 5 \quad (10-129a)$$

$$D_p = y + t_s \quad \text{Distance from top of slab to PNA} \quad D_p = 9.25 \text{ in}$$

$$D_{prime} = 0.9 \times \frac{d + t_s}{7.5} \quad D_{prime} = 5.925 \text{ in}$$

$$\frac{D_p}{D_{prime}} = 1.561 \quad \text{OK!}$$

Since $D_{prime} < D_p < 5D_{prime} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad (10-129c)$$

$$\text{Slab:} \quad C = 1.958 \times 10^3 \text{ k} \quad d_c = \left| \frac{t_s}{2} + y \right| \quad d_c = 5.25 \text{ in}$$

$$\text{Top flange:} \quad AF_{tf} = 712.123 \text{ k} \quad d_{tf} = \left| y - \frac{t_{tf}}{2} \right| \quad d_{tf} = 0.561 \text{ in}$$

$$\text{Web above welded plate:} \quad AF_{w1} = 174.913 \text{ k} \quad d_{w1} = \left| y - t_{tf} - \frac{b_{w1}}{2} \right| \quad d_{w1} = 3.283 \text{ in}$$

$$\text{Welded plate:} \quad AF_p = 750.75 \text{ k} \quad d_p = \left| y - t_{tf} - b_{w1} - \frac{b_p}{2} \right| \quad d_p = 19.438 \text{ in}$$

$$\text{Web below welded plate:} \quad AF_{w2} = 174.913 \text{ k} \quad d_{w2} = \left| y - t_{tf} - b_{w1} - b_p - \frac{b_{w1}}{2} \right| \quad d_{w2} = 35.593 \text{ in}$$

$$\text{Horizontal part of angle:} \quad AF_{ha} = 528 \text{ k} \quad d_{ha} = \left| d - y - 2.125 \text{ in} - \frac{1 \text{ in}}{2} \right| \quad d_{ha} = 37.501 \text{ in}$$

$$\text{Vertical part of angle:} \quad AF_{va} = 198 \text{ k} \quad d_{va} = \left| d - y - 3.125 \text{ in} - \frac{3 \text{ in}}{2} \right| \quad d_{va} = 35.501 \text{ in}$$

$$\text{Bottom flange:} \quad AF_{bf} = 712.123 \text{ k} \quad d_{bf} = \left| d - y - t_{c2} - t_{c1} - \frac{t_{tf}}{2} \right| \quad d_{bf} = 39.437 \text{ in}$$

$$\text{First cover:} \quad AF_{c1} = 0 \text{ k} \quad d_{c1} = \left| d - y - t_{c2} - \frac{t_{c1}}{2} \right| \quad d_{c1} = 40.126 \text{ in}$$

$$\text{Second cover:} \quad AF_{c2} = 0 \text{ k} \quad d_{c2} = \left| d - y - \frac{t_{c2}}{2} \right| \quad d_{c2} = 40.126 \text{ in}$$

$$M_{p1} = C \times d_c + AF_{tf} \times d_{tf} + AF_{w1} \times d_{w1} + AF_p \times d_p + AF_{w2} \times d_{w2} + AF_{bf} \times d_{bf}$$

$$M_{p2} = AF_{ha} \times d_{ha} + AF_{va} \times d_{va} + AF_{c1} \times d_{c1} + AF_{c2} \times d_{c2}$$

$$M_p = M_{p1} + M_{p2}$$

$$M_p = 7.249 \times 10^3 \text{ ft-k}$$

Yield moment:

$$I_9 = 6.449 \times 10^4 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - E_{cc} \quad \text{Distance from bottom of steel to elastic NA} \quad Y = 30.046 \text{ in}$$

$$M_y = F_y \times \frac{I_9}{Y} \quad M_y = 5.902 \times 10^3 \text{ ftk}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{\text{prime}}} \quad M_n = 6.936 \times 10^3 \text{ ftk}$$

$$M_n = 8.323 \times 10^4 \text{ in} \times k$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$K = 5 \quad \text{For unstiffened beams and girders}$$

$$D = 38.62 \text{ in} \quad \text{Clear distance between flanges}$$

$$t_w = 0.84 \text{ in} \quad \text{Web thickness}$$

$$\frac{D}{t_w} = 45.976 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 620.917 k \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 620.917 k \quad (10-113)$$

Rating:

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL-I_Lane}}$	RF = 2.828
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL-I_Lane}}$	RF = 4.72
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	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL-I_Lane}}$	RF = 3.375
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		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL-I_Lane}}$	RF = 5.634
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HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL-I_HS20}}$	RF = 1.849
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL-I_HS20}}$	RF = 3.087
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H-20	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 2.495
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 4.164
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.931
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 4.893
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 4.019
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 6.709
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 2.563
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 4.277
Type-3	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 3.474
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 5.8

Girder no angleSection Properties:

$$A_{ha} = 0 \text{ in}^2 \quad A_{va} = 0 \text{ in}^2 \quad \text{Remove area for angle (both covers already removed)}$$

$$I_g = 46404 \text{ in}^4 \quad \text{Moment of inertia for elastic section (from Excel)}$$

$$Ecc = 11.67 \text{ in} \quad \text{Distance from c.g. slab to c.g elastic composit section (from Excel)}$$

$$L = 70 \text{ ft} \quad \text{Span of beam}$$

$$t_s = 8 \text{ in} \quad \text{Thickness of concrete slab}$$

$$DF = 2.92 \quad \text{Distribution factor for a wheel line}$$

$$x_m = 65 \text{ ft} \quad \text{Distance from edge of beam to calculate maximum live load moment}$$

$$x_s = 70 \text{ ft} \quad \text{Distance from edge of beam to calculate maximum live load shear}$$

$$A_b = A_{tf} + A_{wl} + A_p + A_{w2} + A_{ha} + A_{va} + A_{tf} + A_{cl} + A_{c2} \quad A_b = 76.51 \text{ in}^2$$

$$d = t_{tf} + b_{wl} + b_p + b_{w2} + t_{bf} + t_{cl} + t_{c2} \quad \text{Total depth of steel} \quad d = 41.376 \text{ in}$$

$$D = b_{wl} + b_p + b_{w2} \quad \text{Clear distance between flanges} \quad D = 38.62 \text{ in}$$

$$b_{\text{eff}} = \min \left(\left(\frac{1}{4} \times L \right), \left(21.75 \text{ ft} \right), \left(12 \times t_s \right) \right)$$

$$b_{\text{eff}} = 96 \text{ in} \quad 10.38.3.1$$

Girder Loads:

$$I = \begin{cases} \frac{50 \text{ ft}}{L + 125 \text{ ft}} & \text{if } \frac{50 \text{ ft}}{L + 125 \text{ ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.256 \quad 3.8.2.1$$

Maximum Live Load Moments:

$$\text{Moment: } \frac{L - x_m}{L} = 0.071 \quad \text{Shear: } \frac{L - x_s}{L} = 0 \quad [3] \text{ p.84-87}$$

Lane $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear
Uniform Load of 0.64 k/ft over the whole span fig. 3.7.6.b

$$\begin{aligned} \text{Uniform load: } M_{1\text{Lane}} &= \frac{1}{2} \times \omega \times L \times \left(x_m - \frac{x_m^2}{L} \right) & M_{1\text{Lane}} &= 104 \text{ ftk} \\ V_{1\text{Lane}} &= \frac{1}{2} \times \omega \times L \times \left(2 \times \frac{x_s}{L} - 1 \right) & V_{1\text{Lane}} &= 22.4 \text{ k} \\ \text{Point Load: } M_{2\text{Lane}} &= \frac{L - x_m}{L} \times P_m \times x_m & M_{2\text{Lane}} &= 83.571 \text{ ftk} \\ V_{2\text{Lane}} &= P_s \times \frac{x_s}{L} & V_{2\text{Lane}} &= 26 \text{ k} \end{aligned}$$

All values are lane loads.

$$\begin{aligned} M_{LL} &= M_{1\text{Lane}} + M_{2\text{Lane}} & M_{LL} &= 187.571 \text{ ftk} \\ M_{LL_I_Lane} &= M_{LL} \times (1 + I) \times DF_{\text{Lane}} & M_{LL_I_Lane} &= 335.893 \text{ ftk} \\ V_{LL} &= V_{1\text{Lane}} + V_{2\text{Lane}} & V_{LL} &= 48.4 \text{ k} \\ V_{LL_I_Lane} &= V_{LL} \times (1 + I) \times DF_{\text{Lane}} & V_{LL_I_Lane} &= 86.672 \text{ k} \\ \text{HS-20 } M_{\text{HS20}} &= \frac{36 \text{ k} \times (L - x_m) \times (x_m - 9.33 \text{ ft})}{L} & M_{\text{HS20}} &= 143.151 \text{ ftk} \\ M_{LL_I_HS20} &= M_{\text{HS20}} \times (1 + I) \times DF & M_{LL_I_HS20} &= 525.1 \text{ ftk} \\ V_{\text{HS20}} &= \frac{36 \text{ k} \times (x_s - 9.33 \text{ ft})}{L} & V_{\text{HS20}} &= 31.202 \text{ k} \\ V_{LL_I_HS20} &= V_{\text{HS20}} \times (1 + I) \times DF & V_{LL_I_HS20} &= 114.452 \text{ k} \\ \text{H-20 } M_{\text{H20}} &= \frac{20 \text{ k} \times (L - x_m) \times (x_m - 2.8 \text{ ft})}{L} & M_{\text{H20}} &= 88.857 \text{ ftk} \\ M_{LL_I_H20} &= M_{\text{H20}} \times (1 + I) \times DF & M_{LL_I_H20} &= 325.94 \text{ ftk} \\ V_{\text{H20}} &= \frac{20 \text{ k} \times (x_s - 2.8 \text{ ft})}{L} & V_{\text{H20}} &= 19.2 \text{ k} \end{aligned}$$

	$V_{LL_I_H20} = V_{H20} \times (1 + I) \times DF$	$V_{LL_I_H20} = 70.428 \text{ k}$
Type 3	$M_{Type3} = (25\text{k}) \times (x_m - 7.44\text{ft}) \times \frac{L - x_m}{L}$	$M_{Type3} = 102.786 \text{ ftk}$
	$M_{LL_I_Type3} = M_{Type3} \times (1 + I) \times DF$	$M_{LL_I_Type3} = 377.032 \text{ ftk}$
	$V_{Type3} = \frac{25\text{k} \times (x_s - 7.44\text{ft})}{L}$	$V_{Type3} = 22.343 \text{ k}$
	$V_{LL_I_Type3} = V_{Type3} \times (1 + I) \times DF$	$V_{LL_I_Type3} = 81.957 \text{ k}$

Capacities:

$C_1 = 0.85 \times f_c \times b_{eff} \times t_s$	$C_1 = 1.958 \times 10^3 \text{ k}$	(10-123)
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$C_2 = A_b \times F_y$	$C_2 = 2.525 \times 10^3 \text{ k}$	(10-124)
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$C = \min\left(\left(\begin{matrix} C_1 \\ C_2 \end{matrix}\right)\right)$	Compressive force in slab	$C = 1.958 \times 10^3 \text{ k}$
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$a = \frac{C}{0.85 \times f_c \times b_{eff}}$	Depth of concrete stressblock	$a = 8 \text{ in}$	(10-125)
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Since Eq. (10-123) controls =>
steel has compression

$C_{prime} = \frac{C_2 - C}{2}$	$C_{prime} = 283.211 \text{ k}$
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$AF_{tf} = A_{tf} \times F_y$	top flange	$AF_{tf} = 712.123 \text{ k}$
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$AF_{w1} = A_{w1} \times F_y$	web above welded plate	$AF_{w1} = 174.913 \text{ k}$
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$AF_p = A_p \times F_y$	welded plate	$AF_p = 750.75 \text{ k}$
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$AF_{w2} = AF_{w1}$	web below welded plate	$AF_{w2} = 174.913 \text{ k}$
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$AF_{ha} = A_{ha} \times F_y$	horizontal part of angle	$AF_{ha} = 0 \text{ k}$
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$AF_{va} = A_{va} \times F_y$	vertical part of angle	$AF_{va} = 0 \text{ k}$
-------------------------------	------------------------	-------------------------

$AF_{bf} = AF_{tf}$	bottom flange	$AF_{bf} = 712.123 \text{ k}$
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$AF_{c1} = A_{c1} \times F_y$	first cover	$AF_{c1} = 0 \text{ k}$
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$AF_{c2} = A_{c2} \times F_y$	second cover	$AF_{c2} = 0 \text{ k}$
-------------------------------	--------------	-------------------------

Since $C_{prime} < AF_{tf}$ =>
y lies in the top flange

$t_{tf} = 1.378 \text{ in}$	Thickness of top flange
-----------------------------	-------------------------

$y = \frac{C_{prime}}{AF_{tf}} \times t_{tf}$	y is distance from bottom of slab down to plastic NA	$y = 0.548 \text{ in}$
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Check compact:

$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$	D_{cp} is depth of web in compression at the plastic moment	(10-129)
	Since plastic neutral axis lies in top flange => OK!	

Check (10-129a):

$$\frac{D_p}{D_{prime}} \leq 5 \quad (10-129a)$$

$$D_p = y + t_s \quad \text{Distance from top of slab to PNA} \quad D_p = 8.548 \text{ in}$$

$$D_{prime} = 0.9 \times \frac{d + t_s}{7.5} \quad D_{prime} = 5.925 \text{ in}$$

$$\frac{D_p}{D_{prime}} = 1.443 \quad \text{OK!}$$

Since $D_{prime} < D_p < 5D_{prime} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad (10-129c)$$

$$\text{Slab:} \quad C = 1.958 \times 10^3 \text{ k} \quad d_c = \left| \frac{t_s}{2} + y \right| \quad d_c = 4.548 \text{ in}$$

$$\text{Top flange:} \quad AF_{tf} = 712.123 \text{ k} \quad d_{tf} = \left| y - \frac{t_{tf}}{2} \right| \quad d_{tf} = 0.141 \text{ in}$$

$$\text{Web above welded plate:} \quad AF_{w1} = 174.913 \text{ k} \quad d_{w1} = \left| y - t_{tf} - \frac{b_{w1}}{2} \right| \quad d_{w1} = 3.985 \text{ in}$$

$$\text{Welded plate:} \quad AF_p = 750.75 \text{ k} \quad d_p = \left| y - t_{tf} - b_{w1} - \frac{b_p}{2} \right| \quad d_p = 20.14 \text{ in}$$

$$\text{Web below welded plate:} \quad AF_{w2} = 174.913 \text{ k} \quad d_{w2} = \left| y - t_{tf} - b_{w1} - b_p - \frac{b_{w1}}{2} \right| \quad d_{w2} = 36.295 \text{ in}$$

$$\text{Horizontal part of angle:} \quad AF_{ha} = 0 \text{ k} \quad d_{ha} = \left| d - y - 2.125 \text{ in} - \frac{1 \text{ in}}{2} \right| \quad d_{ha} = 38.203 \text{ in}$$

$$\text{Vertical part of angle:} \quad AF_{va} = 0 \text{ k} \quad d_{va} = \left| d - y - 3.125 \text{ in} - \frac{3 \text{ in}}{2} \right| \quad d_{va} = 36.203 \text{ in}$$

$$\text{Bottom flange:} \quad AF_{bf} = 712.123 \text{ k} \quad d_{bf} = \left| d - y - t_{c2} - t_{c1} - \frac{t_{tf}}{2} \right| \quad d_{bf} = 40.139 \text{ in}$$

$$\text{First cover:} \quad AF_{c1} = 0 \text{ k} \quad d_{c1} = \left| d - y - t_{c2} - \frac{t_{c1}}{2} \right| \quad d_{c1} = 40.828 \text{ in}$$

$$\text{Second cover:} \quad AF_{c2} = 0 \text{ k} \quad d_{c2} = \left| d - y - \frac{t_{c2}}{2} \right| \quad d_{c2} = 40.828 \text{ in}$$

$$M_{p1} = C \times d_c + AF_{tf} \times d_{tf} + AF_{w1} \times d_{w1} + AF_p \times d_p + AF_{w2} \times d_{w2} + AF_{bf} \times d_{bf}$$

$$M_{p2} = AF_{ha} \times d_{ha} + AF_{va} \times d_{va} + AF_{c1} \times d_{c1} + AF_{c2} \times d_{c2}$$

$$M_p = M_{p1} + M_{p2} \quad M_p = 4.98 \times 10^3 \text{ ftk}$$

Yield moment:

$$I_g = 4.64 \times 10^4 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - Ecc \quad \text{Distance from bottom of steel to elastic NA} \quad Y = 33.706 \text{ in}$$

$$M_y = F_y \times \frac{I_y}{Y}$$

$$M_y = 3.786 \times 10^3 \text{ ft-k}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{\text{prime}}}$$

$$M_n = 4.785 \times 10^3 \text{ ft-k}$$

$$M_n = 5.742 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$K = 5$$

For unstiffened beams and girders

$$D = 38.62 \text{ in}$$

Clear distance between flanges

$$t_w = 0.84 \text{ in}$$

Web thickness

$$\frac{D}{t_w} = 45.976$$

$$\frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \Rightarrow$$

$$C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 620.917 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p$$

$$V_n = 620.917 \text{ k} \quad (10-113)$$

Rating:

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 3.303
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 5.513
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 3.023
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 5.046
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 2.113
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 3.527
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 2.289

		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_HS20}}$	RF = 3.821
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 3.404
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_H20}}$	RF = 5.682
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 3.72
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_H20}}$	RF = 6.209
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 2.943
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_Type3}}$	RF = 4.912
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 3.197
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_Type3}}$	RF = 5.336

RATING FOR STRINGERS

Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of concrete}$$

$$f_c = 3\text{ksi} \quad \text{Concrete strength}$$

$$F_y = 33\text{ksi} \quad \text{Steel strength}$$

Interior Stringer 15" I 42.9

Input:

$$A_{tf} = 5.50\text{in} \times 0.834\text{in} \quad \text{Area of top flange} \quad A_{tf} = 4.587\text{in}^2$$

$$A_w = 13.332\text{in} \times 0.41\text{in} \quad \text{Area of web} \quad A_w = 5.466\text{in}^2$$

$$A_{bf} = 5.50\text{in} \times 0.834\text{in} \quad \text{Area of bottom flange} \quad A_{bf} = 4.587\text{in}^2$$

$$t_{tf} = 0.834\text{in} \quad \text{Thickness of top flange}$$

$$b_w = 13.332\text{in} \quad \text{Width of web}$$

$t_w = 0.41 \text{ in}$ Thickness of web

$t_{bf} = 0.834 \text{ in}$ Thickness of bottom flange

Loads For Lane Loading:

$P_s = 26 \text{ k}$ Point Load for Shear for Lane Loading fig. 3.7.6.b

$P_m = 18 \text{ k}$ Point Load for Moment for Lane Loading

$\omega = 0.64 \frac{\text{k}}{\text{ft}}$ Uniform Load for Lane Loading

Live Load Distribution Factor for Lane Load per lane:

$S_b = \frac{(4\text{ft} + 10.5\text{in}) + 4\text{ft}}{2}$ Average stringer spacing in ft $S_b = 4.437 \text{ ft}$ table 3.23.1

$DF_{\text{Lane}} = \frac{S_b}{5.5\text{ft}}$ $DF_{\text{Lane}} = 0.807$

Live Load Distribution Factor for Design Trucks per wheel line:

$S_b = \frac{(4\text{ft} + 10.5\text{in}) + 4\text{ft}}{2}$ Average stringer spacing in ft $S_b = 4.437 \text{ ft}$ table 3.23.1

$DF = \frac{S_b}{5.5\text{ft}}$ $DF = 0.807$

Section Properties:

$I_g = 1947 \text{ in}^4$ Moment of inertia for elastic section (from Excel)

$Ecc = 2.60 \text{ in}$ Distance from c.g. slab to c.g elastic composit section (from Excel)

$L = 17.5 \text{ ft}$ Design span of beam

$t_s = 8 \text{ in}$ Thickness of concrete slab

$A_b = A_{tf} + A_w + A_{bf}$ $A_b = 14.64 \text{ in}^2$

$d = t_{tf} + b_w + t_{bf}$ Total depth of steel $d = 15 \text{ in}$

$D = b_w$ Clear distance between flanges $D = 13.332 \text{ in}$

$b_{\text{eff}} = \min \left[\begin{array}{l} \left[\frac{1}{4} \times L \right] \\ \left[\frac{1}{2} \times (4\text{ft} + 4\text{ft}) \right] \\ 12 \times t_s \end{array} \right]$ $b_{\text{eff}} = 48 \text{ in}$ 10.38.3.1

Girder Loads:

$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases}$ Impact $I = 0.3$ 3.8.2.1

Maximum Live Load Moments:

Lane Load $P_m = 18 \text{ k}$ for moment applied at midspan, [3] p.85, 87
 $P_s = 26 \text{ k}$ for shear applied at one end fig. 3.7.6.b
 Uniform Load of 0.64 k/ft over the whole span

$$\text{Uniform load: } M1_{\text{Lane}} = \frac{\omega \times L^2}{8} \quad M1_{\text{Lane}} = 24.5 \text{ ftk}$$

$$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L \quad V1_{\text{Lane}} = 5.6 \text{ k}$$

$$\text{Point Load: } M2_{\text{Lane}} = \frac{P_m \times L}{4} \quad M2_{\text{Lane}} = 78.75 \text{ ftk}$$

$$V2_{\text{Lane}} = P_s \quad V2_{\text{Lane}} = 26 \text{ k}$$

All values are lane loads. Since the moment and shear are based on wheel line loads and not truck loads => must divide lane loads by 2 to be compatible with other loads.

$$M_{LL} = \frac{1}{2} \times (M1_{\text{Lane}} + M2_{\text{Lane}}) \quad M_{LL} = 51.625 \text{ ftk}$$

$$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF_{\text{Lane}} \quad M_{LL_I_Lane} = 54.148 \text{ ftk}$$

$$V_{LL} = \frac{1}{2} \times (V1_{\text{Lane}} + V2_{\text{Lane}}) \quad V_{LL} = 15.8 \text{ k}$$

$$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF_{\text{Lane}} \quad V_{LL_I_Lane} = 16.572 \text{ k}$$

HS-20
Maximum moment occur when wheel line load is applied at midspan. Maximum shear occur when wheel line load is applied at the end.

$$P = 16 \text{ k}$$

$$M_{LL} = \frac{P \times L}{4} \quad M_{LL} = 70 \text{ ftk}$$

$$M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF \quad M_{LL_I_HS20} = 73.42 \text{ ftk}$$

$$V_{LL} = P + P \times \frac{L - 14 \text{ ft}}{L} \quad V_{LL} = 19.2 \text{ k}$$

$$V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF \quad V_{LL_I_HS20} = 20.138 \text{ k}$$

H-20
Maximum moment occur when wheel line load is applied at midspan. Maximum shear occur when wheel line load is applied at the end.

$$P = 16 \text{ k}$$

$$M_{LL} = \frac{P \times L}{4} \quad M_{LL} = 70 \text{ ftk}$$

$$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF \quad M_{LL_I_H20} = 73.42 \text{ ftk}$$

$$V_{LL} = 16 \text{ k} + 4 \text{ k} \times \frac{L - 14 \text{ ft}}{L} \quad V_{LL} = 16.8 \text{ k}$$

$$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF \quad V_{LL_I_H20} = 20.138 \text{ k}$$

Type-3
Maximum moment occur when one wheel line load is applied 2 ft from midspan the second wheel line is symmetric to the first wheel line.
Maximum shear occur when one wheel line load is applied at the end and another 4 ft to the side.

$$P = 8.5 \text{ k}$$

$$M_{LL} = P \times \left(\frac{L}{2} - 2 \text{ ft} \right) \quad M_{LL} = 57.375 \text{ ftk}$$

$$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF \quad M_{LL_I_Type3} = 60.179 \text{ ftk}$$

$$V_{LL} = 8.5 \text{ k} + 8.5 \text{ k} \times \frac{L - 4 \text{ ft}}{L} \quad V_{LL} = 15.057 \text{ k}$$

$$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF \quad V_{LL_I_Type3} = 15.793 \text{ k}$$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb and parapet equally distributed to all girders/stringers.

$$\text{Steel:} \quad w_b = w_{\text{steel}} \times A_b \quad w_b = 0.05 \frac{\text{k}}{\text{ft}}$$

$$\text{Slab:} \quad w_s = w_{\text{concrete}} \times t_s \times \left[\frac{(4\text{ft} + 10.5\text{in}) + 4\text{ft}}{2} \right] \quad w_s = 0.444 \frac{\text{k}}{\text{ft}}$$

$$\text{Overlay:} \quad w_o = w_{\text{concrete}} \times \frac{(4\text{ft} + 10.5\text{in}) + 4\text{ft}}{2} \times 1.89\text{in} \quad w_o = 0.105 \frac{\text{k}}{\text{ft}}$$

Total Dead Load = sum w + add 5%

$$DL = (w_b + w_s + w_o) \times 1.05 \quad DL = 0.628 \frac{\text{k}}{\text{ft}}$$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8} \quad M_{DL} = 24.053 \text{ ft-k}$$

$$V_{DL} = \frac{1}{2} \times DL \times L \quad V_{DL} = 5.498 \text{ k}$$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s \quad C_1 = 979.2 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y \quad C_2 = 483.124 \text{ k} \quad (10-124)$$

$$C = \min \left(\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} \right) \quad \text{Compressive force in slab} \quad C = 483.124 \text{ k}$$

$$a = \frac{C}{0.85 \times f_c \times b_{\text{eff}}} \quad \text{Depth of stressblock} \quad a = 3.947 \text{ in} \quad (10-125)$$

a is the distance from top of slab down to plastic NA

$$AF_{tf} = A_{tf} \times F_y \quad \text{top flange} \quad AF_{tf} = 151.371 \text{ k}$$

$$AF_w = A_w \times F_y \quad \text{web above welded plate} \quad AF_w = 180.382 \text{ k}$$

$$AF_{bf} = AF_{tf} \quad \text{bottom flange} \quad AF_{bf} = 151.371 \text{ k}$$

Check compact:

$$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \begin{array}{l} D_{cp} \text{ is depth of web in compression.} \\ \text{Since plastic neutral axis lies in slab} \Rightarrow \text{OK!} \end{array} \quad (10-129)$$

Check (10-129a):

$$\frac{D_p}{D_{\text{prime}}} \leq 5 \quad (10-129a)$$

$$D_p = a \quad \text{Distance from top of slab to PNA} \quad D_p = 3.947 \text{ in}$$

$$D_{\text{prime}} = 0.9 \times \frac{d + t_s}{7.5} \quad D_{\text{prime}} = 2.76 \text{ in}$$

$$\frac{D_p}{D_{\text{prime}}} = 1.43 \quad \text{OK!}$$

Since $D_{prime} < D_p < 5D_{prime} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad (10-129c)$$

Slab: $C = 483.124 \text{ k}$ $d_c = \frac{a}{2}$ $d_c = 1.974 \text{ in}$

Top flange: $AF_{tf} = 151.371 \text{ k}$ $d_{tf} = t_s - a + \frac{t_{tf}}{2}$ $d_{tf} = 4.47 \text{ in}$

Web: $AF_w = 180.382 \text{ k}$ $d_w = t_s - a + t_{tf} + \frac{t_w}{2}$ $d_w = 5.092 \text{ in}$

Bottom flange: $AF_{bf} = 151.371 \text{ k}$ $d_{bf} = d + t_s - a - \frac{t_{tf}}{2}$ $d_{bf} = 18.636 \text{ in}$

$$M_p = C \times d_c + AF_{tf} \times d_{tf} + AF_w \times d_w + AF_{bf} \times d_{bf} \quad M_p = 447.459 \text{ ftk}$$

Yield moment:

$$I_g = 1.947 \times 10^3 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - Ecc \quad \text{Distance from bottom of steel to elastic NA} \quad Y = 16.4 \text{ in}$$

$$M_y = F_y \times \frac{I_g}{Y} \quad M_y = 326.479 \text{ ftk}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad M_n = 429.185 \text{ ftk}$$

$$M_n = 5.15 \times 10^3 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$K = 5$ For unstiffened beams and girders

$D = 13.332 \text{ in}$ Clear distance between flanges

$t_w = 0.41 \text{ in}$ Web thickness

$$\frac{D}{t_w} = 32.517 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 104.622 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 104.622 \text{ k} \quad (10-113)$$

Rating:Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$ Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 3.387
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 5.653
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 2.711
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 4.525
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 2.498
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 4.169
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 2.231
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 3.723
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.498
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 4.169
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.549
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 4.255
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 3.047
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 5.086
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.844
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 4.748

End stringer 10" I 25.4Live Load Distribution Factors:

DF = 0.807	Same distribution factor for design truck loads as for previous stringer
DF _{Lane} = 0.807	Same distribution factor for design lane load as for previous stringer

Section Properties:

$I_g = 701 \text{ in}^4$	Moment of inertia for elastic section (from Excel)	
Ecc = 2.16in	Distance from c.g. slab to c.g. elastic composit section (from Excel)	
L = 8.75ft	Design span of beam	
$t_s = 8 \text{ in}$	Thickness of concrete slab	
$A_{tf} = 4.66 \text{ in} \times 0.673 \text{ in}$	Area of top flange	$A_{tf} = 3.136 \text{ in}^2$
$A_w = 8.654 \text{ in} \times 0.31 \text{ in}$	Area of web	$A_w = 2.683 \text{ in}^2$
$A_{bf} = 4.66 \text{ in} \times 0.673 \text{ in}$	Area of bottom flange	$A_{bf} = 3.136 \text{ in}^2$
$t_{tf} = 0.673 \text{ in}$	Thickness of top flange	
$b_w = 8.654 \text{ in}$	Width of web	
$t_{bf} = 0.673 \text{ in}$	Thickness of bottom flange	
$A_b = A_{tf} + A_w + A_{bf}$	Area of steel	$A_b = 8.955 \text{ in}^2$
$d = t_{tf} + b_w + t_{bf}$	Total depth of steel	$d = 10 \text{ in}$
$D = b_w$	Clear distance between flanges	$D = 8.654 \text{ in}$
$t_w = 0.31 \text{ in}$	Thickness of web	
$b_{eff} = \min \left[\begin{bmatrix} \frac{1}{4} \times L \\ \frac{1}{2} \times (4\text{ft} + 4\text{ft}) \\ 12 \times t_s \end{bmatrix} \right]$		$b_{eff} = 26.25 \text{ in}$

10.38.3.1

Girder Loads:

$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases}$	Impact	$I = 0.3$	3.8.2.1
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Maximum Live Load Moments:

Lane Load	$P_m = 18\text{k}$ for moment applied at midspan, $P_s = 26\text{k}$ for shear applied at one end Uniform Load of 0.64 k/ft over the whole span	[3] p.85, 87 fig. 3.7.6.b
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Uniform load:	$M_{1\text{Lane}} = \frac{\omega \times L^2}{8}$	$M_{1\text{Lane}} = 6.125 \text{ ftk}$
	$V_{1\text{Lane}} = \frac{1}{2} \times \omega \times L$	$V_{1\text{Lane}} = 2.8 \text{ k}$

Point Load: $M_{2Lane} = \frac{P_m \times L}{4}$ $M_{2Lane} = 39.375 \text{ ftk}$

$V_{2Lane} = P_s$ $V_{2Lane} = 26 \text{ k}$

All values are lane loads. Since the distribution factor is based on wheel line load and not truck load => must divide lane loads by 2.

$M_{LL} = \frac{1}{2}(M_{1Lane} + M_{2Lane})$ $M_{LL} = 22.75 \text{ ftk}$

$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF_{Lane}$ $M_{LL_I_Lane} = 23.862 \text{ ftk}$

$V_{LL} = \frac{1}{2}(V_{1Lane} + V_{2Lane})$ $V_{LL} = 14.4 \text{ k}$

$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF_{Lane}$ $V_{LL_I_Lane} = 15.104 \text{ k}$

HS-20 Maximum moment occur when wheel line load is applied at midspan. Maximum shear occur when wheel line load is applied at the end.

$P = 16 \text{ k}$

$M_{LL} = \frac{P \times L}{4}$ $M_{LL} = 35 \text{ ftk}$

$M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$ $M_{LL_I_HS20} = 36.71 \text{ ftk}$

$V_{LL} = P$ $V_{LL} = 16 \text{ k}$

$V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$ $V_{LL_I_HS20} = 16.782 \text{ k}$

H-20 Maximum moment occur when wheel line load is applied at midspan. Maximum shear occur when wheel line load is applied at the end.

$P = 16 \text{ k}$

$M_{LL} = \frac{P \times L}{4}$ $M_{LL} = 35 \text{ ftk}$

$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$ $M_{LL_I_HS20} = 36.71 \text{ ftk}$

$V_{LL} = P$ $V_{LL} = 16 \text{ k}$

$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$ $V_{LL_I_HS20} = 16.782 \text{ k}$

Type-3 Maximum moment occur when wheel line load is applied at midspan
Maximum shear occur when one wheel line load is applied at the end.

$P = 8.5 \text{ k}$

$M_{LL} = \frac{P \times L}{4}$ $M_{LL} = 18.594 \text{ ftk}$

$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$ $M_{LL_I_Type3} = 19.502 \text{ ftk}$

$V_{LL} = 8.5 \text{ k} + 8.5 \text{ k} \times \frac{L - 4 \text{ ft}}{L}$ $V_{LL} = 13.114 \text{ k}$

$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$ $V_{LL_I_Type3} = 13.755 \text{ k}$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb and parapet equally distributed to all girders/stringers.

Steel: $w_b = w_{\text{steel}} \times A_b$ $w_b = 0.03 \frac{k}{ft}$

Slab: $w_s = w_{\text{concrete}} \times t_s \times \left[\frac{(4ft + 10.5in) + 4ft}{2} \right]$ $w_s = 0.444 \frac{k}{ft}$

Overlay: $w_o = w_{\text{concrete}} \times \frac{(4ft + 10.5in) + 4ft}{2} \times 1.89in$ $w_o = 0.105 \frac{k}{ft}$

Total Dead Load = sum w + add 5%

$DL = (w_b + w_s + w_o) \times 1.05$ $DL = 0.608 \frac{k}{ft}$

Uniform Load:

$M_{DL} = \frac{DL \times L^2}{8}$ $M_{DL} = 5.819 \text{ ftk}$

$V_{DL} = \frac{1}{2} \times DL \times L$ $V_{DL} = 2.66 \text{ k}$

Capacities:

$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s$ $C_1 = 535.5 \text{ k}$ (10-123)

$C_2 = A_b \times F_y$ $C_2 = 295.518 \text{ k}$ (10-124)

$C = \min \left(\left(\begin{matrix} C_1 \\ C_2 \end{matrix} \right) \right)$ Compressive force in slab $C = 295.518 \text{ k}$

$a = \frac{C}{0.85 \times f_c \times b_{\text{eff}}}$ Depth of stressblock $a = 4.415 \text{ in}$ (10-125)

a is distance from top of slab down to plastic NA

$AF_{tf} = A_{tf} \times F_y$ top flange $AF_{tf} = 103.494 \text{ k}$

$AF_w = A_w \times F_y$ web above welded plate $AF_w = 88.53 \text{ k}$

$AF_{bf} = AF_{tf}$ bottom flange $AF_{bf} = 103.494 \text{ k}$

Check compact:

$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$ Dcp is depth of web in compression.
Since plastic neutral axis lies in slab => OK! (10-129)

Check (10-129a):

$\frac{D_p}{D_{\text{prime}}} \leq 5$ (10-129a)

$D_p = a$ Distance from top of slab to PNA $D_p = 4.415 \text{ in}$

$D_{\text{prime}} = 0.9 \times \frac{d + t_s}{7.5}$ $D_{\text{prime}} = 2.16 \text{ in}$

$\frac{D_p}{D_{\text{prime}}} = 2.044$ OK!

Since $D_{prime} < D_p < 5D_{prime} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad (10-129c)$$

Slab: $C = 295.518 \text{ k}$ $d_c = \frac{a}{2}$ $d_c = 2.207 \text{ in}$

Top flange: $AF_{tf} = 103.494 \text{ k}$ $d_{tf} = t_s - a + \frac{t_{tf}}{2}$ $d_{tf} = 3.922 \text{ in}$

Web: $AF_w = 88.53 \text{ k}$ $d_w = t_s - a + t_{tf} + \frac{t_w}{2}$ $d_w = 4.413 \text{ in}$

Bottom flange: $AF_{bf} = 103.494 \text{ k}$ $d_{bf} = d + t_s - a - \frac{t_{tf}}{2}$ $d_{bf} = 13.249 \text{ in}$

$$M_p = C \times d_c + AF_{tf} \times d_{tf} + AF_w \times d_w + AF_{bf} \times d_{bf} \quad M_p = 235.005 \text{ ftk}$$

Yield moment:

$$I_9 = 701 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - Ecc \quad \text{Distance from bottom of steel to elastic NA} \quad Y = 11.84 \text{ in}$$

$$M_y = F_y \times \frac{I_9}{Y} \quad M_y = 162.817 \text{ ftk}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad M_n = 209.792 \text{ ftk}$$

$$M_n = 2.517 \times 10^3 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$K = 5$ For unstiffened beams and girders

$D = 8.654 \text{ in}$ Clear distance between flanges

$t_w = 0.31 \text{ in}$ Web thickness

$$\frac{D}{t_w} = 27.916 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 51.348 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 51.348 \text{ k} \quad (10-113)$$

Rating:Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$ Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 3.906
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 6.519
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 1.461
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 2.439
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 2.539
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 4.237
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 1.315
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 2.195
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.539
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 4.237
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 1.315
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 2.195
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 4.779
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 7.976
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 1.604
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 2.678

RATING FOR FLOORBEAMSUnits:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of concrete}$$

$$f_c = 3\text{ksi} \quad \text{Concrete strength}$$

$$F_y = 33\text{ksi} \quad \text{Steel strength}$$

28" Beth I 113Input:

$$A_{\text{tf}} = 10.03\text{in} \times 1.135\text{in} \quad \text{Area of top flange} \quad A_{\text{tf}} = 11.384 \text{ in}^2$$

$$A_w = 25.85\text{in} \times 0.54\text{in} \quad \text{Area of web} \quad A_w = 13.959 \text{ in}^2$$

$$A_{\text{bf}} = 10.03\text{in} \times 1.135\text{in} \quad \text{Area of bottom flange} \quad A_{\text{bf}} = 11.384 \text{ in}^2$$

$$t_{\text{tf}} = 1.135\text{in} \quad \text{Thickness of top flange}$$

$$b_w = 25.85\text{in} \quad \text{Width of web}$$

$$t_{\text{bf}} = 1.135\text{in} \quad \text{Thickness of bottom flange}$$

$$t_w = 0.54\text{in} \quad \text{Thickness of web}$$

Live Load Distribution Factor:

$$S_b = 17.5\text{ft} \quad \text{Average floorbeam spacing in ft} \quad S_b = 17.5\text{ft} \quad \text{table 3.23.3.1}$$

$$DF = \frac{S_b}{5.5\text{ft}} \quad DF = 3.182$$

However, since $DF > 1$, see f in 3.23.3.2 => Flooring between the beams acts as a simple beam
=> $DF = 1$

Section Properties:

$$I_9 = 11444\text{in}^4 \quad \text{Moment of inertia for elastic section (from Excel)}$$

$$Ecc = 6.54\text{in} \quad \text{Distance from c.g. slab to c.g elastic composit section (from Excel)}$$

$$L = 21.75\text{ft} \quad \text{Design span of beam (distance between main girders)}$$

$$t_s = 8\text{in} \quad \text{Thickness of concrete slab}$$

$$A_b = A_{\text{tf}} + A_w + A_{\text{bf}} \quad A_b = 36.727 \text{ in}^2$$

$$d = t_{\text{tf}} + b_w + t_{\text{bf}} \quad \text{Total depth of steel} \quad d = 28.12\text{in}$$

$$D = b_w \quad \text{Clear distance between flanges} \quad D = 25.85\text{in}$$

$$b_{\text{eff}} = \min \left[\begin{array}{c} \frac{1}{4} \times L \\ \frac{1}{2} \times (17.5 \text{ ft} + 17.5 \text{ ft}) \\ 12.t_s \end{array} \right] \quad b_{\text{eff}} = 65.25 \text{ in} \quad 10.38.3.1$$

Girder Loads:

$$I = \begin{cases} \frac{50 \text{ ft}}{L + 125 \text{ ft}} & \text{if } \frac{50 \text{ ft}}{L + 125 \text{ ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.3 \quad 3.8.2.1$$

Loads for Lane Loading

$P_s = 26 \text{ k}$ Point Load for Shear for Lane Loading fig. 3.7.6.b

$P_m = 18 \text{ k}$ Point Load for Moment for Lane Loading

$\omega = 0.64 \frac{\text{k}}{\text{ft}}$ Uniform Load for Lane Loading

Maximum Live Load Moments:

Lane Load **For moment:** the uniform lane load of 0.640 lb/ft is placed at the center of the floorbeam with 2x10 ft width. The point load of 18 k is placed at midspan to obtain critical values. 3.6.1
Assume ends are 25% fixed. FEM are fixed end moments. 3.6.3

$a = 20 \text{ ft}$	Width of uniform lane load	$a = 20 \text{ ft}$
$b = 0.875 \text{ ft}$	Distance from uniform lane load to end of floorbeam	$b = 0.875 \text{ ft}$
$\text{FEM} = \frac{\omega \times a^2}{6} \times \left(2 + \frac{b}{L} \right) + \frac{P_m \times L}{8}$		$\text{FEM} = 135.987 \text{ ftk}$
$M_{\text{end}} = \frac{\text{FEM}}{4}$		$M_{\text{end}} = 33.997 \text{ ftk}$
$M_{\text{max}} = -M_{\text{end}} + \frac{\omega \times a}{8} \times (L + 2 \times b) + \frac{P_m \times L}{4}$		$M_{\text{max}} = 101.478 \text{ ftk}$
$M_{\text{LL}_1 \text{ Lane}} = M_{\text{max}} \times (1 + I) \times \text{DF}$		$M_{\text{LL}_1 \text{ Lane}} = 131.922 \text{ ftk}$

For shear: the uniform lane load is placed at the left end, and the point load is placed at the same end.

$b = 1.75 \text{ ft}$	Distance from uniform load to the right end	$b = 1.75 \text{ ft}$
$\text{FEM}_{\text{left}} = \frac{\omega \times a^2}{12} \times \left[1 + 2 \times \frac{b}{L} + 3 \times \left(\frac{b}{L} \right)^2 \right]$		$\text{FEM}_{\text{left}} = 25.181 \text{ ftk}$
$M_{\text{left}} = \frac{\text{FEM}_{\text{left}}}{4}$		$M_{\text{left}} = 6.295 \text{ ftk}$
$\text{FEM}_{\text{right}} = \frac{\omega \times a^2}{12} \times \left[\frac{a}{L} \times \left(1 + 3 \times \frac{b}{L} \right) \right]$		$\text{FEM}_{\text{right}} = 24.352 \text{ ftk}$

$$M_{\text{right}} = \frac{FEM_{\text{right}}}{4}$$

$$M_{\text{right}} = 6.088 \text{ ftk}$$

$$V_{\text{max}} = \frac{\omega \times a}{2} \times \left(1 + \frac{b}{L}\right) + P_s - \frac{M_{\text{right}} - M_{\text{left}}}{L}$$

$$V_{\text{max}} = 32.924 \text{ k}$$

$$V_{LL_I_Lane} = V_{\text{max}} \times (1 + I) \times DF$$

$$V_{LL_I_Lane} = 42.802 \text{ k}$$

HS-20

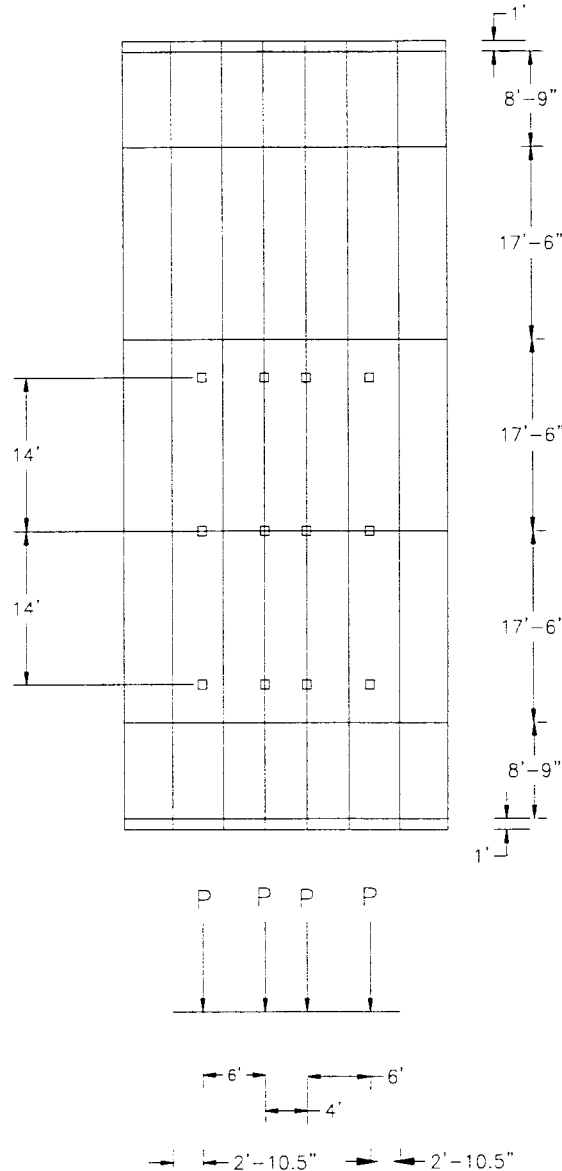


Figure D.4. Location of two HS-20 trucks on 28" Beth I 113.

Maximum Load on Floorbeam 28 Beth I 113 per wheel line. Units in kips and feet

$$P = 4k \times \frac{17.5\text{ft} - 14\text{ft}}{17.5\text{ft}} + 16k \times (1) + 16k \times \frac{17.5\text{ft} - 14\text{ft}}{17.5\text{ft}} \quad P = 20k$$

Design length of span is the distance between the main girders = 21.75 ft.

Moments at floorbeam due to outside wheel line located 2.875 ft from the main girder for both trucks as shown above.

For shear, the location of the outside wheel line for one truck is on the girder.

Spacing is 4 ft both for moment and for shear.

Due to symmetry of loads => moments and shears are symmetric

If beam is 100 % fixed, due to both trucks

FEM due to first truck on floor beam.

$$M_{A_100\%-1} = \frac{P \times a \times b^2}{L^2} + \frac{P \times a \times b^2}{L^2} = \frac{P \times 2.875 \times 18.875^2}{21.75^2} + \frac{P \times 8.875 \times 12.875^2}{21.75^2} = 5.275P$$

FEM due to second truck on floor beam.

$$M_{A_100\%-2} = \frac{P \times a \times b^2}{L^2} + \frac{P \times a \times b^2}{L^2} = \frac{P \times 12.875 \times 8.875^2}{21.75^2} + \frac{P \times 18.875 \times 2.875^2}{21.75^2} = 2.474P$$

FEM due to both trucks on floor beam.

$$M_{A_100\%} = M_{A_100\%-1} + M_{A_100\%-2} = 5.275P + 2.474P = 7.749 \times P$$

$$M_{B_100\%} = M_{A_100\%} = 7.749 \times P$$

Assume 25% fixed

$$M_A = \frac{M_{A_100\%}}{4} = \frac{7.749 \times P}{4} = 1.937 \times P$$

$$M_B = \frac{M_{B_100\%}}{4} = \frac{7.749 \times P}{4} = 1.937 \times P$$

$$R_A = R_B = 2 \times P$$

Max moment occur at wheel line second closest to A

$$M_{\max} = -M_A + R_A \times 2.875 + (R_A - P) \times 6 = -1.937 \times P + 2 \times P \times 2.875 + (2P - P) \times 6 = 9.813 \times P$$

$$M_{\max} = 9.813 \text{ ft} \times P$$

$$M_{\max} = 196.26 \text{ ftk}$$

Max shear occur at one end (at A)

If beam is 100 % fixed, due to both trucks

$$M_{A_100\%-1} = \frac{P \times a \times b^2}{L^2} + \frac{P \times a \times b^2}{L^2} = 0 + \frac{P \times 6 \times 15.75^2}{21.75^2} = 3.146P$$

Truck 1

$$M_{A_100\%-2} = \frac{P \times a \times b^2}{L^2} + \frac{P \times a \times b^2}{L^2} = \frac{P \times 10 \times 11.75^2}{21.75^2} + \frac{P \times 16 \times 5.75^2}{21.75^2} = 4.037P$$

Truck 2

$$M_{A_100\%} = M_{A_100\%-1} + M_{A_100\%-2} = 3.146P + 4.037P = 7.183 \times P$$

$$M_{B_100\%-1} = \frac{P \times a^2 \times b}{L^2} + \frac{P \times a^2 \times b}{L^2} = 0 + \frac{P \times 6^2 \times 15.75}{21.75^2} = 1.199P$$

Truck 1

$$M_{B_100\%-2} = \frac{P \times a^2 \times b}{L^2} + \frac{P \times a^2 \times b}{L^2} = \frac{P \times 10^2 \times 11.75}{21.75^2} + \frac{P \times 16^2 \times 5.75}{21.75^2} = 5.595P$$

Truck 2

$$M_{B_100\%} = M_{B_100\%-1} + M_{B_100\%-2} = 1.199P + 5.595P = 6.794 \times P$$

Assume 25% fixed

$$M_A = \frac{M_{A_{100\%}}}{4} = \frac{7.183 \times P}{4} = 1.796 \times P$$

$$M_B = \frac{M_{B_{100\%}}}{4} = \frac{6.794 \times P}{4} = 1.698 \times P$$

$$R_A = \left(P + \frac{21.75 - 6}{21.75} \times P + \frac{21.75 - 10}{21.75} \times P + \frac{21.75 - 16}{21.75} \times P \right) - \frac{M_B - M_A}{L}$$

$$R_A = 2.529 \times P - \frac{1.698 \times P - 1.796 \times P}{21.75} = 2.534 \times P$$

Max shear

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 50.68 \text{ k}$$

Design Loads:

$$M_{\text{HS20}} = M_{\max}$$

$$M_{\text{HS20}} = 196.26 \text{ ft-k}$$

$$V_{\text{HS20}} = V_{\max}$$

$$V_{\text{HS20}} = 50.68 \text{ k}$$

All values are lane loads.

$$M_{\text{LL}} = M_{\text{HS20}}$$

$$M_{\text{LL}} = 196.26 \text{ ft-k}$$

$$M_{\text{LL}_I_{\text{HS20}}} = M_{\text{LL}} \times (1 + I) \times \text{DF}$$

$$M_{\text{LL}_I_{\text{HS20}}} = 255.138 \text{ ft-k}$$

$$V_{\text{LL}} = V_{\text{HS20}}$$

$$V_{\text{LL}} = 50.68 \text{ k}$$

$$V_{\text{LL}_I_{\text{HS20}}} = V_{\text{LL}} \times (1 + I) \times \text{DF}$$

$$V_{\text{LL}_I_{\text{HS20}}} = 65.884 \text{ k}$$

H-20

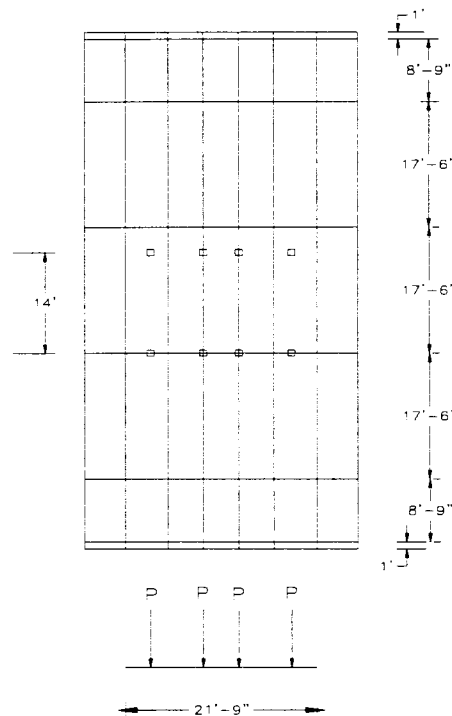


Figure D.5. Location of two H-20 trucks on 28" Beth I 113.

Maximum Load on Floorbeam 28 Beth I 113

$$P = 4k \times \left(\frac{17.5\text{ft} - 14\text{ft}}{17.5\text{ft}} \right) + 16k \times (1)$$

$$P = 16.8 \text{ k}$$

Same calculations as above

$$M_{\max} = 9.813\text{ft} \times P$$

$$M_{\max} = 164.858 \text{ ftk}$$

$$M_{H20} = M_{\max}$$

$$M_{H20} = 164.858 \text{ ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 42.571 \text{ k}$$

$$V_{H20} = V_{\max}$$

$$V_{H20} = 42.571 \text{ k}$$

All values are lane loads.

$$M_{LL} = M_{H20}$$

$$M_{LL} = 164.858 \text{ ftk}$$

$$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_H20} = 214.316 \text{ ftk}$$

$$V_{LL} = V_{H20}$$

$$V_{LL} = 42.571 \text{ k}$$

$$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_H20} = 55.343 \text{ k}$$

Type 3

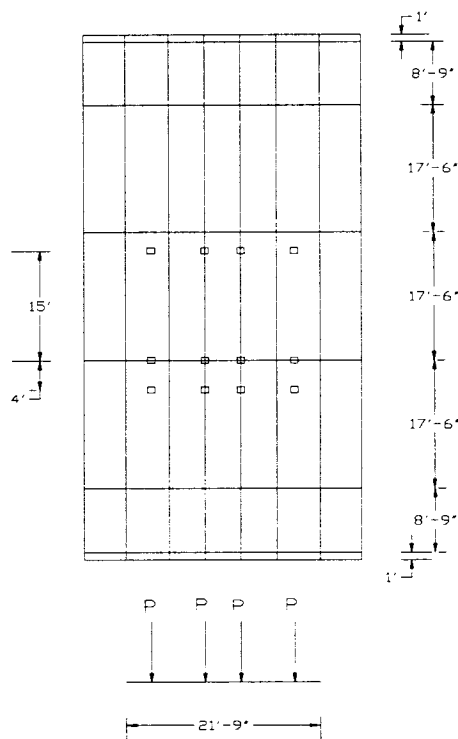


Figure D.6. Location of two Type-3 trucks on 28" Beth I 113.

Maximum Load on Floorbeam 28 Beth I 113

$$P = 8.5k \times \left(\frac{17.5\text{ft} - 4\text{ft}}{17.5\text{ft}} \right) + 8.5k \times (1) + 8k \times \left(\frac{17.5\text{ft} - 15\text{ft}}{17.5\text{ft}} \right) \quad P = 16.2 \text{ k}$$

Same calculations as above

$$M_{\max} = 9.813 \text{ ft} \times P$$

$$M_{\max} = 158.971 \text{ ftk}$$

$$M_{\text{Type3}} = M_{\max}$$

$$M_{\text{Type3}} = 158.971 \text{ ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 41.051 \text{ k}$$

$$V_{\text{Type3}} = V_{\max}$$

$$V_{\text{Type3}} = 41.051 \text{ k}$$

All values are lane loads.

$$M_{LL} = M_{\text{Type3}}$$

$$M_{LL} = 158.971 \text{ ftk}$$

$$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_Type3} = 206.662 \text{ ftk}$$

$$V_{LL} = V_{\text{Type3}}$$

$$V_{LL} = 41.051 \text{ k}$$

$$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_Type3} = 53.366 \text{ k}$$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb and parapet equally distributed to all girders/stringers.

Steel: $w_b = w_{\text{steel}} \times A_b$

$$w_b = 0.125 \frac{\text{k}}{\text{ft}}$$

Stringers: $w_{st} = \frac{w_{\text{steel}} \times 12.49 \text{ in}^2 \times 17.5 \text{ ft} \times 4}{21.75 \text{ ft}}$

$$w_{st} = 0.137 \frac{\text{k}}{\text{ft}}$$

Slab: $w_s = w_{\text{concrete}} \times t_s \times (17.5 \text{ ft})$

$$w_s = 1.75 \frac{\text{k}}{\text{ft}}$$

Overlay: $w_o = w_{\text{concrete}} \times 17.5 \text{ ft} \times 1.89 \text{ in}$

$$w_o = 0.413 \frac{\text{k}}{\text{ft}}$$

Total Dead Load = sum w + add 5%

$$DL = (w_b + w_{st} + w_s + w_o) \times 1.05$$

$$DL = 2.546 \frac{\text{k}}{\text{ft}}$$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8}$$

$$M_{DL} = 150.575 \text{ ftk}$$

$$V_{DL} = \frac{1}{2} \times DL \times L$$

$$V_{DL} = 27.692 \text{ k}$$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s$$

$$C_1 = 1.331 \times 10^3 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y$$

$$C_2 = 1.212 \times 10^3 \text{ k} \quad (10-124)$$

$$C = \min \left(\left(\begin{array}{c} C_1 \\ C_2 \end{array} \right) \right) \quad \text{Compressive force in slab}$$

$$C = 1.212 \times 10^3 \text{ k}$$

$$a = \frac{C}{0.85 \times f_c \times b_{\text{eff}}} \quad \text{Depth of stressblock} \quad a = 7.284 \text{ in} \quad (10-125)$$

a is distance from top of slab down to plastic NA

Check compact:

$$\frac{2 \times D_{\text{cp}}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \begin{array}{l} D_{\text{cp}} \text{ is depth of web in comprssion} \\ \text{Since PNA lies in slab} \Rightarrow \text{OK!} \end{array} \quad (10-129)$$

Check (10-129a):

$$\frac{D_p}{D_{\text{prime}}} \leq 5 \quad (10-129a)$$

$$D_p = a \quad \text{Distance from top of slab to PNA} \quad D_p = 7.284 \text{ in}$$

$$D_{\text{prime}} = 0.9 \times \frac{d + t_s}{7.5} \quad D_{\text{prime}} = 4.334 \text{ in}$$

$$\frac{D_p}{D_{\text{prime}}} = 1.681 \quad \text{OK!}$$

Since $D_{\text{prime}} < D_p < 5D_{\text{prime}} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{\text{prime}}} \quad (10-129c)$$

$$\begin{array}{ll} \text{Slab:} & C = 1.212 \times 10^3 \text{ k} \\ & d_c = \frac{a}{2} \\ & d_c = 3.642 \text{ in} \end{array}$$

$$\begin{array}{ll} \text{Top flange:} & AF_{\text{tf}} = A_{\text{tf}} \times F_v \\ & d_{\text{tf}} = t_s - a + \frac{t_{\text{tf}}}{2} \\ & AF_{\text{tf}} = 375.674 \text{ k} \\ & d_{\text{tf}} = 1.283 \text{ in} \end{array}$$

$$\begin{array}{ll} \text{Web :} & AF_w = A_w \times F_v \\ & d_w = t_s - a + t_{\text{tf}} + \frac{t_w}{2} \\ & AF_w = 460.647 \text{ k} \\ & d_w = 2.121 \text{ in} \end{array}$$

$$\begin{array}{ll} \text{Bottom flange:} & AF_{\text{bf}} = AF_{\text{tf}} \\ & d_{\text{bf}} = d + t_s - a - \frac{t_{\text{tf}}}{2} \\ & AF_{\text{bf}} = 375.674 \text{ k} \\ & d_{\text{bf}} = 28.268 \text{ in} \end{array}$$

$$M_p = C \times d_c + AF_{\text{tf}} \times d_{\text{tf}} + AF_w \times d_w + AF_{\text{bf}} \times d_{\text{bf}}$$

$$M_p = 1.374 \times 10^3 \text{ ftk}$$

Yield moment:

$$I_9 = 1.144 \times 10^4 \text{ in}^4 \quad \text{Moment of intertia for composite section}$$

$$Y = d + \frac{t_s}{2} - \text{Ecc} \quad \text{Distance from bottom of steel to elastic NA} \quad Y = 25.58 \text{ in}$$

$$M_y = F_y \times \frac{I_9}{Y} \quad M_y = 1.23 \times 10^3 \text{ ftk}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}}$$

$$M_n = 1.318 \times 10^3 \text{ ftk}$$

$$M_n = 1.582 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

K = 5 For unstiffened beams and girders

D = 25.85 in Clear distance between flanges

t_w = 0.54 in Web thickness

$$\frac{D}{t_w} = 47.87 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 267.175 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 267.175 \text{ k} \quad (10-113)$$

Rating:

Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$

Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

Lane Flexure: Inventory: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$ $RF = 3.922$

Operating: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$ $RF = 6.547$

Shear: Inventory: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$ $RF = 2.489$

Operating: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$ $RF = 4.155$

HS-20 Flexure: Inventory: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$ $RF = 2.028$

Operating: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$ $RF = 3.385$

Shear: Inventory: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$ $RF = 1.617$

Operating: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$ $RF = 2.699$

H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.414
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 4.03
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 1.925
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 3.213
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 2.504
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 4.179
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 1.996
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 3.332

27" Beth I 100Input:

$A_{tf} = 9.98\text{in} \times 1.015\text{in}$	Area of top flange	$A_{tf} = 10.13\text{in}^2$
$A_w = 25.85\text{in} \times 0.49\text{in}$	Area of web	$A_w = 12.666\text{in}^2$
$A_{bf} = 9.98\text{in} \times 1.015\text{in}$	Area of bottom flange	$A_{bf} = 10.13\text{in}^2$
$t_{tf} = 1.015\text{in}$	Thickness of top flange	
$b_w = 25.85\text{in}$	Width of web	
$t_{bf} = 1.015\text{in}$	Thickness of bottom flange	
$t_w = 0.49\text{in}$	Thickness of web	

Live Load Distribution Factor:

$S_b = 17.5\text{ft}$	Average floorbeam spacing in ft	$S_b = 17.5\text{ft}$	table 3.23.3.1
$DF = \frac{S_b}{5.5\text{ft}}$		DF = 3.182	

However, since $DF > 1$, see f in 3.23.3.2

=> Flooring between the beams acts as a simple beam.

DF = 1

Section Properties:

$I_g = 10281\text{in}^4$	Moment of inertia for elastic section (from Excel)
Ecc = 6.0in	Distance from c.g. slab to c.g. elastic composit section (from Excel)
L = 21.75ft	Design span of beam
$t_s = 8\text{in}$	Thickness of concrete slab

$$A_b = A_{tf} + A_w + A_{bf}$$

$$A_b = 32.926 \text{ in}^2$$

$$d = t_{tf} + b_w + t_{bf} \quad \text{Total depth of steel}$$

$$d = 27.88 \text{ in}$$

$$D = b_w \quad \text{Clear distance between flanges}$$

$$D = 25.85 \text{ in}$$

$$b_{\text{eff}} = \min \left[\begin{array}{l} \frac{1}{4} \times L \\ \frac{1}{2} \times (17.5\text{ft} + 8.75\text{ft}) \\ 12 \times t_s \end{array} \right]$$

$$b_{\text{eff}} = 65.25 \text{ in}$$

10.38.3.1

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases}$$

Impact

$$I = 0.3$$

3.8.2.1

Maximum Live Load Moments:

Lane Same live load moments as previously calculated

Load

$$M_{LL_I_Lane} = 131.922 \text{ ft-k}$$

$$V_{LL_I_Lane} = 42.802 \text{ k}$$

HS-20

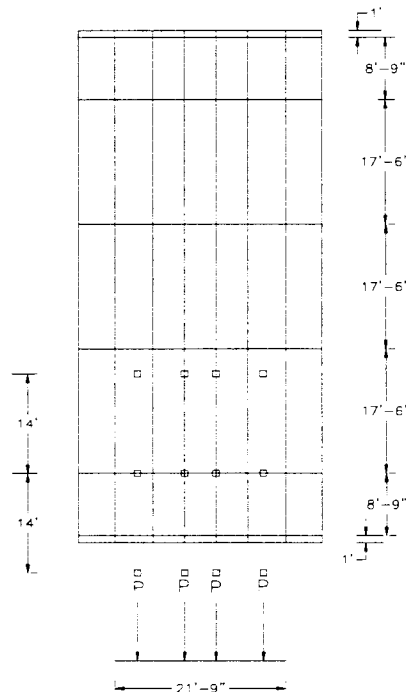


Figure D.7. Location of two HS-20 trucks on 27" Beth I 100.

Maximum Load on Floorbeam 27 Beth I 100

$$P = 4\text{k} \times (0) + 16\text{k} \times (1) + 16\text{k} \times \left(\frac{17.5\text{ft} - 14\text{ft}}{17.5\text{ft}} \right)$$

$$P = 19.2 \text{ k}$$

Same calculations as above

$$M_{\max} = 9.813 \text{ ft} \times P$$

$$M_{\max} = 188.41 \text{ ftk}$$

$$M_{\text{HS20}} = M_{\max}$$

$$M_{\text{HS20}} = 188.41 \text{ ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 48.653 \text{ k}$$

$$V_{\text{HS20}} = V_{\max}$$

$$V_{\text{HS20}} = 48.653 \text{ k}$$

All values are lane loads.

$$M_{\text{LL}} = M_{\text{HS20}}$$

$$M_{\text{LL}} = 188.41 \text{ ftk}$$

$$M_{\text{LL}_I_{\text{HS20}}} = M_{\text{LL}} \times (1 + I) \times \text{DF}$$

$$M_{\text{LL}_I_{\text{HS20}}} = 244.932 \text{ ftk}$$

$$V_{\text{LL}} = V_{\text{HS20}}$$

$$V_{\text{LL}} = 48.653 \text{ k}$$

$$V_{\text{LL}_I_{\text{HS20}}} = V_{\text{LL}} \times (1 + I) \times \text{DF}$$

$$V_{\text{LL}_I_{\text{HS20}}} = 63.249 \text{ k}$$

H-20

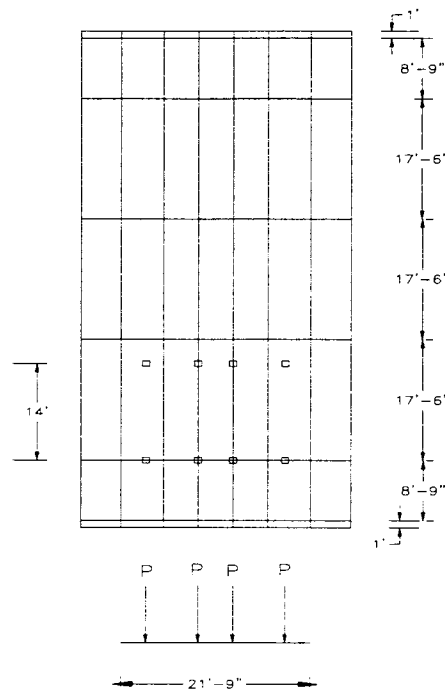


Figure D.8. Location of two H-20 trucks on 27" Beth I 100.

Maximum Load on Floorbeam 27 Beth I 100

$$P = 16 \text{ k} \times (1) + 4 \text{ k} \times \left(\frac{17.5 \text{ ft} - 14 \text{ ft}}{17.5 \text{ ft}} \right)$$

$$P = 16.8 \text{ k}$$

Same calculations as above

$$M_{\max} = 9.813 \text{ ft} \times P$$

$$M_{\max} = 164.858 \text{ ftk}$$

$$M_{\text{H20}} = M_{\max}$$

$$M_{\text{H20}} = 164.858 \text{ ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 42.571 \text{ k}$$

$$V_{H20} = V_{\max}$$

$$V_{H20} = 42.571 \text{ k}$$

All values are lane loads.

$$M_{LL} = M_{H20}$$

$$M_{LL} = 164.858 \text{ ftk}$$

$$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_H20} = 214.316 \text{ ftk}$$

$$V_{LL} = V_{H20}$$

$$V_{LL} = 42.571 \text{ k}$$

$$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_H20} = 55.343 \text{ k}$$

Type 3

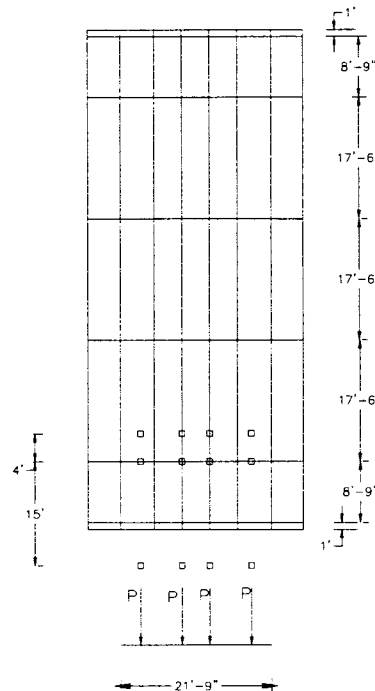


Figure D.9. Location of two Type-3 trucks on 27" Beth I 100.

Maximum Load on Floorbeam 27 Beth I 100

$$P = 8k \times (0) + 8.5k \times (1) + 8.5k \times \left(\frac{17.5\text{ft} - 4\text{ft}}{17.5\text{ft}} \right)$$

$$P = 15.057 \text{ k}$$

Same calculations as above

$$M_{\max} = 9.813\text{ft} \times P$$

$$M_{\max} = 147.756 \text{ ftk}$$

$$M_{\text{Type3}} = M_{\max}$$

$$M_{\text{Type3}} = 147.756 \text{ ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 38.155 \text{ k}$$

$$V_{\text{Type3}} = V_{\max}$$

$$V_{\text{Type3}} = 38.155 \text{ k}$$

All values are lane loads.

$$M_{LL} = M_{Type3}$$

$$M_{LL} = 147.756 \text{ ftk}$$

$$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_Type3} = 192.082 \text{ ftk}$$

$$V_{LL} = V_{Type3}$$

$$V_{LL} = 38.155 \text{ k}$$

$$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_Type3} = 49.601 \text{ k}$$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb and parapet equally distributed to all girders/stringers.

Steel:	$w_b = w_{\text{steel}} \times A_b$	$w_b = 0.112 \frac{\text{k}}{\text{ft}}$
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Stringers:	$w_{st} = \frac{w_{\text{steel}} \times \left(12.49 \text{ in}^2 \times \frac{17.5 \text{ ft}}{2} + 7.38 \text{ in}^2 \times \frac{8.75 \text{ ft}}{2} \right) \times 4}{21.75 \text{ ft}}$	$w_{st} = 0.089 \frac{\text{k}}{\text{ft}}$
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Slab:	$w_s = w_{\text{concrete}} \times t_s \times (13.125 \text{ ft})$	$w_s = 1.313 \frac{\text{k}}{\text{ft}}$
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Overlay:	$w_o = w_{\text{concrete}} \times 13.125 \text{ ft} \times 1.89 \text{ in}$	$w_o = 0.31 \frac{\text{k}}{\text{ft}}$
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Total Dead Load = sum w + add 5%

$DL = (w_b + w_{st} + w_s + w_o) \times 1.05$	$DL = 1.914 \frac{\text{k}}{\text{ft}}$
---	---

Uniform Load:

$M_{DL} = \frac{DL \times L^2}{8}$	$M_{DL} = 113.2 \text{ ftk}$
------------------------------------	------------------------------

$V_{DL} = \frac{1}{2} \times DL \times L$	$V_{DL} = 20.818 \text{ k}$
---	-----------------------------

Capacities:

$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s$	$C_1 = 1.331 \times 10^3 \text{ k} \quad (10-123)$
--	--

$C_2 = A_b \times F_y$	$C_2 = 1.087 \times 10^3 \text{ k} \quad (10-124)$
------------------------	--

$C = \min \left(\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} \right)$	Compressive force in slab	$C = 1.087 \times 10^3 \text{ k}$
--	---------------------------	-----------------------------------

$a = \frac{C}{0.85 \times f_c \times b_{\text{eff}}}$	Depth of stressblock	$a = 6.53 \text{ in} \quad (10-125)$
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a is distance from top of slab down to plastic NA

$AF_{tf} = A_{tf} \times F_y$	top flange	$AF_{tf} = 334.28 \text{ k}$
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$AF_w = A_w \times F_y$	web above welded plate	$AF_w = 417.995 \text{ k}$
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$AF_{bf} = AF_{tf}$	bottom flange	$AF_{bf} = 334.28 \text{ k}$
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Check compact:

$$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \begin{array}{l} D_{cp} \text{ is depth of web in compression} \\ \text{Since PNA lies in slab} \Rightarrow \text{OK!} \end{array} \quad (10-129)$$

Check (10-129a):

$$\frac{D_p}{D_{prime}} \leq 5 \quad (10-129a)$$

$$D_p = a \quad \text{Distance from top of slab to PNA} \quad D_p = 6.53 \text{ in}$$

$$D_{prime} = 0.9 \times \frac{d + t_s}{7.5} \quad D_{prime} = 4.306 \text{ in}$$

$$\frac{D_p}{D_{prime}} = 1.517 \quad \text{OK!}$$

Since $D_{prime} < D_p < 5D_{prime} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad (10-129c)$$

$$\text{Slab:} \quad C = 1.087 \times 10^3 \text{ k} \quad d_c = \frac{a}{2} \quad d_c = 3.265 \text{ in}$$

$$\text{Top flange:} \quad AF_{tf} = 334.28 \text{ k} \quad d_{tf} = t_s - a + \frac{t_{tf}}{2} \quad d_{tf} = 1.977 \text{ in}$$

$$\text{Web:} \quad AF_w = 417.995 \text{ k} \quad d_w = t_s - a + t_{tf} + \frac{t_w}{2} \quad d_w = 2.73 \text{ in}$$

$$\text{Bottom flange:} \quad AF_{bf} = 334.28 \text{ k} \quad d_{bf} = d + t_s - a - \frac{t_{tf}}{2} \quad d_{bf} = 28.842 \text{ in}$$

$$M_p = C \times d_c + AF_{tf} \times d_{tf} + AF_w \times d_w + AF_{bf} \times d_{bf} \quad M_p = 1.249 \times 10^3 \text{ ft-k}$$

Yield moment:

$$I_g = 1.028 \times 10^4 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - \text{Ecc} \quad \text{Distance from bottom of steel to elastic NA} \quad Y = 25.88 \text{ in}$$

$$M_y = F_y \times \frac{I_g}{Y} \quad M_y = 1.092 \times 10^3 \text{ ft-k}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{prime}} \quad M_n = 1.208 \times 10^3 \text{ ft-k}$$

$$M_n = 1.449 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$K = 5$ For unstiffened beams and girders

$D = 25.85$ in Clear distance between flanges

$t_w = 0.49$ in Web thickness

$$\frac{D}{t_w} = 52.755 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 242.437 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 242.437 \text{ k} \quad (10-113)$$

Rating:

Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$

Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

Lane Load Flexure: Inventory: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$ $RF = 3.705$

Operating: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$ $RF = 6.185$

Shear: Inventory: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$ $RF = 2.319$

Operating: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$ $RF = 3.871$

HS-20 Flexure: Inventory: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$ $RF = 1.996$

Operating: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$ $RF = 3.331$

Shear: Inventory: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$ $RF = 1.569$

Operating: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$ $RF = 2.619$

H-20 Flexure: Inventory: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$ $RF = 2.281$

Operating: $RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$ $RF = 3.807$

Shear: Inventory: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$ $RF = 1.793$

Operating: $RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$ $RF = 2.994$

Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 2.545
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 4.248
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.001
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 3.34

25"8 Beth I 85.5Input:

$A_{tf} = 9.48\text{in} \times 0.922\text{in}$	Area of top flange	$A_{tf} = 8.741\text{in}^2$
$A_w = 24.04\text{in} \times 0.45\text{in}$	Area of web	$A_w = 10.818\text{in}^2$
$A_{bf} = 9.48\text{in} \times 0.922\text{in}$	Area of bottom flange	$A_{bf} = 8.741\text{in}^2$
$t_{tf} = 0.922\text{in}$		
$b_w = 24.04\text{in}$		
$t_{bf} = 0.922\text{in}$		
$t_w = 0.45\text{in}$		

Live Load Distribution Factor:

$S = \frac{1}{2} \times [(8\text{ft} + 9\text{in}) + 1\text{ft}]$	Average floorbeam spacing in ft	$S = 4.875\text{ft}$	table 3.23.3.1
$DF = \frac{S}{6\text{ft}}$		$DF = 0.813$	

Section Properties:

$I_g = 7549\text{in}^4$	Moment of inertia for elastic section (from Excel)		
$Ecc = 5.32\text{in}$	Distance from c.g. slab to c.g elastic composit section (from Excel)		
$L = 21.75\text{ft}$	Design span of beam		
$t_s = 8\text{in}$	Thickness of concrete slab		
$A_b = A_{tf} + A_w + A_{bf}$		$A_b = 28.299\text{in}^2$	
$d = t_{tf} + b_w + t_{bf}$	Total depth of steel	$d = 25.884\text{in}$	
$D = b_w$	Clear distance between flanges	$D = 24.04\text{in}$	
$b_{eff} = \min \left[\left[\frac{\frac{1}{4} \times L}{\frac{1}{2} \times [(8\text{ft} + 9\text{in}) + 1\text{ft}]} \right] \right]$		$b_{eff} = 58.5\text{in}$	10.38.3.1

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases}$$

Impact

$$I = 0.3$$

3.8.2.1

Maximum Live Load Moments:

HS-20

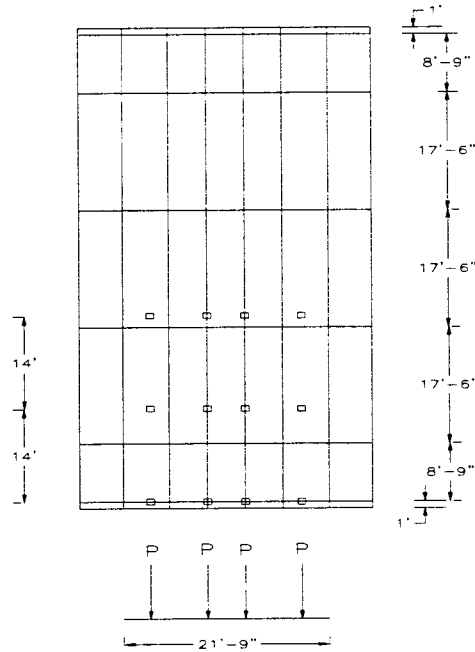


Figure D.10. Location of two HS-20 trucks on 25'8" Beth I 85.5.

Maximum Load on Floorbeam 27 Beth I 100

$$P = 4\text{k} \times (0) + 16\text{k} \times (0) + 16\text{k} \times (1)$$

$$P = 16\text{k}$$

Same calculations as above

$$M_{\max} = 9.813\text{ft} \times P$$

$$M_{\max} = 157.008\text{ftk}$$

$$M_{\text{HS20}} = M_{\max}$$

$$M_{\text{HS20}} = 157.008\text{ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 40.544\text{k}$$

$$V_{\text{HS20}} = V_{\max}$$

$$V_{\text{HS20}} = 40.544\text{k}$$

All values are lane loads.

$$M_{\text{LL}} = M_{\text{HS20}}$$

$$M_{\text{LL}} = 157.008\text{ftk}$$

$$M_{\text{LL}_I\text{HS20}} = M_{\text{LL}} \times (1 + I) \times \text{DF}$$

$$M_{\text{LL}_I\text{HS20}} = 165.84\text{ftk}$$

$$V_{\text{LL}} = V_{\text{HS20}}$$

$$V_{\text{LL}} = 40.544\text{k}$$

$$V_{\text{LL}_I\text{HS20}} = V_{\text{LL}} \times (1 + I) \times \text{DF}$$

$$V_{\text{LL}_I\text{HS20}} = 42.825\text{k}$$

H-20

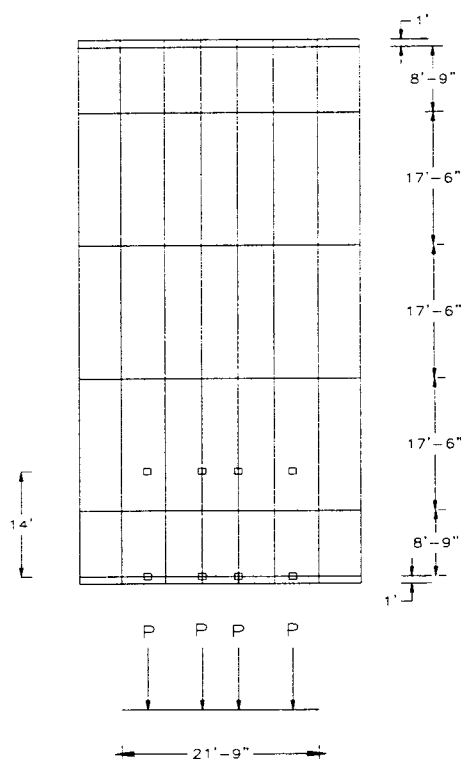


Figure D.11. Location of two H-20 trucks on 25'8 Beth I 85.5.

Maximum Load on Floorbeam 27 Beth I 100

$$P = 16k \times (1) + 4k \times (0)$$

$$P = 16k$$

Same calculations as above

$$M_{\max} = 9.813\text{ft} \times P$$

$$M_{\max} = 157.008\text{ftk}$$

$$M_{H20} = M_{\max}$$

$$M_{H20} = 157.008\text{ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 40.544\text{k}$$

$$V_{H20} = V_{\max}$$

$$V_{H20} = 40.544\text{k}$$

All values are lane loads.

$$M_{LL} = M_{H20}$$

$$M_{LL} = 157.008\text{ftk}$$

$$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_H20} = 165.84\text{ftk}$$

$$V_{LL} = V_{H20}$$

$$V_{LL} = 40.544\text{k}$$

$$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_H20} = 42.825\text{k}$$

Type 3

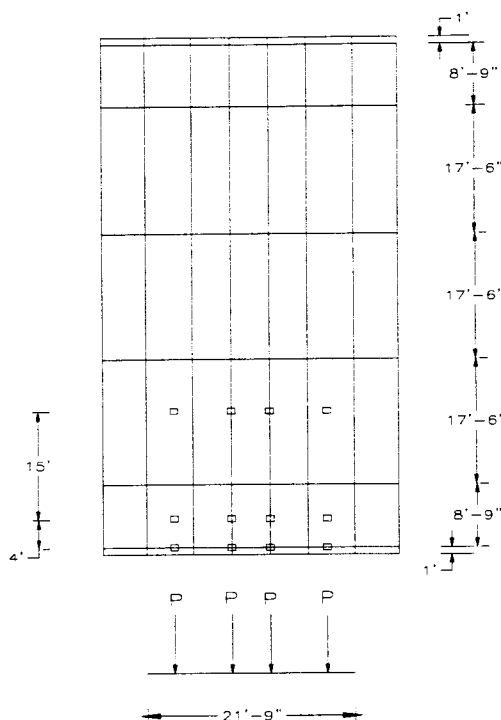


Figure D.12. Location of two Type-3 trucks on 25"8 Beth I 85.5.

Maximum Load on Floorbeam 27 Beth I 100

$$P = 8.5k \times (1) + 8.5k \times \left(\frac{8.75\text{ft} - 4\text{ft}}{8.75\text{ft}} \right) + 8k \times (0)$$

$$P = 13.114 \text{ k}$$

Same calculations as above

$$M_{\max} = 9.813\text{ft} \times P$$

$$M_{\max} = 128.69 \text{ ftk}$$

$$M_{\text{Type3}} = M_{\max}$$

$$M_{\text{Type3}} = 128.69 \text{ ftk}$$

Shear:

$$V_{\max} = 2.534 \times P$$

$$V_{\max} = 33.232 \text{ k}$$

$$V_{\text{Type3}} = V_{\max}$$

$$V_{\text{Type3}} = 33.232 \text{ k}$$

All values are lane loads.

$$M_{LL} = M_{\text{Type3}}$$

$$M_{LL} = 128.69 \text{ ftk}$$

$$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_Type3} = 135.929 \text{ ftk}$$

$$V_{LL} = V_{\text{Type3}}$$

$$V_{LL} = 33.232 \text{ k}$$

$$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_Type3} = 35.101 \text{ k}$$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb and parapet equally distributed to all girders/stringers.

$$\text{Steel:} \quad w_b = w_{\text{steel}} \times A_b \quad w_b = 0.096 \frac{\text{k}}{\text{ft}}$$

$$\text{Stringers:} \quad w_{st} = \frac{w_{\text{steel}} \left(7.38 \text{ in}^2 \times \frac{8.75 \text{ ft}}{2} \right) \times 4}{21.75 \text{ ft}} \quad w_{st} = 0.02 \frac{\text{k}}{\text{ft}}$$

$$\text{Slab:} \quad w_s = w_{\text{concrete}} \times t_s \times \left[\frac{1}{2} \times (8.75 \text{ ft} + 1 \text{ ft}) \right] \quad w_s = 0.488 \frac{\text{k}}{\text{ft}}$$

$$\text{Overlay:} \quad w_o = w_{\text{concrete}} \times \left[\frac{1}{2} \times (8.75 \text{ ft} + 1 \text{ ft}) \right] \times 1.89 \text{ in} \quad w_o = 0.115 \frac{\text{k}}{\text{ft}}$$

Total Dead Load = sum w + add 5%

$$DL = (w_b + w_{st} + w_s + w_o) \times 1.05 \quad DL = 0.755 \frac{\text{k}}{\text{ft}}$$

Uniform Load:

$$M_{DL} = \frac{DL \times L^2}{8} \quad M_{DL} = 44.651 \text{ ft-k}$$

$$V_{DL} = \frac{1}{2} \times DL \times L \quad V_{DL} = 8.212 \text{ k}$$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s \quad C_1 = 1.193 \times 10^3 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y \quad C_2 = 933.871 \text{ k} \quad (10-124)$$

$$C = \min \left(\left(\begin{array}{c} C_1 \\ C_2 \end{array} \right) \right) \quad \text{Compressive force in slab} \quad C = 933.871 \text{ k}$$

$$a = \frac{C}{0.85 \times f_c \times b_{\text{eff}}} \quad \text{Depth of stressblock} \quad a = 6.26 \text{ in} \quad (10-125)$$

a is distance from top of slab down to plastic NA

$$AF_{tf} = A_{tf} \times F_y \quad \text{top flange} \quad AF_{tf} = 288.438 \text{ k}$$

$$AF_w = A_w \times F_y \quad \text{web above welded plate} \quad AF_w = 356.994 \text{ k}$$

$$AF_{bf} = AF_{tf} \quad \text{bottom flange} \quad AF_{bf} = 288.438 \text{ k}$$

Check compact:

$$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \begin{array}{l} D_{cp} \text{ is depth of web in compression} \\ \text{Since PNA lies in slab} \Rightarrow \text{OK!} \end{array} \quad (10-129)$$

Check (10-129a):

$$\frac{D_p}{D_{\text{prime}}} \leq 5 \quad (10-129a)$$

$D_p = a$ Distance from top of slab to PNA

$$D_p = 6.26 \text{ in}$$

$$D_{\text{prime}} = 0.9 \times \frac{d + t_s}{7.5}$$

$$D_{\text{prime}} = 4.066 \text{ in}$$

$$\frac{D_p}{D_{\text{prime}}} = 1.54 \quad \text{OK!}$$

Since $D_{\text{prime}} < D_p < 5D_{\text{prime}} \Rightarrow$

$$M_u = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{\text{prime}}} \quad (10-129c)$$

Slab: $C = 933.871 \text{ k}$ $d_c = \frac{a}{2}$

$$d_c = 3.13 \text{ in}$$

Top flange: $AF_{tf} = 288.438 \text{ k}$ $d_{tf} = t_s - a + \frac{t_{tf}}{2}$

$$d_{tf} = 2.201 \text{ in}$$

Web: $AF_w = 356.994 \text{ k}$ $d_w = t_s - a + t_{tf} + \frac{t_w}{2}$

$$d_w = 2.887 \text{ in}$$

Bottom flange: $AF_{bf} = 288.438 \text{ k}$ $d_{bf} = d + t_s - a - \frac{t_{tf}}{2}$

$$d_{bf} = 27.163 \text{ in}$$

$$M_p = C \times d_c + AF_{tf} \times d_{tf} + AF_w \times d_w + AF_{bf} \times d_{bf} \quad M_p = 1.035 \times 10^3 \text{ ftk}$$

Yield moment:

$$I_g = 7.549 \times 10^3 \text{ in}^4 \quad \text{Moment of inertia for composite section}$$

$$Y = d + \frac{t_s}{2} - \text{Ecc} \quad \text{Distance from bottom of steel to elastic NA}$$

$$Y = 24.564 \text{ in}$$

$$M_y = F_y \times \frac{I_g}{Y}$$

$$M_y = 845.129 \text{ ftk}$$

Moment Capacity:

$$M_n = \frac{5M_p - 0.85M_y}{4} + \frac{0.85 \times M_y - M_p}{4} \times \frac{D_p}{D_{\text{prime}}}$$

$$M_n = 992.518 \text{ ftk}$$

$$M_n = 1.191 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$K = 5$ For unstiffened beams and girders

$D = 24.04 \text{ in}$ Clear distance between flanges

$t_w = 0.45 \text{ in}$ Web thickness

$$\frac{D}{t_w} = 53.422 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 207.057 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p$$

$$V_n = 207.057 \text{ k} \quad (10-113)$$

Rating:

Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$
 Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

Lane Load	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 3.264
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 5.449
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 2.114
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 3.529
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 2.597
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 4.334
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 2.113
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 3.527
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.597
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 4.334
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.113
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 3.527
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 3.168
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 5.288
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.578
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 4.304

D.4. RATING FOR BRIDGE #4

RATING FOR GIRDER

Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{\text{k}}{\text{in}^2} \quad \text{ftk} = \text{k} \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of concrete}$$

$$f_c = 3.5\text{ksi} \quad \text{Concrete strength}$$

$$F_y = 36\text{ksi} \quad \text{Steel strength}$$

Loads for Lane Loading

$$P_m = 18\text{k} \quad \text{Point Load for Moment for Lane Loading}$$

$$P_s = 26\text{k} \quad \text{Point Load for Shear for Lane Loading}$$

$$P_m = 18\text{k} \quad \text{Point Load for Moment for Lane Loading}$$

$$\omega = 0.64 \frac{\text{k}}{\text{ft}} \quad \text{Uniform Load for Lane Loading}$$

Structure

$$S_b = 20\text{ft} + 2\text{in} \quad \text{Girder spacing}$$

$$t_s = 7.8\text{in} \quad \text{Thickness of concrete slab}$$

$$\text{overhang} = 37\text{in} \quad \text{Overhang of concrete slab}$$

$$L_{\text{span1}} = 46.5\text{ft} \quad \text{Design span length at span 1}$$

$$L_{\text{span2}} = 61.5\text{ft} \quad \text{Design span length at span 2.}$$

$$L_{\text{pier1}} = 54\text{ft} \quad \text{Design span lengths of pier 1 and pier 2 are taken as the average span lengths of the adjacent spans.}$$

$$L_{\text{pier2}} = 61.5\text{ft}$$

Live Load Distribution Factor for all girder sections per wheel line:

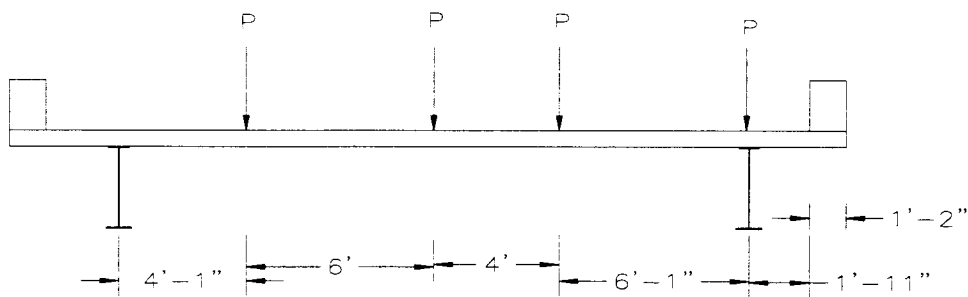


Figure D.13. Live Load Distribution factor.

$$DF = \frac{(4\text{ft} + 1\text{in}) + (10\text{ft} + 1\text{in}) + (14\text{ft} + 1\text{in}) + (20\text{ft} + 1\text{in})}{20\text{ft} + 2\text{in}} \quad DF = 2.397$$

Lane Load Distribution factor per lane:

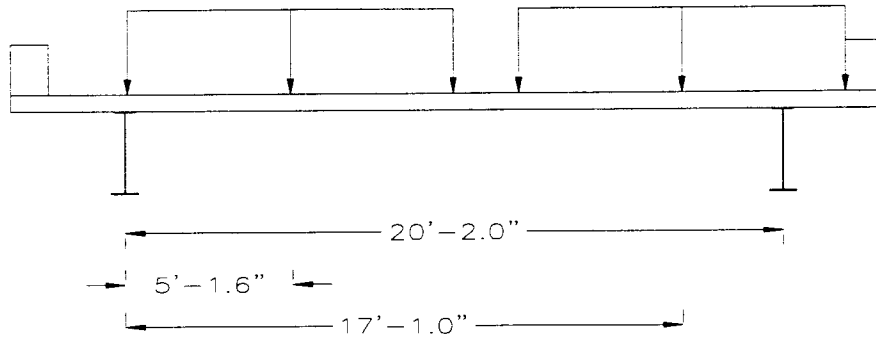


Figure D.14. Lane Load Distribution factor.

$$DF_{\text{Lane}} = \frac{(5\text{ft} + 1.6\text{in}) + (17\text{ft} + 1\text{in})}{20\text{ft} + 2\text{in}} \quad DF_{\text{Lane}} = 1.102$$

Impact:

$$I_{\text{span1}} = \begin{cases} \frac{50\text{ft}}{L_{\text{span1}} + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L_{\text{span1}} + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad I_{\text{span1}} = 0.292 \quad 3.8.2.1$$

$$I_{\text{span2}} = \begin{cases} \frac{50\text{ft}}{L_{\text{span2}} + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L_{\text{span2}} + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad I_{\text{span2}} = 0.268$$

$$I_{\text{pier1}} = \begin{cases} \frac{50\text{ft}}{L_{\text{pier1}} + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L_{\text{pier1}} + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad I_{\text{pier1}} = 0.279$$

$$I_{\text{pier2}} = \begin{cases} \frac{50\text{ft}}{L_{\text{pier2}} + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L_{\text{pier2}} + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad I_{\text{pier2}} = 0.268$$

Dead Load at midspan for all spans (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb and parapet equally distributed to all girders/stringers.

$$\text{Steel:} \quad w_b = w_{\text{steel}} \times 22.125\text{in}^2 \quad w_b = 0.075 \frac{\text{k}}{\text{ft}}$$

$$\text{Floorbeams:} \quad w_f = w_{\text{steel}} \times 23.53\text{in}^2 \times \frac{S_b}{2} \times \frac{11}{(46.5\text{ft} + 61.5\text{ft}) \times 2} \quad w_f = 0.041 \frac{\text{k}}{\text{ft}}$$

$$\text{Slab:} \quad w_s = w_{\text{concrete}} \times t_s \times \left(\frac{S_b}{2} + \text{overhang} \right) \quad w_s = 1.284 \frac{\text{k}}{\text{ft}}$$

$$\text{Curb:} \quad w_c = w_{\text{concrete}} \times 14\text{in} \times 3.875\text{in} \quad w_c = 0.057 \frac{\text{k}}{\text{ft}}$$

$$\text{Parapet:} \quad w_p = w_{\text{concrete}} \times 26\text{in} \times 6\text{in} \quad w_p = 0.163 \frac{\text{k}}{\text{ft}}$$

Total Dead Load = sum w + add 5%

$$\text{DL} = (w_b + w_f + w_s + w_c + w_p) \times 1.05 \quad \text{DL} = 1.7 \frac{\text{k}}{\text{ft}}$$

Dead Load at first pier (steel, parapet, slab, curb):

$$\text{Steel:} \quad w_b = w_{\text{steel}} \times 38.25\text{in}^2 \quad w_b = 0.13 \frac{\text{k}}{\text{ft}}$$

$$\text{Floorbeams:} \quad w_f = w_{\text{steel}} \times 23.53\text{in}^2 \times \frac{S_b}{2} \times \frac{11}{(46.5\text{ft} + 61.5\text{ft}) \times 2} \quad w_f = 0.041 \frac{\text{k}}{\text{ft}}$$

$$\text{Slab:} \quad w_s = w_{\text{concrete}} \times t_s \times \left(\frac{S_b}{2} + \text{overhang} \right) \quad w_s = 1.284 \frac{\text{k}}{\text{ft}}$$

$$\text{Curb:} \quad w_c = w_{\text{concrete}} \times 14\text{in} \times 3.875\text{in} \quad w_c = 0.057 \frac{\text{k}}{\text{ft}}$$

$$\text{Parapet:} \quad w_p = w_{\text{concrete}} \times 26\text{in} \times 6\text{in} \quad w_p = 0.163 \frac{\text{k}}{\text{ft}}$$

Total Dead Load = sum w + add 5%

$$\text{DL} = (w_b + w_f + w_s + w_c + w_p) \times 1.05 \quad \text{DL} = 1.758 \frac{\text{k}}{\text{ft}}$$

Dead Load at second pier (steel, parapet, slab, curb):

$$\text{Steel:} \quad w_b = w_{\text{steel}} \times 41\text{in}^2 \quad w_b = 0.139 \frac{\text{k}}{\text{ft}}$$

$$\text{Floorbeams:} \quad w_f = w_{\text{steel}} \times 23.53\text{in}^2 \times \frac{S_b}{2} \times \frac{11}{(46.5\text{ft} + 61.5\text{ft}) \times 2} \quad w_f = 0.041 \frac{\text{k}}{\text{ft}}$$

$$\text{Slab:} \quad w_s = w_{\text{concrete}} \times t_s \times \left(\frac{S_b}{2} + \text{overhang} \right) \quad w_s = 1.284 \frac{\text{k}}{\text{ft}}$$

$$\text{Curb:} \quad w_c = w_{\text{concrete}} \times 14\text{in} \times 3.875\text{in} \quad w_c = 0.057 \frac{\text{k}}{\text{ft}}$$

$$\text{Parapet:} \quad w_p = w_{\text{concrete}} \times 26\text{in} \times 6\text{in} \quad w_p = 0.163 \frac{\text{k}}{\text{ft}}$$

Total Dead Load = sum w + add 5%

$$\text{DL} = (w_b + w_f + w_s + w_c + w_p) \times 1.05 \quad \text{DL} = 1.768 \frac{\text{k}}{\text{ft}}$$

Use QCon to calculate the Dead Load Moment and Shear for all girder sections.

$$\text{Shear at abutment:} \quad V_{\text{DL_abut}} = 28.84\text{k}$$

$$\text{Positive moment at first span:} \quad M_{\text{DL_span1}} = 210.94\text{ftk}$$

$$\text{Positive moment at second span:} \quad M_{\text{DL_span2}} = 277.72\text{ftk}$$

$$\text{Shear at first pier:} \quad V_{\text{DL_pier1}} = 51.84\text{k}$$

$$\text{Negative moment at first pier:} \quad M_{\text{DL_pier1}} = 499.44\text{ftk}$$

$$\text{Shear at second pier:} \quad V_{\text{DL_pier2}} = 53.82\text{k}$$

$$\text{Negative moment at second pier:} \quad M_{\text{DL_pier2}} = 557.40\text{ftk}$$

Live Load analysis using QCon to calculate maximum moment and shearPositive moment at first span:

Lane Load:	Lane load. Max moment is found for point load at $x = 0.45L$ from pier 1 at span 1 in addition to uniform load at spans 1 and 3.	$M_{LL} = 163.38 \text{ ftk}$
	$M_{LL_span1_Lane} = M_{LL} \times (1 + I_{span1}) \times DF_{Lane}$	$M_{LL_span1_Lane} = 232.463 \text{ ftk}$
HS-20	Truck load. Max moment is found for middle axle at $0.49L$ from the abutment.	$M_{LL} = 223.3 \text{ ftk}$
	$M_{LL_span1_HS20} = M_{LL} \times (1 + I_{span1}) \times DF$	$M_{LL_span1_HS20} = 691.212 \text{ ftk}$
H-20	Truck load. Max moment is found for rear axle at $0.42L$ to the right of the abutment.	$M_{LL} = 171.53 \text{ ftk}$
	$M_{LL_span1_H20} = M_{LL} \times (1 + I_{span1}) \times DF$	$M_{LL_span1_H20} = 530.961 \text{ ftk}$
Type 3	Truck load. Max moment is found for middle axle at $0.42L$ to the right of abutment.	$M_{LL} = 176.01 \text{ ftk}$
	$M_{LL_span1_Type3} = M_{LL} \times (1 + I_{span1}) \times DF$	$M_{LL_span1_Type3} = 544.828 \text{ ftk}$

Shear at abutment:

Lane Load:	Load 26k at abutment in addition to uniform loading on spans 1 and 3.	$V_{LL} = 19.96 \text{ k}$
	$V_{LL_abut_Lane} = V_{LL} \times DF_{Lane}$	$V_{LL_abut_Lane} = 21.989 \text{ k}$
HS-20	Truck load. Rear axle at abutment.	$V_{LL} = 27.4 \text{ k}$
	$V_{LL_abut_HS20} = V_{LL} \times DF$	$V_{LL_abut_HS20} = 65.669 \text{ k}$
H-20	Truck load. Rear axle at abutment.	$V_{LL} = 18.54 \text{ k}$
	$V_{LL_abut_H20} = V_{LL} \times DF$	$V_{LL_abut_H20} = 44.435 \text{ k}$
Type 3	Truck load. Rear axle at abutment.	$V_{LL} = 20.19 \text{ k}$
	$V_{LL_abut_Type3} = V_{LL} \times DF$	$V_{LL_abut_Type3} = 48.389 \text{ k}$

Positive moment at second span:

Lane Load:		$M_{LL} = 183.01 \text{ ftk}$
	$M_{LL_span2_Lane} = M_{LL} \times (1 + I_{span2}) \times DF_{Lane}$	$M_{LL_span2_Lane} = 255.665 \text{ ftk}$
HS-20	Truck load. Max moment is found for middle axle at span 2 at $0.53L$ from pier 1.	$M_{LL} = 255.1 \text{ ftk}$
	$M_{LL_span2_HS20} = M_{LL} \times (1 + I_{span2}) \times DF$	$M_{LL_span2_HS20} = 775.31 \text{ ftk}$
H-20	Truck load. Max moment is found for rear axle at $0.52L$ to the right of pier 1.	$M_{LL} = 183.81 \text{ ftk}$
	$M_{LL_span2_H20} = M_{LL} \times (1 + I_{span2}) \times DF$	$M_{LL_span2_H20} = 558.643 \text{ ftk}$

Type 3	Truck load. Max moment is found for middle axle at 0.49L to the right of pier 1.	$M_{LL} = 192.83 \text{ ftk}$
	$M_{LL_span2_Type3} = M_{LL} \times (1 + I_{span2}) \times DF$	$M_{LL_span2_Type3} = 586.057 \text{ ftk}$

Negative moment at first pier:

Lane Load:	In addition to the uniform load, put 18k at 0.38L to the right of pier 1, and another 18k at 0.42L to the left of pier 1	$M_{LL} = 199.37 \text{ ftk}$
	$M_{LL_pier1_Lane} = M_{LL} \times (1 + I_{pier1}) \times DF_{Lane}$	$M_{LL_pier1_Lane} = 280.988 \text{ ftk}$
HS-20	Truck load. Max moment is found for front axle at 30' to the right of pier 1.	$M_{LL} = 164.9 \text{ ftk}$
	$M_{LL_pier1_HS20} = M_{LL} \times (1 + I_{pier1}) \times DF$	$M_{LL_pier1_HS20} = 505.61 \text{ ftk}$
H-20	Truck load. Max moment is found for front axle at 13' to the right of pier 1.	$M_{LL} = 106.20 \text{ ftk}$
	$M_{LL_pier1_H20} = M_{LL} \times (1 + I_{pier1}) \times DF$	$M_{LL_pier1_H20} = 325.626 \text{ ftk}$
Type 3	Truck load. Max moment is found for front axle at 36' to the right of pier 1.	$M_{LL} = 127.90 \text{ ftk}$
	$M_{LL_pier1_Type3} = M_{LL} \times (1 + I_{pier1}) \times DF$	$M_{LL_pier1_Type3} = 392.162 \text{ ftk}$

Shear at first pier:

Lane Load:	Load 26k at pier 1 in addition to uniform load on spans 1, 2 and 4.	$V_{LL} = 23.98 \text{ k}$
	$V_{LL_pier1_Lane} = V_{LL} \times (1 + I_{pier1}) \times DF_{Lane}$	$V_{LL_pier1_Lane} = 33.797 \text{ k}$
HS-20	Truck load. Max shear for rear axle at pier 1.	$V_{LL} = 31.25 \text{ k}$
	$V_{LL_pier1_HS20} = V_{LL} \times (1 + I_{pier1}) \times DF$	$V_{LL_pier1_HS20} = 95.818 \text{ k}$
H-20	Truck load. Rear axle at pier 1.	$V_{LL} = 19.25 \text{ k}$
	$V_{LL_pier1_H20} = V_{LL} \times (1 + I_{pier1}) \times DF$	$V_{LL_pier1_H20} = 59.024 \text{ k}$
Type 3	Truck load. Front axle at 14' to the right of pier 1.	$V_{LL} = 22.45 \text{ k}$
	$V_{LL_pier1_Type3} = V_{LL} \times (1 + I_{pier1}) \times DF$	$V_{LL_pier1_Type3} = 68.835 \text{ k}$

Negative moment at second pier:

Lane Load:	In addition to the uniform load, put 18k at 0.38L to the right of pier 1, and another 18k at 0.38L to the left of pier 1	$M_{LL} = 219.47 \text{ ftk}$
	$M_{LL_pier2_Lane} = M_{LL} \times (1 + I_{pier2}) \times DF_{Lane}$	$M_{LL_pier2_Lane} = 306.6 \text{ ftk}$
HS-20	Truck load. Max moment is found for front axle at 29' to the right of pier 2.	$M_{LL} = 168.14 \text{ ftk}$
	$M_{LL_pier2_HS20} = M_{LL} \times (1 + I_{pier2}) \times DF$	$M_{LL_pier2_HS20} = 511.018 \text{ ftk}$

H-20	Max moment is found for rear axle at 34' from pier 1.	$M_{LL} = 98.50 \text{ftk}$
	$M_{LL_pier2_H20} = M_{LL} \times (1 + I_{pier2}) \times DF$	$M_{LL_pier2_H20} = 299.365 \text{ftk}$
Type 3	Truck load. Max moment is found for front axle at 36' to the right of pier 2.	$M_{LL} = 118.73 \text{ftk}$
	$M_{LL_pier2_Type3} = M_{LL} \times (1 + I_{pier2}) \times DF$	$M_{LL_pier2_Type3} = 360.849 \text{ftk}$

Shear at second pier:

Lane Load:	Load 26k at pier 2 in addition to uniform load on spans 2 and 3.	$V_{LL} = 24.08 \text{k}$
	$V_{LL_pier2_Lane} = V_{LL} \times (1 + I_{pier2}) \times DF_{Lane}$	$V_{LL_pier2_Lane} = 33.64 \text{k}$
HS-20	Truck load. Max shear for rear axle at pier 3.	$V_{LL} = 31.06 \text{k}$
	$V_{LL_pier2_HS20} = V_{LL} \times (1 + I_{pier2}) \times DF$	$V_{LL_pier2_HS20} = 94.399 \text{k}$
H-20	Truck load. Front axle at 11' to the right of pier 2.	$V_{LL} = 19.24 \text{k}$
	$V_{LL_pier2_H20} = V_{LL} \times (1 + I_{pier2}) \times DF$	$V_{LL_pier2_H20} = 58.475 \text{k}$
Type 3	Truck load. Rear axle at pier 2.	$V_{LL} = 22.34 \text{k}$
	$V_{LL_pier2_Type3} = V_{LL} \times (1 + I_{pier2}) \times DF$	$V_{LL_pier2_Type3} = 67.897 \text{k}$

Girder at first spanInput:

$A_{tf} = 8 \text{in} \times 0.5 \text{in}$	Area of top flange	$A_{tf} = 4 \text{in}^2$	
$A_w = 0.3125 \text{in} \times 38 \text{in}$	Area of web	$A_w = 11.875 \text{in}^2$	
$A_{bf} = 10 \text{in} \times 0.625 \text{in}$	Area of bottom flange	$A_{bf} = 6.25 \text{in}^2$	
$t_{tf} = 0.5 \text{in}$	Thickness of top flange		
$b_w = 38 \text{in}$	Width of web		
$t_{bf} = 0.625 \text{in}$	Thickness of bottom flange		
$t_w = .3125 \text{in}$	Thickness of web		
$b_{eff} = \min \left(\left(\frac{1}{4} \times L_{span1} \right), \left(S_b \right), \left(12 \times t_s \right) \right)$		Controls for all girder sections	$b_{eff} = 93.6 \text{in}$ 10.38.3.1

Section Properties:

$I_g = 21632 \text{in}^4$	Moment of inertia for elastic section (from Excel)	
$Ecc = 2.4 \text{in}$	Distance from c.g. slab to c.g elastic composit section (from Excel)	
$A_b = A_{tf} + A_w + A_{bf}$	Total area of steel	$A_b = 22.125 \text{in}^2$
$d = t_{tf} + b_w + t_{bf}$	Total depth of steel	$d = 39.125 \text{in}$
$D = b_w$	Clear distance between flanges	$D = 38 \text{in}$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{eff} \times t_s \quad C_1 = 2.172 \times 10^3 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y \quad C_2 = 796.5 \text{ k} \quad (10-124)$$

$$C = \min \left(\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} \right) \quad \text{Compressive force in slab} \quad C = 796.5 \text{ k}$$

$$a = \frac{C}{0.85 \times f_c \times b_{eff}} \quad \text{Depth of concrete stressblock} \quad a = 2.86 \text{ in} \quad (10-125)$$

a is the distance from top of slab down to plastic neutral axis.

$$\begin{aligned} AF_{tf} &= A_{tf} \times F_y & \text{Force in top flange} & AF_{tf} = 144 \text{ k} \\ AF_w &= A_w \times F_y & \text{Force in web} & AF_w = 427.5 \text{ k} \\ AF_{bf} &= A_{bf} \times F_y & \text{Force in bottom flange} & AF_{bf} = 225 \text{ k} \end{aligned}$$

Check compact:

$$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad \begin{array}{l} D_{cp} \text{ is depth of web in compression.} \\ \text{Since PNA lies in slab} \Rightarrow \text{OK!} \end{array} \quad (10-129)$$

Check (10-129a):

$$\frac{D_p}{D_{prime}} \leq 5 \quad (10-129a)$$

$$\begin{aligned} D_p &= a & \text{Distance from top of slab to PNA} & D_p = 2.86 \text{ in} \\ D_{prime} &= 0.9 \times \frac{d + t_s}{7.5} & & D_{prime} = 5.631 \text{ in} \end{aligned}$$

$$\frac{D_p}{D_{prime}} = 0.508 \quad \text{OK!}$$

Since $D_p < D_{prime} \Rightarrow$ use full plastic moment $\Rightarrow M_u = M_p$ (10-129b)

$$\text{Slab:} \quad C = 796.5 \text{ k} \quad d_c = \frac{a}{2} \quad d_c = 1.43 \text{ in}$$

$$\text{Top flange:} \quad AF_{tf} = 144 \text{ k} \quad d_{tf} = t_s - a + \frac{t_{tf}}{2} \quad d_{tf} = 5.19 \text{ in}$$

$$\text{Web above welded plate:} \quad AF_w = 427.5 \text{ k} \quad d_w = t_s - a + t_{tf} + \frac{b_w}{2} \quad d_w = 24.44 \text{ in}$$

$$\text{Bottom flange:} \quad AF_{bf} = 225 \text{ k} \quad d_{bf} = t_s - a + t_{tf} + b_w + \frac{t_{bf}}{2} \quad d_{bf} = 43.752 \text{ in}$$

$$M_p = C \times d_c + AF_{tf} \times d_{tf} + AF_w \times d_w + AF_{bf} \times d_{bf} \quad M_p = 1.848 \times 10^3 \text{ ftk}$$

Moment Capacity at midspan, first span:

$$M_n = M_p \quad M_n = 1.848 \times 10^3 \text{ ftk} \quad (10-129b)$$

$$M_n = 2.218 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity at abutment:

$$d_o = 2\text{ft} + 9\text{in} \quad \text{Distance between the transverse stiffeners}$$

$$D = 38\text{ in} \quad \text{Clear distance between flanges}$$

$$K = 5 + \frac{5}{\left(\frac{d_o}{D}\right)^2}$$

$$K = 11.63$$

$$10.48.8.1$$

Check (10-116) and (10-117)

$$\frac{D}{t_w} \geq \frac{7500 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$D = 38\text{ in} \quad \text{Clear distance between flanges}$$

$$t_w = 0.313\text{ in} \quad \text{Web thickness}$$

$$\frac{D}{t_w} = 121.6 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 107.842 \quad \frac{7500 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 134.803 \quad \Rightarrow C \text{ is given by (10-116)}$$

$$C = \frac{6000 \times \sqrt{K}}{\left(\frac{D}{t_w}\right) \times \sqrt{\frac{F_y}{1 \text{ psi}}}} \quad C = 0.887 \quad (10-117)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 247.95 \text{ k} \quad (10-115)$$

$$V_n = V_p \times \left[C + \frac{0.87 \times (1 - C)}{\sqrt{1 + \left(\frac{d_o}{D}\right)^2}} \right] \quad V_n = 238.324 \text{ k} \quad (10-113)$$

Rating for positive moment at first span and shear at the abutment:

$$\text{Inventory:} \quad A_1 = 1.3 \quad A_{2i} = 2.17$$

$$\text{Operating:} \quad A_1 = 1.3 \quad A_{2o} = 1.3$$

$$\text{Lane} \quad \text{Flexure:} \quad \text{Inventory:} \quad \text{RF} = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2i} \times M_{LL_span1_Lane}} \quad \text{RF} = 3.12$$

$$\text{Operating:} \quad \text{RF} = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2o} \times M_{LL_span1_Lane}} \quad \text{RF} = 5.208$$

$$\text{Shear:} \quad \text{Inventory:} \quad \text{RF} = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2i} \times V_{LL_abut_Lane}} \quad \text{RF} = 4.209$$

$$\text{Operating:} \quad \text{RF} = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2o} \times V_{LL_abut_Lane}} \quad \text{RF} = 7.026$$

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2i} \times M_{LL_span1_HS20}}$	RF = 1.049
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2o} \times M_{LL_span1_HS20}}$	RF = 1.752
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2i} \times V_{LL_abut_HS20}}$	RF = 1.409
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2o} \times V_{LL_abut_HS20}}$	RF = 2.352
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2i} \times M_{LL_span1_H20}}$	RF = 1.366
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2o} \times M_{LL_span1_H20}}$	RF = 2.28
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2i} \times V_{LL_abut_H20}}$	RF = 2.083
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2o} \times V_{LL_abut_H20}}$	RF = 3.477
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2i} \times M_{LL_span1_Type3}}$	RF = 1.331
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_span1}}{A_{2o} \times M_{LL_span1_Type3}}$	RF = 2.222
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2i} \times V_{LL_abut_Type3}}$	RF = 1.913
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_abut}}{A_{2o} \times V_{LL_abut_Type3}}$	RF = 3.193

LOADS EXTRACTED FROM THE BDI-SOFTWARE FOR GIRDER AT FIRST SPAN

Impact factor used in BDI:

$$I = 0.3$$

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 1101in \times k$
			Live load	$M_{LL} = 4670in \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 6.071 \times 10^3 in \times k$
	Shear	Inventory	Dead load	$V_{DL_HS20} = 17.14k$
			Live load	$V_{LL} = 51.64k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 67.132 k$
H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 1329in \times k$

			Live load	$M_{LL} = 3500 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 4.55 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_H20} = 17.14k$
			Live load	$V_{LL} = 33.83k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 43.979k$
Type-3	Flexure	Inventory	Dead load	$M_{DL_Type3} = 1329 \text{ in} \times k$
			Live load	$M_{LL} = 3556 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 4.623 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_Type3} = 17.14k$
			Live load	$V_{LL} = 37.98k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 49.374k$

BDI Ratings for Girder at first pier:Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$ Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.575
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 2.629
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 1.483
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 2.476
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 2.071
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 3.457
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.264
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 3.779
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 2.039
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 3.403

Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.016
	Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 3.366

Girder at midspan, second span

This section has the same cross-section as the above section (Girder at abutment, Span 1). The only difference is the design span length.

$$L_{span2} = 61.5 \text{ ft}$$

Design span length

$$DF = 2.397$$

Live load distribution factor (from above)

$$b_{eff} = \min \left(\left(\frac{1}{4} \times L_{span2} \right), \left(S_b \right), \left(12 \times t_s \right) \right)$$

$$b_{eff} = 93.6 \text{ in} \quad 10.38.3.1$$

Capacities:

Since the section properties and beff are the same as for span 1, the moment capacity to be used in the ratings done by hand calculations remains the same as for span 1.

$$M_n = 1.848 \times 10^3 \text{ ftk}$$

$$M_n = 2.218 \times 10^4 \text{ in} \times \text{k}$$

Rating for positive moment at second span:

Inventory:	$A_1 = 1.3$	$A_{2i} = 2.17$
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Operating:	$A_1 = 1.3$	$A_{2o} = 1.3$
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Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2i} \times M_{LL_span2_Lane}}$	RF = 2.681
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2o} \times M_{LL_span2_Lane}}$	RF = 4.475
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HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2i} \times M_{LL_span2_HS20}}$	RF = 0.884
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2o} \times M_{LL_span2_HS20}}$	RF = 1.476
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H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2i} \times M_{LL_span2_H20}}$	RF = 1.227
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2o} \times M_{LL_span2_H20}}$	RF = 2.048
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Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2i} \times M_{LL_span2_Type3}}$	RF = 1.169
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_span2}}{A_{2o} \times M_{LL_span2_Type3}}$	RF = 1.952
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LOADS EXTRACTED FROM THE BDI-SOFTWARE FOR GIRDER AT SECOND SPAN

Impact factor used in BDI:

$$I = 0.3$$

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 1856 \text{ in} \times k$
			Live load	$M_{LL} = 5953 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 7.739 \times 10^3 \text{ in} \times k$
H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 1855 \text{ in} \times k$
			Live load	$M_{LL} = 4173 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 5.425 \times 10^3 \text{ in} \times k$
Type-3	Flexure	Inventory	Dead load	$M_{DL_Type3} = 1855 \text{ in} \times k$
			Live load	$M_{LL} = 4420 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 5.746 \times 10^3 \text{ in} \times k$

BDI Ratings for Girde at second span:

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 1.177
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 1.965
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.679
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 2.803
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.585
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 2.646

Girder at first pierInput:

$A_{tf} = 13 \text{ in} \times 0.875 \text{ in}$	Area of top flange	$A_{tf} = 11.375 \text{ in}^2$
$A_w = 0.3125 \text{ in} \times 38 \text{ in}$	Area of web	$A_w = 11.875 \text{ in}^2$
$A_{bf} = 15 \text{ in} \times 1 \text{ in}$	Area of bottom flange	$A_{bf} = 15 \text{ in}^2$
$t_{tf} = 0.875 \text{ in}$	Thickness of top flange	
$b_w = 38 \text{ in}$	Width of web	
$t_{bf} = 1 \text{ in}$	Thickness of bottom flange	
$t_w = .3125 \text{ in}$	Thickness of web	
overhang = 37 in	Overhang of concrete slab	

Section Properties:

$$I_g = 11299 \text{ in}^4 \quad \text{Moment of inertia for elastic section, non-composite section (from Excel)}$$

$$L = \frac{1}{2} \times (46.5 \times \text{ft} + 61.5 \text{ft}) \quad \text{Design span of beam is taken as the average of adjacent span lengths} \quad L = 54 \text{ ft}$$

$$S_b = 20 \text{ft} + 2 \text{in} \quad \text{Girder spacing}$$

$$t_s = 7.8 \text{in} \quad \text{Thickness of concrete slab}$$

$$A_b = A_{tf} + A_w + A_{bf} \quad \text{Total area of steel} \quad A_b = 38.25 \text{ in}^2$$

$$d = t_{tf} + b_w + t_{bf} \quad \text{Total depth of steel} \quad d = 39.875 \text{ in}$$

$$D = b_w \quad \text{Clear distance between flanges} \quad D = 38 \text{ in}$$

$$y_e = \frac{A_{tf} \times \frac{t_{tf}}{2} + A_w \times \left(t_{tf} + \frac{b_w}{2} \right) + A_{bf} \times \left(t_{tf} + b_w + \frac{t_{bf}}{2} \right)}{A_{tf} + A_w + A_{bf}} \quad y_e = 21.742 \text{ in}$$

y_e is the distance from top of top flange and down to elastic NA

Check compact:

10.48.1

$$\frac{b_{\text{prime}}}{t} < \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad b_{\text{prime}} = \frac{1 \text{ ft} + 3 \text{ in}}{2} \quad (10-93)$$

$$t = 1 \text{ in}$$

$$\frac{b_{\text{prime}}}{t} = 7.5 \quad \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 10.831 \quad \text{OK!}$$

$$\frac{D}{t_w} < \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad D = 3.167 \text{ ft}$$

$$t_w = 0.313 \text{ in}$$

$$\frac{D}{t_w} = 121.6 \quad \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 101.351 \quad \text{Not OK} \Rightarrow \text{non-compact}$$

Check Braced Noncompact Section

10.48.2

$$\frac{D_c}{t_w} < \frac{15400}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad (10-100)$$

$$D_c = D + t_{tf} - y_e \quad \text{Depth of web in compression} \quad D_c = 17.133 \text{ in}$$

$$\frac{D_c}{t_w} = 54.827 \quad \frac{15400}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 81.165 \quad \text{OK!}$$

$$L_b < \frac{20000000 \times A_{bf}}{\frac{F_y}{1 \text{ psi}} \times d} \quad (10-100)$$

$$L_b = 3 \text{ ft} + 8 \text{ in}$$

Max Spacing of lateral bracing

$$L_b = 3.667 \text{ ft}$$

$$L_b = 3.667 \text{ ft}$$

$$\frac{20000000 \times A_{bf}}{\frac{F_y}{1 \text{ psi}} \times d} = 17.416 \text{ ft}$$

OK!

=> OK! Girder at pier 1 is a Braced Non-Compact Section => $M_u = F_y \times S$

Moment Capacity:

$$I_g = 1.13 \times 10^4 \text{ in}^4$$

Moment of inertia for elastic region

$$y_e = 21.742 \text{ in}$$

Distance from top of top flange down to elastic NA

$$S = \frac{I_g}{y_e}$$

Section Modulus

$$S = 519.694 \text{ in}^3$$

$$M_n = S \times F_y$$

Moment Capacity

$$M_n = 1.559 \times 10^3 \text{ ftk}$$

$$M_n = 1.871 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity for first pier:

$$d_o = 2 \text{ ft} + 9 \text{ in}$$

Distance between the transverse stiffeners

$$D = 38 \text{ in}$$

Clear distance between flanges

$$K = 5 + \frac{5}{\left(\frac{d_o}{D}\right)^2}$$

$$K = 11.63$$

$$10.48.8.1$$

Check (10-116) and (10-117)

$$\frac{D}{t_w} \geq \frac{7500 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$D = 38 \text{ in}$$

Clear distance between flanges

$$t_w = 0.313 \text{ in}$$

Web thickness

$$\frac{D}{t_w} = 121.6$$

$$\frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 107.842$$

$$\frac{7500 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 134.803$$

=> C is given by (10-116)

$$C = \frac{6000 \times \sqrt{K}}{\left(\frac{D}{t_w}\right) \times \sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$C = 0.887$$

$$(10-117)$$

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 247.95 \text{ k}$$

$$(10-115)$$

$$V_n = V_p \times \left[C + \frac{0.87 \times (1 - C)}{\sqrt{1 + \left(\frac{d_o}{D}\right)^2}} \right]$$

$$V_n = 238.324 \text{ k}$$

$$(10-113)$$

Rating for negative moment and shear at first pier:

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2i} \times M_{LL_pier1_Lane}}$	RF = 1.492
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2o} \times M_{LL_pier1_Lane}}$	RF = 2.491
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2i} \times V_{LL_pier1_Lane}}$	RF = 2.331
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2o} \times V_{LL_pier1_Lane}}$	RF = 3.89
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2i} \times M_{LL_pier1_HS20}}$	RF = 0.829
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2o} \times M_{LL_pier1_HS20}}$	RF = 1.384
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2i} \times V_{LL_pier1_HS20}}$	RF = 0.822
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2o} \times V_{LL_pier1_HS20}}$	RF = 1.372
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2i} \times M_{LL_pier1_H20}}$	RF = 1.288
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2o} \times M_{LL_pier1_H20}}$	RF = 2.149
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2i} \times V_{LL_pier1_H20}}$	RF = 1.335
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2o} \times V_{LL_pier1_H20}}$	RF = 2.228
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2i} \times M_{LL_pier1_Type3}}$	RF = 1.069
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier1}}{A_{2o} \times M_{LL_pier1_Type3}}$	RF = 1.785
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2i} \times V_{LL_pier1_Type3}}$	RF = 1.144
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier1}}{A_{2o} \times V_{LL_pier1_Type3}}$	RF = 1.91

LOADS EXTRACTED FROM THE BDI-SOFTWARE FOR GIRDER AT FIRST PIER

Impact factor used in BDI:

$$I = 0.3$$

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 4053 \text{ in} \times k$
			Live load	$M_{LL} = 5749 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 7.474 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_HS20} = 28.80k$
			Live load	$V_{LL} = 57.57k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 74.841 k$
H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 4053 \text{ in} \times k$
			Live load	$M_{LL} = 3493 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 4.541 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_H20} = 28.80k$
			Live load	$V_{LL} = 35.47k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 46.111 k$
Type-3	Flexure	Inventory	Dead load	$M_{DL_Type3} = 4053 \text{ in} \times k$
			Live load	$M_{LL} = 4097 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 5.326 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_Type3} = 28.80k$
			Live load	$V_{LL} = 41.51k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 53.963 k$

Capacities converted from one-foot strip to one-inch strip

Inventory:	$A_1 = 1.3$	$A_{2i} = 2.17$
Operating:	$A_1 = 1.3$	$A_{2o} = 1.3$

BDI Ratings for Girder at first pier:

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 0.829
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 1.383
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 1.237
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 2.065

H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.364
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 2.277
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.008
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 3.351
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.163
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 1.941
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 1.715
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 2.864

Girder at second pierInput:

$A_{tf} = 14\text{in} \times 0.9375\text{in}$	Area of top flange	$A_{tf} = 13.125\text{ in}^2$
$A_w = 0.3125\text{in} \times 38\text{in}$	Area of web	$A_w = 11.875\text{ in}^2$
$A_{bf} = 16\text{in} \times 1\text{in}$	Area of bottom flange	$A_{bf} = 16\text{ in}^2$
$t_{tf} = 0.9375\text{in}$	Thickness of top flange	
$b_w = 38\text{in}$	Width of web	
$t_{bf} = 1\text{in}$	Thickness of bottom flange	
$t_w = .3125\text{in}$	Thickness of web	
overhang = 37in	Overhang of concrete slab	

Section Properties:

$I_g = 12412\text{in}^4$	Moment of inertia for elastic section (from Excel)	
$L = \frac{1}{2} \times (61.5 \times \text{ft} + 61.5\text{ft})$	Design span of beam is taken as the average of adjacent span lengths	$L = 61.5\text{ ft}$
$S_b = 20\text{ft} + 2\text{in}$	Girder spacing	
$t_s = 7.8\text{in}$	Thickness of concrete slab	
$A_b = A_{tf} + A_w + A_{bf}$	Total area of steel	$A_b = 41\text{ in}^2$
$d = t_{tf} + b_w + t_{bf}$	Total depth of steel	$d = 39.938\text{ in}$
$D = b_w$	Clear distance between flanges	$D = 38\text{ in}$

$$y_e = \frac{A_{tf} \times \frac{t_{tf}}{2} + A_w \times \left(t_{tf} + \frac{b_w}{2} \right) + A_{bf} \times \left(t_{tf} + b_w + \frac{t_{bf}}{2} \right)}{A_{tf} + A_w + A_{bf}} \quad y_e = 21.315 \text{ in}$$

y_e is the distance from top of top flange and down to elastic NA

Check compact:

10.48.1

$$\frac{b_{prime}}{t} < \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad b_{prime} = \frac{1 \text{ ft} + 3 \text{ in}}{2} \quad (10-93)$$

$$t = 1 \text{ in}$$

$$\frac{b_{prime}}{t} = 7.5 \quad \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 10.831 \quad \text{OK!}$$

$$\frac{D}{t_w} < \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad D = 3.167 \text{ ft}$$

$$t_w = 0.313 \text{ in}$$

$$\frac{D}{t_w} = 121.6 \quad \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 101.351 \quad \text{Not OK} \Rightarrow \text{non-compact}$$

Check Braced Noncompact Section

10.48.2

$$\frac{D_c}{t_w} < \frac{15400}{\sqrt{\frac{F_y}{1 \text{ psi}}}} \quad (10-100)$$

$$D_c = D + t_{tf} - y_e$$

Depth of web in compression

$$D_c = 17.623 \text{ in}$$

$$\frac{D_c}{t_w} = 56.392$$

$$\frac{15400}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 81.165$$

OK!

$$L_b < \frac{20000000 \times A_{bf}}{\frac{F_y}{1 \text{ psi}} \times d} \quad (10-100)$$

$$L_b = 2 \text{ ft} + 9 \text{ in}$$

Max Spacing of lateral bracing

$$L_b = 2.75 \text{ ft}$$

$$L_b = 2.75 \text{ ft}$$

$$\frac{20000000 \times A_{bf}}{\frac{F_y}{1 \text{ psi}} \times d} = 18.547 \text{ ft}$$

OK!

\Rightarrow OK! Girder at first pier is a Braced Non-Compact Section $\Rightarrow M_u = F_y \cdot S$

Moment Capacity:

$$I_g = 1.13 \times 10^4 \text{ in}^4$$

Moment of inertia for elastic region

$$y_e = 21.315 \text{ in}$$

Distance from top of top flange down
to elastic NA

$$S = \frac{I_g}{y_e}$$

Section Modulus

$$S = 530.099 \text{ in}^3$$

$$M_n = S \times F_y$$

Moment Capacity

$$M_n = 1.59 \times 10^3 \text{ ftk}$$

$$M_n = 1.908 \times 10^4 \text{ in} \times \text{k}$$

Shear Capacity for second pier:

$$d_o = 2 \text{ ft} + 6 \text{ in}$$

Distance between the transverse stiffeners

$$D = 38 \text{ in}$$

Clear distance between flanges

$$K = 5 + \frac{5}{\left(\frac{d_o}{D}\right)^2}$$

$$K = 13.022$$

$$10.48.8.1$$

Check (10-116) and (10-117)

$$\frac{D}{t_w} \geq \frac{7500 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$D = 38 \text{ in}$$

Clear distance between flanges

$$t_w = 0.313 \text{ in}$$

Web thickness

$$\frac{D}{t_w} = 121.6$$

$$\frac{6500 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 123.625$$

=> C is given by (10-117)

$$C = 1.0$$

$$C = 1$$

$$(10-117)$$

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 247.95 \text{ k}$$

$$(10-115)$$

$$V_n = V_p \times \left[C + \frac{0.87 \times (1 - C)}{\sqrt{1 + \left(\frac{d_o}{D}\right)^2}} \right]$$

$$V_n = 247.95 \text{ k}$$

$$(10-113)$$

Rating for negative moment and shear at second pier:

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2i} \times M_{LL_pier2_Lane}}$	RF = 1.301
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2o} \times M_{LL_pier2_Lane}}$	RF = 2.172
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	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2i} \times V_{LL_pier2_Lane}}$	RF = 2.438
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		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2o} \times V_{LL_pier2_Lane}}$	RF = 4.07
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HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2i} \times M_{LL_pier2_HS20}}$	RF = 0.781
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2o} \times M_{LL_pier2_HS20}}$	RF = 1.303
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2i} \times V_{LL_pier2_HS20}}$	RF = 0.869
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2o} \times V_{LL_pier2_HS20}}$	RF = 1.45
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2i} \times M_{LL_pier2_H20}}$	RF = 1.333
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2o} \times M_{LL_pier2_H20}}$	RF = 2.224
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2i} \times V_{LL_pier2_H20}}$	RF = 1.403
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2o} \times V_{LL_pier2_H20}}$	RF = 2.341
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2i} \times M_{LL_pier2_Type3}}$	RF = 1.106
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_pier2}}{A_{2o} \times M_{LL_pier2_Type3}}$	RF = 1.845
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2i} \times V_{LL_pier2_Type3}}$	RF = 1.208
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_pier2}}{A_{2o} \times V_{LL_pier2_Type3}}$	RF = 2.016

LOADS EXTRACTED FROM THE BDI-SOFTWARE FOR GIRDER AT SECOND PIER

Impact factor used in BDI:

$$I = 0.3$$

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 5050 \text{ in} \times k$
			Live load	$M_{LL} = 5204 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 6.765 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_HS20} = 31.56 k$
			Live load	$V_{LL} = 56.64 k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 73.632 k$

H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 5050 \text{ in} \times k$
			Live load	$M_{LL} = 3166 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 4.116 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_H20} = 31.56 k$
			Live load	$V_{LL} = 35.03 k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 45.539 k$
Type-3	Flexure	Inventory	Dead load	$M_{DL_Type3} = 5050 \text{ in} \times k$
			Live load	$M_{LL} = 3709 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 4.822 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_Type3} = 31.56 k$
			Live load	$V_{LL} = 40.74 k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 52.962 k$

BDI Ratings for Girder at second pier:

Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$

Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	$RF = 0.853$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	$RF = 1.423$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	$RF = 1.295$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	$RF = 2.162$
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	$RF = 1.402$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	$RF = 2.34$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	$RF = 2.094$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	$RF = 3.495$
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	$RF = 1.196$

	Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	$RF = 1.997$
Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	$RF = 1.8$
	Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	$RF = 3.005$

LOADS EXTRACTED FROM THE BDI-SOFTWARE FOR HS-20 TRUCK

Girder at first span	Flexure	Inventory	Capacity	$M_{n1} = 22180 \text{ in} \times k$
			Dead Load	$M_{DL1} = 1101 \text{ in} \times k$
			Live Load	$M_{LL} = 4670 \text{ in} \times k$
			$M_{LL_I_1} = M_{LL} \times (1 + I)$	$M_{LL_I_1} = 6.071 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Capacity	$V_{n1} = 238.3 \times k$
			Dead Load	$V_{DL1} = 17.14 \times k$
			Live Load	$V_{LL} = 51.64 \times k$
			$V_{LL_I_1} = V_{LL} \times (1 + I)$	$V_{LL_I_1} = 67.132 k$
Girder at second span	Flexure	Inventory	Capacity	$M_{n2} = 22180 \text{ in} \times k$
			Dead Load	$M_{DL2} = 1856 \text{ in} \times k$
			Live Load	$M_{LL} = 5953 \text{ in} \times k$
			$M_{LL_I_2} = M_{LL} \times (1 + I)$	$M_{LL_I_2} = 7.739 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Capacity	$V_{n3} = 238.3 \times k$
			Dead Load	$V_{DL3} = 28.80 \times k$
			Live Load	$V_{LL} = 57.57 \times k$
			$V_{LL_I_3} = V_{LL} \times (1 + I)$	$V_{LL_I_3} = 74.841 k$
Girder at first pier	Flexure	Inventory	Capacity	$M_{n3} = 18710 \text{ in} \times k$
			Dead Load	$M_{DL3} = 4053 \text{ in} \times k$
			Live Load	$M_{LL} = 5749 \text{ in} \times k$
			$M_{LL_I_3} = M_{LL} \times (1 + I)$	$M_{LL_I_3} = 7.474 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Capacity	$V_{n3} = 238.3 \times k$
			Dead Load	$V_{DL3} = 28.80 \times k$
			Live Load	$V_{LL} = 57.57 \times k$
			$V_{LL_I_3} = V_{LL} \times (1 + I)$	$V_{LL_I_3} = 74.841 k$
Girder at second pier	Flexure	Inventory	Capacity	$M_{n4} = 19080 \text{ in} \times k$
			Dead Load	$M_{DL4} = 5050 \text{ in} \times k$
			Live Load	$M_{LL} = 5204 \text{ in} \times k$
			$M_{LL_I_4} = M_{LL} \times (1 + I)$	$M_{LL_I_4} = 6.765 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Capacity	$V_{n4} = 248 \times k$
			Dead Load	$V_{DL4} = 31.56 \times k$

			Live Load	$V_{LL} = 56.64 \times k$
			$V_{LL_I_4} = V_{LL} \times (1 + I)$	$V_{LL_I_4} = 73.632 k$
Floor beam	Flexure	Inventory	Capacity	$M_{n5} = 6157 \text{ in} \times k$
			Dead Load	$M_{DL5} = 1011 \text{ in} \times k$
			Live Load	$M_{LL} = 2041 \text{ in} \times k$
			$M_{LL_I_5} = M_{LL} \times (1 + I)$	$M_{LL_I_5} = 2.653 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Capacity	$V_{n5} = 141.7 \times k$
			Dead Load	$V_{DL5} = 9.784 \times k$
			Live Load	$V_{LL} = 22.94 \times k$
			$V_{LL_I_5} = V_{LL} \times (1 + I)$	$V_{LL_I_5} = 29.822 k$

BDI Ratings:

Girder at first span	Flexure:	Inventory:	$RF = \frac{M_{n1} - A_1 \times M_{DL1}}{A_{2i} \times M_{LL_I_1}}$	$RF = 1.575$
		Operating:	$RF = \frac{M_{n1} - A_1 \times M_{DL1}}{A_{2o} \times M_{LL_I_1}}$	$RF = 2.629$
	Shear:	Inventory:	$RF = \frac{V_{n1} - A_1 \times V_{DL1}}{A_{2i} \times V_{LL_I_1}}$	$RF = 1.483$
		Operating:	$RF = \frac{V_{n1} - A_1 \times V_{DL1}}{A_{2o} \times V_{LL_I_1}}$	$RF = 2.475$
Girder at second span	Flexure:	Inventory:	$RF = \frac{M_{n2} - A_1 \times M_{DL2}}{A_{2i} \times M_{LL_I_2}}$	$RF = 1.177$
		Operating:	$RF = \frac{M_{n2} - A_1 \times M_{DL2}}{A_{2o} \times M_{LL_I_2}}$	$RF = 1.965$
Girder at first pier	Flexure:	Inventory:	$RF = \frac{M_{n3} - A_1 \times M_{DL3}}{A_{2i} \times M_{LL_I_3}}$	$RF = 0.829$
		Operating:	$RF = \frac{M_{n3} - A_1 \times M_{DL3}}{A_{2o} \times M_{LL_I_3}}$	$RF = 1.383$
	Shear:	Inventory:	$RF = \frac{V_{n3} - A_1 \times V_{DL3}}{A_{2i} \times V_{LL_I_3}}$	$RF = 1.237$
		Operating:	$RF = \frac{V_{n3} - A_1 \times V_{DL3}}{A_{2o} \times V_{LL_I_3}}$	$RF = 2.064$
Girder at second pier	Flexure:	Inventory:	$RF = \frac{M_{n4} - A_1 \times M_{DL4}}{A_{2i} \times M_{LL_I_4}}$	$RF = 0.852$

Floor beam	Operating:		$RF = \frac{M_{n4} - A_1 \times M_{DL4}}{A_{20} \times M_{LL_I_4}}$	RF = 1.423
	Shear:	Inventory:	$RF = \frac{V_{n4} - A_1 \times V_{DL4}}{A_{2i} \times V_{LL_I_4}}$	RF = 1.295
		Operating:	$RF = \frac{V_{n4} - A_1 \times V_{DL4}}{A_{20} \times V_{LL_I_4}}$	RF = 2.162
	Flexure:	Inventory:	$RF = \frac{M_{n5} - A_1 \times M_{DL5}}{A_{2i} \times M_{LL_I_5}}$	RF = 0.841
		Operating:	$RF = \frac{M_{n5} - A_1 \times M_{DL5}}{A_{20} \times M_{LL_I_5}}$	RF = 1.404
	Shear:	Inventory:	$RF = \frac{V_{n5} - A_1 \times V_{DL5}}{A_{2i} \times V_{LL_I_5}}$	RF = 1.993
		Operating:	$RF = \frac{V_{n5} - A_1 \times V_{DL5}}{A_{20} \times V_{LL_I_5}}$	RF = 3.327

RATING FOR FLOORBEAMS, 21 WF 55Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of concrete}$$

$$f_c = 3\text{ksi} \quad \text{Concrete strength}$$

$$F_y = 33\text{ksi} \quad \text{Steel strength}$$

Input:

$$A_{tf} = 8.25\text{in} \times 0.5\text{in} \quad \text{Area of top flange} \quad A_{tf} = 4.125\text{in}^2$$

$$A_w = 0.375\text{in} \times 19.75\text{in} \quad \text{Area of web} \quad A_w = 7.406\text{in}^2$$

$$A_{bf} = 8.25\text{in} \times 0.5\text{in} \quad \text{Area of bottom flange} \quad A_{bf} = 4.125\text{in}^2$$

$$t_{tf} = 0.5\text{in} \quad \text{Thickness of top flange}$$

$$b_w = 19.75\text{in} \quad \text{Width of web}$$

$$t_{bf} = 0.5\text{in} \quad \text{Thickness of bottom flange}$$

$$t_w = 0.375\text{in} \quad \text{Thickness of web}$$

Live Load Distribution Factor:

$$S_b = 20.5\text{ft} \quad \text{Average floorbeam spacing in ft} \quad S_b = 20.5\text{ft} \quad \text{table 3.23.3.1}$$

$$DF = \frac{S_b}{6ft}$$

However, since $DF > 1$, see f in 3.23.3.2
=> Flooring between the beams acts as
a simple beam.

$$DF = 3.417$$

$$DF = 1$$

Section Properties:

$$I_9 = 3907 \text{ in}^4$$

Moment of inertia for elastic section (from Excel)

$$Ecc = 2.99 \text{ in}$$

Distance from c.g. slab to c.g elastic composit section (from Excel)

$$L = 20 \text{ ft} + 2 \text{ in}$$

Design span of beam

$$t_s = 7.8 \text{ in}$$

Thickness of concrete slab

$$A_b = A_{tf} + A_w + A_{bf}$$

$$A_b = 15.656 \text{ in}^2$$

$$d = t_{tf} + b_w + t_{bf}$$

Total depth of steel

$$d = 20.75 \text{ in}$$

$$D = b_w$$

Clear distance between flanges

$$D = 19.75 \text{ in}$$

$$b_{\text{eff}} = \min \left[\left[\frac{1}{4} \times L \right], \left[\frac{1}{2} \times (20.5 \text{ ft} + 20.5 \text{ ft}) \right], \left[12 \cdot t_s \right] \right]$$

$$b_{\text{eff}} = 60.5 \text{ in}$$

8.10.1.1

Girder Loads:

$$I = \begin{cases} \frac{50 \text{ ft}}{L + 125 \text{ ft}} & \text{if } \frac{50 \text{ ft}}{L + 125 \text{ ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact}$$

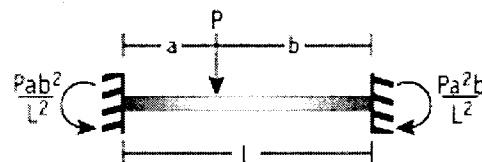
$$I = 0.3$$

3.8.2.1

Maximum Live Load Moments in terms of P (units in kip and ft):

Maximum Load on Floorbeam per wheel line

Assume 25% fixed at the ends. Put two trucks (four line loads) at equal distance from each abutment to produce maximum moment

$$M_A = \frac{P \times a \times b^2}{L^2}$$


$$M_B = \frac{P \times a^2 \times b}{L^2}$$

Figure D.15. Fixed end moments (FEM) due to point load.

HS-20

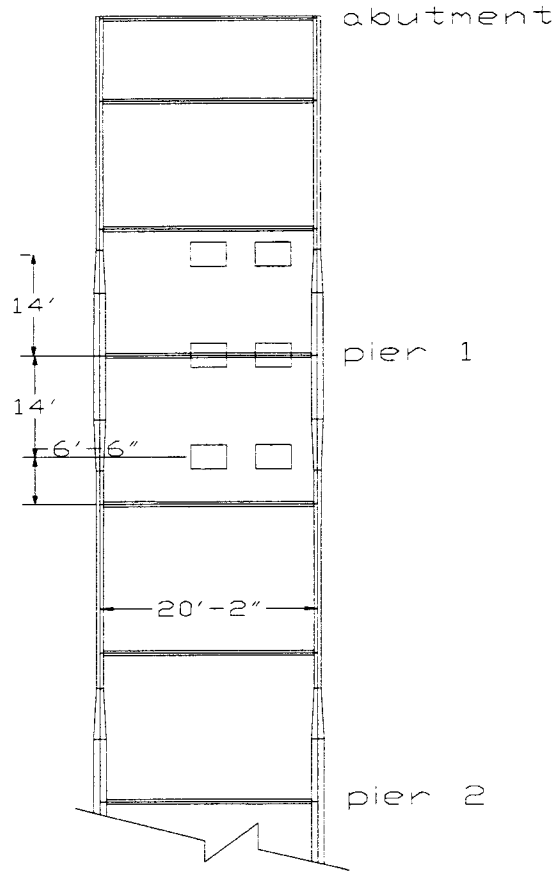


Figure D.16. Location of HS-20 truck to produce maximum live loads on floor beam.

Maximum Load P on Floorbeam per wheel line

$$P = 4k \times \frac{20.5\text{ft} - 14\text{ft}}{20.5\text{ft}} + 16k \times (1) + 16k \times \frac{20.5\text{ft} - 14\text{ft}}{20.5\text{ft}} \quad P = 22.341k$$

Moments at floorbeam due to one truck 2 ft from curb at A and spacing of 4 ft between the two trucks. Same for shear since minimum distance from curb is 2 ft.

If beam is 100 % fixed, due to both trucks

$$M_{A_{100\%_1}} = \frac{P \times a \times b^2}{L^2} + \frac{P \times a \times b^2}{L^2} = \frac{P \times 2 \times 18.167^2}{20.167^2} + \frac{P \times 8 \times 12.167^2}{20.167^2} = 4.535P \quad \text{Truck 1}$$

$$M_{A_{100\%_2}} = \frac{P \times a \times b^2}{L^2} + \frac{P \times a \times b^2}{L^2} = \frac{P \times 12 \times 8.167^2}{20.167^2} + \frac{P \times 18 \times 2.167^2}{20.167^2} = 2.176P \quad \text{Truck 2}$$

$$M_{A_{100\%}} = M_{A_{100\%_1}} + M_{A_{100\%_2}} = 6.711P$$

$$M_{B_{100\%_1}} = \frac{P \times a^2 \times b}{L^2} + \frac{P \times a^2 \times b}{L^2} = \frac{P \times 2^2 \times 18.167}{20.167^2} + \frac{P \times 8^2 \times 12.167}{20.167^2} = 2.093P \quad \text{Truck 1}$$

$$M_{B_{100\%_2}} = \frac{P \times a^2 \times b}{L^2} + \frac{P \times a^2 \times b}{L^2} = \frac{P \times 12^2 \times 8.167}{20.167^2} + \frac{P \times 18^2 \times 2.167}{20.167^2} = 4.618P \quad \text{Truck 2}$$

$$M_{B_{100\%}} = M_{B_{100\%}_1} + M_{B_{100\%}_2} = 6.711P$$

Assume 25% fixed

$$M_A = \frac{M_{A_{100\%}}}{4} = \frac{6.711 \times P}{4} = 1.678 \times P$$

$$M_B = \frac{M_{B_{100\%}}}{4} = \frac{6.711 \times P}{4} = 1.678 \times P$$

$$R_A = 2 \times P$$

Max moment occur at wheel line second closest to A

$$M_{\max} = -M_A + R_A \times 2 + (R_A - P) \times 6 = -1.678 \times P + 2 \times P \times 2 + (2P - P) \times 6 = 8.32 \times P$$

$$M_{\max} = 8.32 \text{ ft} \times P$$

$$M_{\max} = 185.881 \text{ ftk}$$

Max shear occur at the end (at A)

$$V_{\max} = 2 \times P$$

$$V_{\max} = 44.683 \text{ k}$$

All values are lane loads.

$$M_{LL} = M_{\max}$$

$$M_{LL} = 185.881 \text{ ftk}$$

$$V_{LL} = V_{\max}$$

$$V_{LL} = 44.683 \text{ k}$$

$$M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_HS20} = 241.645 \text{ ftk}$$

$$V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_HS20} = 58.088 \text{ k}$$

H-20

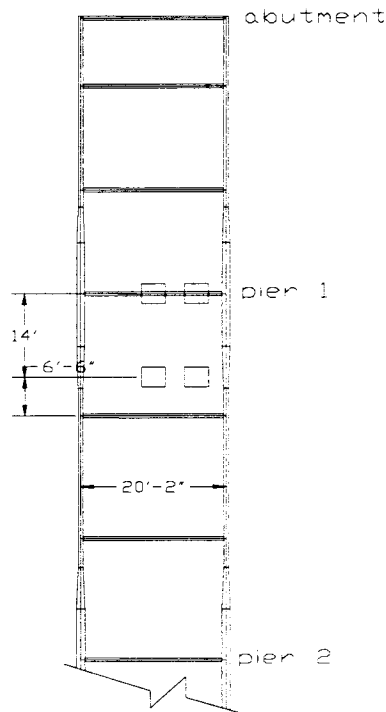


Figure D.17. Location of H-20 truck to produce maximum live loads on floor beam.

Maximum Load P on Floorbeam per wheel line

$$P = 4k \times \left(\frac{20.5\text{ft} - 14\text{ft}}{20.5\text{ft}} \right) + 16k \times (1)$$

$$P = 17.268 \text{ k}$$

$$M_{LL} = 8.32\text{ft} \times P$$

$$M_{LL} = 143.672 \text{ ftk}$$

$$V_{LL} = 2 \times P$$

$$V_{LL} = 34.537 \text{ k}$$

$$M_{LL_I_H20} = M_{LL} \times (1 + I)$$

$$M_{LL_I_H20} = 186.774 \text{ ftk}$$

$$V_{LL_I_H20} = V_{LL} \times (1 + I)$$

$$V_{LL_I_H20} = 44.898 \text{ k}$$

Type 3

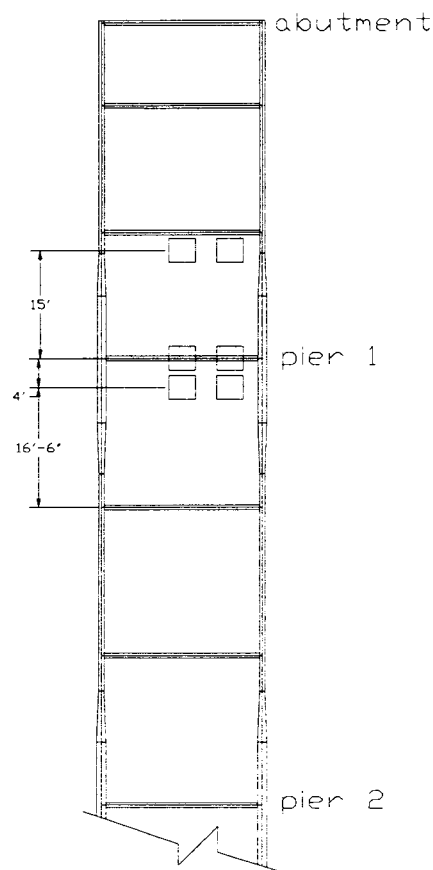


Figure D.18. Location of Type-3 truck to produce maximum live loads on floor beam.

Maximum Load on Floor beam

$$P = 8.5k \times \left(\frac{20.5\text{ft} - 4\text{ft}}{20.5\text{ft}} \right) + 8.5k \times (1) + 8k \times \left(\frac{20.5\text{ft} - 15\text{ft}}{20.5\text{ft}} \right)$$

$$P = 17.488 \text{ k}$$

$$M_{LL} = 8.32\text{ft} \times P$$

$$M_{LL} = 145.499 \text{ ftk}$$

$$V_{LL} = 2 \times P$$

$$V_{LL} = 34.976 \text{ k}$$

$$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$$

$$M_{LL_I_Type3} = 189.148 \text{ ftk}$$

$$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$$

$$V_{LL_I_Type3} = 45.468 \text{ k}$$

Dead Loads (steel, slab):

Assume "heaviest" steel throughout section. Assume that the slab is distributed to the floorbeam using a triangular load and the steel using a uniform load.

$$\text{Steel:} \quad w_b = w_{\text{steel}} \times A_b \quad w_b = 0.053 \frac{\text{k}}{\text{ft}}$$

$$\text{Slab:} \quad w_s = w_{\text{concrete}} \times t_s \times (20.5 \text{ ft}) \quad w_s = 1.999 \frac{\text{k}}{\text{ft}}$$

Uniform Load (dead load steel):

$$\text{If end is 100\% fixed:} \quad M_A = M_B = \frac{w_b \times L^2}{12}$$

$$\text{Use 25\% end restrain:} \quad M_{A_25\%} = \frac{1}{4} \times \frac{w_b \times L^2}{12} = \frac{w_b \times L^2}{48} \quad R_A = R_B = \frac{w_b \times L}{2}$$

$$\text{Moment at midspan} \quad M_1 = -M_{A_25\%} + \frac{1}{2} \times R_A \times \frac{L}{2} = \frac{-w_b \times L^2}{48} + \frac{1}{2} \times \frac{w_b \times L}{2} \times \frac{L}{2}$$

$$M_1 = \frac{5 \times w_b \times L^2}{48}$$

$$\text{Shear at end:} \quad V_1 = R_A = \frac{w_b \times L}{2}$$

Triangular load (dead load slab):

$$\text{If end is 100\% fixed:} \quad M_A = M_B = \frac{5 \times w_s \times L^2}{96}$$

$$\text{Use 25\% end restrain:} \quad M_{A_25\%} = \frac{1}{4} \times M_A = \frac{5 \times w_s \times L^2}{384} \quad R_A = R_B = \frac{w_s \times L}{4}$$

$$\text{Moment at midspan:} \quad M_2 = -M_{A_25\%} + \frac{w_s \times L^2}{12} = \frac{5 \times w_s \times L^2}{384} + \frac{w_s \times L^2}{12} = \frac{9 \times w_s \times L^2}{128}$$

$$\text{Shear at end:} \quad V_2 = R_A = \frac{w_s \times L}{4}$$

Total dead load:

$$M_{DL} = M_1 + M_2 \quad M_{DL} = \frac{5 \times w_b \times L^2}{48} + \frac{9 \times w_s \times L^2}{128} \quad M_{DL} = 59.412 \text{ ftk}$$

$$V_{DL} = V_1 + V_2 \quad V_{DL} = \frac{w_b \times L}{2} + \frac{w_s \times L}{4} \quad V_{DL} = 10.614 \text{ k}$$

Capacities:

$$C_1 = 0.85 \times f_c \times b_{\text{eff}} \times t_s \quad C_1 = 1.203 \times 10^3 \text{ k} \quad (10-123)$$

$$C_2 = A_b \times F_y \quad C_2 = 516.656 \text{ k} \quad (10-124)$$

$$C = \min \left(\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} \right)$$

$$a = \frac{C}{0.85 \times f_c \times b_{eff}}$$

Compressive force in slab

$$C = 516.656 \text{ k}$$

Depth of stressblock

$$a = 3.349 \text{ in} \quad (10-125)$$

a is distance from top of slab down to plastic NA

Check compact:

$$\frac{2 \times D_{cp}}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

 D_{cp} is depth of web in compression

Since PNA lies in slab => OK!

(10-129)

Check (10-129a):

$$\frac{D_p}{D_{prime}} \leq 5$$

(10-129a)

$$D_p = a$$

Distance from top of slab to PNA

$$D_p = 3.349 \text{ in}$$

$$D_{prime} = 0.9 \times \frac{d + t_s}{7.5}$$

$$D_{prime} = 3.426 \text{ in}$$

$$\frac{D_p}{D_{prime}} = 0.978$$

OK!

Slab:

Since $D_p < D_{prime}$ => use full plastic moment => $M_u = M_p$

(10-129b)

$$C = 516.656 \text{ k}$$

$$d_c = \frac{a}{2}$$

$$d_c = 1.674 \text{ in}$$

Top flange:

$$AF_{tf} = A_{tf} \times F_y$$

$$AF_{tf} = 136.125 \text{ k}$$

$$d_{tf} = t_s - a + \frac{t_{tf}}{2}$$

$$d_{tf} = 4.701 \text{ in}$$

Web :

$$AF_w = A_w \times F_y$$

$$AF_w = 244.406 \text{ k}$$

$$d_w = t_s - a + t_{tf} + \frac{t_w}{2}$$

$$d_w = 5.139 \text{ in}$$

Bottom flange:

$$AF_{bf} = AF_{tf}$$

$$AF_{bf} = 136.125 \text{ k}$$

$$d_{bf} = d + t_s - a - \frac{t_{tf}}{2}$$

$$d_{bf} = 24.951 \text{ in}$$

$$M_p = C \times d_c + AF_{tf} \times d_{tf} + AF_w \times d_w + AF_{bf} \times d_{bf}$$

$$M_p = 513.118 \text{ ftk}$$

Moment Capacity:

$$M_n = M_p$$

$$M_n = 513.118 \text{ ftk}$$

$$M_n = 6.157 \times 10^3 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

K = 5 For unstiffened beams and girders

D = 19.75 in Clear distance between flanges

 $t_w = 0.375$ in Web thickness

$$\frac{D}{t_w} = 52.667 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 73.855 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 141.756 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 141.756 \text{ k} \quad (10-113)$$

Rating:Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$ Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 0.831
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 1.388

	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 1.015
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 1.694

H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.075
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 1.795

	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 1.313
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 2.192

Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.062
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	Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_Type3}}$	$RF = 1.773$
Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	$RF = 1.297$
	Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_Type3}}$	$RF = 2.165$

LOADS EXTRACTED FROM THE BDI-SOFTWARE FOR FLOOR BEAM

Impact factor used in BDI:

$I = 0.3$

HS-20	Flexure	Inventory	Dead load	$M_{DL_HS20} = 1011 \text{ in} \times k$
			Live load	$M_{LL} = 2041 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 2.653 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_HS20} = 9.784k$
			Live load	$V_{LL} = 22.94k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 29.822k$
H-20	Flexure	Inventory	Dead load	$M_{DL_H20} = 1011 \text{ in} \times k$
			Live load	$M_{LL} = 1554 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 2.02 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_H20} = 9.784k$
			Live load	$V_{LL} = 20.01k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 26.013k$
Type-3	Flexure	Inventory	Dead load	$M_{DL_Type3} = 1011 \text{ in} \times k$
			Live load	$M_{LL} = 1567 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 2.037 \times 10^3 \text{ in} \times k$
	Shear	Inventory	Dead load	$V_{DL_Type3} = 9.784k$
			Live load	$V_{LL} = 17.96k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 23.348k$

BDI Ratings for Floorbeam:

Inventory:	$A_1 = 1.3$	$A_{2i} = 2.17$
Operating:	$A_1 = 1.3$	$A_{20} = 1.3$

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	$RF = 0.841$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{20} \times M_{LL_I_HS20}}$	$RF = 1.404$

H-20	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 1.994
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 3.328
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.105
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 1.844
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.286
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 3.816
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.096
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 1.829
Type-3	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.547
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 4.251

D.5. RATING OF BRIDGE #5

NON-COMPOSITE ANALYSIS OF STRINGERS

Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2}$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of concrete}$$

$$f_c = 3.5\text{ksi} \quad \text{Concrete strength}$$

$$F_y = 36\text{ksi} \quad \text{Steel strength}$$

Interior Stringer (old steel section)

Input:

$$A_{tf} = 7.492\text{in} \times 0.52\text{in} \quad \text{Area of top flange} \quad A_{tf} = 3.896\text{in}^2$$

$A_w = 16.86\text{in} \times 0.35\text{in}$	Area of web	$A_w = 5.901\text{ in}^2$
$A_{bf} = 7.492\text{in} \times 0.52\text{in}$	Area of bottom flange	$A_{bf} = 3.896\text{ in}^2$
$t_{tf} = 0.52\text{in}$	Thickness of top flange	
$b_w = 16.86\text{in}$	Width of web	
$t_w = 0.35\text{in}$	Thickness of web	
$t_{bf} = 0.52\text{in}$	Thickness of bottom flange	

Section Properties:

$L = 25\text{ft}$	Design span of beam	
$t_s = 9.75\text{in}$	Thickness of concrete slab including the overlay	
$A_b = A_{tf} + A_w + A_{bf}$		$A_b = 13.693\text{ in}^2$
$d = t_{tf} + b_w + t_{bf}$	Total depth of steel	$d = 17.9\text{ in}$
$D = b_w$	Clear distance between flanges	$D = 16.86\text{ in}$

Loads For Lane Loading:

$P_s = 26\text{k}$	Point Load for Shear for Lane Loading	fig. 3.7.6.b
$P_m = 18\text{k}$	Point Load for Moment for Lane Loading	
$\omega = 0.64 \frac{\text{k}}{\text{ft}}$	Uniform Load for Lane Loading	

Live Load Distribution Factor for Design Trucks:

$S_b = 4\text{ft} + 7\text{in}$	Average stringer spacing in ft	$S_b = 4.583\text{ ft}$	table 3.23.1
$DF = \frac{S_b}{5.5\text{ft}}$		$DF = 0.833$	

Girder Loads:

$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases}$	Impact	$I = 0.3$	3.8.2.1
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Maximum Live Load Moments:

Lane Load	$P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear Uniform Load of 0.64 k/ft over the whole span	fig. 3.7.6.b
Uniform load:	$M1_{\text{Lane}} = \frac{\omega \times L^2}{8}$	$M1_{\text{Lane}} = 50\text{ftk}$
	$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L$	$V1_{\text{Lane}} = 8\text{ k}$
Point Load:	$M2_{\text{Lane}} = \frac{P_m \times L}{4}$	$M2_{\text{Lane}} = 112.5\text{ftk}$
	$V2_{\text{Lane}} = P_s$	$V2_{\text{Lane}} = 26\text{ k}$

All values are lane loads. Since design truck moments and shears are based on wheel line load, the lane live loads must be divided by 2 to be compatible with the other loads.

	$M_{LL} = \frac{1}{2}(M_{1Lane} + M_{2Lane})$ $M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF$ $V_{LL} = \frac{1}{2}(V_{1Lane} + V_{2Lane})$ $V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF$	$M_{LL} = 81.25 \text{ ftk}$ $M_{LL_I_Lane} = 88.021 \text{ ftk}$ $V_{LL} = 17 \text{ k}$ $V_{LL_I_Lane} = 18.417 \text{ k}$
HS-20	<p>Max moment occur when rear axle is placed at midspan. Max shear occur for middle axle at one end</p> $M_{LL} = \frac{P \times L}{4}$ $M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$ $V_{LL} = P + \frac{L - 14\text{ft}}{L} \times P$ $V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$	$P = 16 \text{ k}$ $M_{LL} = 100 \text{ ftk}$ $M_{LL_I_HS20} = 108.333 \text{ ftk}$ $V_{LL} = 23.04 \text{ k}$ $V_{LL_I_HS20} = 24.96 \text{ k}$
H-20	<p>Max moment occur when rear axle is placed at midspan. Max shear occur for rear axle at one end.</p> $M_{LL} = \frac{P_1 \times L}{4}$ $M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$ $V_{LL} = P_1 + \frac{L - 14\text{ft}}{L} \times P_2$ $V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$	$P_1 = 16 \text{ k}$ $P_2 = 4 \text{ k}$ $M_{LL} = 100 \text{ ftk}$ $M_{LL_I_H20} = 108.333 \text{ ftk}$ $V_{LL} = 17.76 \text{ k}$ $V_{LL_I_H20} = 19.24 \text{ k}$
Type 3	<p>Max moment occur when middle axle is 11.5 ft from one end. Max shear occur for rear axle at the end.</p> $R_{end} = \frac{L - 11.5\text{ft}}{L} \times P_1 + \frac{L - 11.5\text{ft} - 4\text{ft}}{L} \times P_2$ $M_{LL} = R_{end} \times 11.5\text{ft}$ $M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$ $V_{LL} = P_1 + \frac{L - 4\text{ft}}{L} \times P_1 + \frac{L - 4\text{ft} - 15\text{ft}}{L} \times P_2$ $V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$	$P_1 = 8.5 \text{ k}$ $P_2 = 8 \text{ k}$ $R_{end} = 7.82 \text{ k}$ $M_{LL} = 89.93 \text{ ftk}$ $M_{LL_I_Type3} = 97.424 \text{ ftk}$ $V_{LL} = 17.56 \text{ k}$ $V_{LL_I_Type3} = 19.023 \text{ k}$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, curb, overlay and channel equally distributed to all girders/stringers.

Steel:	$w_b = w_{\text{steel}} \times A_b$	$w_b = 0.047 \frac{\text{k}}{\text{ft}}$
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Slab:	$w_s = w_{\text{concrete}} \times t_s \times (4\text{ft} + 7\text{in})$	$w_s = 0.559 \frac{\text{k}}{\text{ft}}$
Curb:	$w_c = w_{\text{concrete}} \times \frac{10\text{in} \times 27\text{in} + 10\text{in} \times 27\text{in}}{5}$	$w_c = 0.113 \frac{\text{k}}{\text{ft}}$
Channel:	$w_{ch} = w_{\text{steel}} \times 6.03\text{in}^2 \times \frac{2}{5}$	$w_{ch} = 8.206 \times 10^{-3} \frac{\text{k}}{\text{ft}}$

Total Dead Load = sum w

$DL = w_b + w_s + w_c + w_{ch}$	$DL = 0.726 \frac{\text{k}}{\text{ft}}$
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Uniform Load:

$M_{DL} = \frac{DL \times L^2}{8}$	$M_{DL} = 56.71 \text{ ftk}$
$V_{DL} = \frac{1}{2} \times DL \times L$	$V_{DL} = 9.074 \text{ k}$

Capacities:

$C = A_b \times F_y$		$C = 492.936 \text{ k}$	(10-124)
$AF_{tf} = A_{tf} \times F_y$	Top flange	$AF_{tf} = 140.25 \text{ k}$	
$AF_w = A_w \times F_y$	Web above welded plate	$AF_w = 212.436 \text{ k}$	
$AF_{bf} = A_{bf} \times F_y$	Bottom flange	$AF_{bf} = 140.25 \text{ k}$	
$y = t_{bf} + \frac{b_w}{2}$	Distance from bottom os steel to PNA	$y = 8.95 \text{ in}$	
$D_{cp} = \frac{b_w}{2}$	Depth of web in compression at PNA	$D_{cp} = 8.43 \text{ in}$	

Check compact:

$b = \frac{7.492\text{in} - 0.35\text{in}}{2}$	Width of projecting flange element	$b = 3.571 \text{ in}$	
$\frac{b}{t_w} \leq \frac{2055}{\sqrt{\frac{F_y}{1\text{psi}}}}$	$\frac{b}{t_w} = 10.203$	$\frac{2055}{\sqrt{\frac{F_y}{1\text{psi}}}} = 10.831$	OK! (10-93)
$\frac{D}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1\text{psi}}}}$	$\frac{D}{t_w} = 48.171$	$\frac{19230}{\sqrt{\frac{F_y}{1\text{psi}}}} = 101.351$	OK! (10-93)

Since not both of the two criteria above exceed 75% of limit => don't check (10-95)

$M_n = F_y \times Z$		(10-92)
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$y = 8.95 \text{ in}$	Distance from bottom of steel to PNA	$y = 8.95 \text{ in}$
$y_{bf} = y - \frac{0.52\text{in}}{2}$	Distance from PNA to C.G bottom flange	$y_{bf} = 8.69 \text{ in}$
$y_w = \frac{1}{2} \times \frac{16.86\text{in}}{2}$	Distance from PNA to C.G web above PNA	$y_w = 4.215 \text{ in}$

$$A_{tf} = 3.896 \text{ in}^2$$

Area of top flange

$$A_{tf} = 3.896 \text{ in}^2$$

$$A_w = 5.901 \text{ in}^2$$

Area of the whole web both above and below PNA

$$A_w = 5.901 \text{ in}^2$$

$$Z = 2 \times y_{bf} \times A_{tf} + 2 \times y_w \times \frac{A_w}{2} \quad \text{Plastic section modulus}$$

$$Z = 92.582 \text{ in}^3$$

$$M_n = F_y \times Z$$

$$M_n = 277.747 \text{ ft-k}$$

$$M_n = 3.333 \times 10^3 \text{ in} \times k$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$$

$$K = 5$$

For unstiffened beams and girders

$$D = 16.86 \text{ in}$$

Clear distance between flanges

$$t_w = 0.35 \text{ in}$$

Web thickness

$$\frac{D}{t_w} = 48.171$$

$$\frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 70.711 \quad \Rightarrow$$

$$C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 123.213 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p$$

$$V_n = 123.213 \text{ k} \quad (10-113)$$

Rating:

$$\text{Inventory:} \quad A_1 = 1.3 \quad A_{2i} = 2.17$$

$$\text{Operating:} \quad A_1 = 1.3 \quad A_{2o} = 1.3$$

Lane	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	$RF = 1.068$
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	$RF = 1.783$
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	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	$RF = 2.788$
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		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	$RF = 4.654$
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HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	$RF = 0.868$
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		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	$RF = 1.449$
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H-20	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 2.057
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 3.434
	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 0.868
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 1.449
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.669
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 4.455
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 0.965
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 1.611
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.699
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 4.505

Exterior Stringer (use dimensions from old girder => same as for interior stringer)

Loads For Lane Loading:

$P_s = 26k$	Point Load for Shear for Lane Loading	fig. 3.7.6.b
$P_m = 18k$	Point Load for Moment for Lane Loading	
$\omega = 0.64 \frac{k}{ft}$	Uniform Load for Lane Loading	

Live Load Distribution Factor:

overhang = 5in	Overhang of concrete slab		
$S_b = \frac{4ft + 7in}{2} + \text{overhang}$	Average stringer spacing in ft	$S_b = 2.708 \text{ ft}$	table 3.23.1
$DF_1 = \frac{S_b}{5.5ft}$		$DF_1 = 0.492$	3.23.2.3.1.5
Find new DF for treating the exterior stringer as a simple beam			3.23.2.3.1.2
$DF_2 = \frac{(4ft + 7in) - 5in - 2ft}{4ft + 7in}$		$DF_2 = 0.473$	

Use maximum distribution factor

$$DF = \max\left(\left(\frac{DF_1}{DF_2}\right)\right) \quad DF = 0.492$$

Section Properties:

$L = 25\text{ft}$	Design span of beam	
$t_s = 9.75\text{in}$	Thickness of concrete slab	
$A_b = A_{tf} + A_w + A_{bf}$		$A_b = 13.693\text{ in}^2$
$d = t_{tf} + b_w + t_{bf}$	Total depth of steel	$d = 17.9\text{ in}$
$D = b_w$	Clear distance between flanges	$D = 16.86\text{ in}$

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.3 \quad 3.8.2.1$$

Maximum Live Load Moments:

Lane Load $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear fig. 3.7.6.b
Uniform Load of 0.64 k/ft over the whole span

Uniform load:	$M1_{\text{Lane}} = \frac{\omega \times L^2}{8}$	$M1_{\text{Lane}} = 50\text{ftk}$
	$V1_{\text{Lane}} = \frac{1}{2} \times \omega \times L$	$V1_{\text{Lane}} = 8\text{ k}$
Point Load:	$M2_{\text{Lane}} = \frac{P_m \times L}{4}$	$M2_{\text{Lane}} = 112.5\text{ftk}$
	$V2_{\text{Lane}} = P_s$	$V2_{\text{Lane}} = 26\text{ k}$

All values are lane loads. Since the design truck moments are based on line loads, the lane loads must be divided by 2 to be compatible with the other loads.

$M_{LL} = \frac{1}{2}(M1_{\text{Lane}} + M2_{\text{Lane}})$	$M_{LL} = 81.25\text{ftk}$
$M_{LL_I_Lane} = M_{LL} \times (1 + I) \times DF$	$M_{LL_I_Lane} = 52.012\text{ftk}$
$V_{LL} = \frac{1}{2}(V1_{\text{Lane}} + V2_{\text{Lane}})$	$V_{LL} = 17\text{ k}$
$V_{LL_I_Lane} = V_{LL} \times (1 + I) \times DF$	$V_{LL_I_Lane} = 10.883\text{ k}$

HS-20 Max moment occur when rear axle is placed at midspan. Max shear occur for middle axle at one end

$M_{LL} = \frac{P \times L}{4}$	$M_{LL} = 100\text{ftk}$
$M_{LL_I_HS20} = M_{LL} \times (1 + I) \times DF$	$M_{LL_I_HS20} = 64.015\text{ftk}$
$V_{LL} = P + \frac{L - 14\text{ft}}{L} \times P$	$V_{LL} = 23.04\text{ k}$

	$V_{LL_I_HS20} = V_{LL} \times (1 + I) \times DF$	$V_{LL_I_HS20} = 14.749 \text{ k}$
H-20	Max moment occur when rear axle is placed at midspan. Max shear occur for rear axle at one end.	$P_1 = 16 \text{ k}$
	$M_{LL} = \frac{P_1 \times L}{4}$	$P_2 = 4 \text{ k}$
	$M_{LL_I_H20} = M_{LL} \times (1 + I) \times DF$	$M_{LL} = 100 \text{ ftk}$
	$V_{LL} = P_1 + \frac{L - 14 \text{ ft}}{L} \times P_2$	$M_{LL_I_H20} = 64.015 \text{ ftk}$
	$V_{LL_I_H20} = V_{LL} \times (1 + I) \times DF$	$V_{LL} = 17.76 \text{ k}$
Type 3	Max moment occur when middle axle is 11.5 ft from one end. Max shear occur for rear axle at the end.	$V_{LL_I_H20} = 11.369 \text{ k}$
	$R_{\text{end}} = \frac{L - 11.5 \text{ ft}}{L} \times P_1 + \frac{L - 11.5 \text{ ft} - 4 \text{ ft}}{L} \times P_1$	$P_1 = 8.5 \text{ k}$
	$M_{LL} = R_{\text{end}} \times 11.5 \text{ ft}$	$P_2 = 8 \text{ k}$
	$M_{LL_I_Type3} = M_{LL} \times (1 + I) \times DF$	$R_{\text{end}} = 7.82 \text{ k}$
	$V_{LL} = P_1 + \frac{L - 4 \text{ ft}}{L} \times P_1 + \frac{L - 4 \text{ ft} - 15 \text{ ft}}{L} \times P_2$	$M_{LL} = 89.93 \text{ ftk}$
	$V_{LL_I_Type3} = V_{LL} \times (1 + I) \times DF$	$M_{LL_I_Type3} = 57.569 \text{ ftk}$
		$V_{LL} = 17.56 \text{ k}$
		$V_{LL_I_Type3} = 11.241 \text{ k}$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, channel equally distributed to all girders/stringers. Assume curb to be distributed to the exterior beams only.

Steel:	$w_b = w_{\text{steel}} \times A_b$	$w_b = 0.047 \frac{\text{k}}{\text{ft}}$
Slab:	$w_s = w_{\text{concrete}} \times t_s \times \left(\frac{4 \text{ ft} + 7 \text{ in}}{2} + \text{overhang} \right)$	$w_s = 0.33 \frac{\text{k}}{\text{ft}}$
Curb:	$w_c = w_{\text{concrete}} \times (10 \text{ in} \times 27 \text{ in})$	$w_c = 0.281 \frac{\text{k}}{\text{ft}}$
Channel:	$w_{\text{ch}} = w_{\text{steel}} \times 6.03 \text{ in}^2 \times \frac{2}{5}$	$w_{\text{ch}} = 8.206 \times 10^{-3} \frac{\text{k}}{\text{ft}}$
Total Dead Load = sum w		
	$DL = w_b + w_s + w_c + w_{\text{ch}}$	$DL = 0.666 \frac{\text{k}}{\text{ft}}$

Uniform Load:

$M_{DL} = \frac{DL \times L^2}{8}$	$M_{DL} = 52.04 \text{ ftk}$
$V_{DL} = \frac{1}{2} \times DL \times L$	$V_{DL} = 8.326 \text{ k}$

Capacities:

$C = A_b \times F_y$	$C = 492.936 \text{ k}$	(10-124)
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$AF_{tf} = A_{tf} \times F_y$	Top flange	$AF_{tf} = 140.25 \text{ k}$
$AF_w = A_w \times F_y$	Web above welded plate	$AF_w = 212.436 \text{ k}$
$AF_{bf} = AF_{tf}$	Bottom flange	$AF_{bf} = 140.25 \text{ k}$
$y = t_{bf} + \frac{b_w}{2}$	Distance from bottom os steel to PNA	$y = 8.95 \text{ in}$
$D_{cp} = \frac{b_w}{2}$	Depth of web in compression at PNA	$D_{cp} = 8.43 \text{ in}$

Check compact:

$b = \frac{7.492\text{in} - 0.35\text{in}}{2}$	Width of projecting flange element	$b = 3.571 \text{ in}$	
$\frac{b}{t_w} \leq \frac{2055}{\sqrt{\frac{F_y}{1\text{psi}}}}$	$\frac{b}{t_w} = 10.203$	$\frac{2055}{\sqrt{\frac{F_y}{1\text{psi}}}} = 10.831$	OK! (10-93)
$\frac{D}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1\text{psi}}}}$	$\frac{D}{t_w} = 48.171$	$\frac{19230}{\sqrt{\frac{F_y}{1\text{psi}}}} = 101.351$	OK! (10-93)

Since not both of the two criteria above exceed 75% of limit => don't check (10-95)

$$M_n = F_y \times Z \quad (10-92)$$

$y = 8.95 \text{ in}$	Distance from bottom of steel to PNA	$y = 8.95 \text{ in}$
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$y_{bf} = y - \frac{0.52\text{in}}{2}$	Distance from PNA to C.G bottom flange	$y_{bf} = 8.69 \text{ in}$
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$y_w = \frac{1}{2} \times \frac{16.86\text{in}}{2}$	Distance from PNA to C.G web above PNA	$y_w = 4.215 \text{ in}$
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$A_{tf} = 3.896 \text{ in}^2$	Area of top flange	$A_{tf} = 3.896 \text{ in}^2$
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$A_w = 5.901 \text{ in}^2$	Area of the whole web both above and below PNA	$A_w = 5.901 \text{ in}^2$
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$Z = 2 \times y_{bf} \times A_{tf} + 2 \times y_w \times \frac{A_w}{2}$	Plastic section modulus	$Z = 92.582 \text{ in}^3$
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$$M_n = F_y \times Z \quad M_n = 277.747 \text{ ftk}$$

$$M_n = 3.333 \times 10^3 \text{ in} \times \text{k}$$

Shear Capacity:

Check (10-116)

$$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1\text{psi}}}}$$

$K = 5$	For unstiffened beams and girders
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$D = 16.86 \text{ in}$	Clear distance between flanges
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$t_w = 0.35 \text{ in}$	Web thickness
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$$\frac{D}{t_w} = 48.171 \quad \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 70.711 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w \quad V_p = 123.213 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p \quad V_n = 123.213 \text{ k} \quad (10-113)$$

Rating:

$$\text{Inventory:} \quad A_1 = 1.3 \quad A_{2i} = 2.17$$

$$\text{Operating:} \quad A_1 = 1.3 \quad A_{2o} = 1.3$$

$$\text{Lane} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}} \quad RF = 1.861$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}} \quad RF = 3.107$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}} \quad RF = 4.759$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}} \quad RF = 7.944$$

$$\text{HS-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}} \quad RF = 1.512$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}} \quad RF = 2.525$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}} \quad RF = 3.512$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}} \quad RF = 5.862$$

$$\text{H-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}} \quad RF = 1.512$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}} \quad RF = 2.525$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}} \quad RF = 4.556$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}} \quad RF = 7.604$$

$$\text{Type-3} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}} \quad RF = 1.682$$

	Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	$RF = 2.807$
Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	$RF = 4.607$
	Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	$RF = 7.691$

Exterior Stringer (new girder)Live Load Distribution Factor:

overhang = 12in

Overhang of concrete slab

$$S_b = \frac{4\text{ft} + 7\text{in}}{2} + \text{overhang} \quad \text{Average stringer spacing in ft} \quad S_b = 3.292 \text{ ft} \quad \text{table 3.23.1}$$

$$DF_1 = \frac{S_b}{5.5\text{ft}} \quad DF_1 = 0.598 \quad 3.23.2.3.1.5$$

Find new DF for treating the exterior stringer as a simple beam 3.23.2.3.1.2

$$DF_2 = \frac{(4\text{ft} + 7\text{in}) + 1\text{in} - 2\text{ft}}{4\text{ft} + 7\text{in}} \quad DF_2 = 0.582$$

Use maximum distribution factor

$$DF = \max\left(\left(\begin{matrix} DF_1 \\ DF_2 \end{matrix}\right)\right) \quad DF = 0.598$$

Section Properties:

$L = 25\text{ft}$	Design span of beam	
$t_s = 9.75\text{in}$	Thickness of concrete slab	
$A_b = 14.7\text{in}^2$		$A_b = 14.7\text{in}^2$
$d = 17.99\text{in}$	Total depth of steel	$d = 17.99\text{in}$
$D = 16.86\text{in}$	Clear distance between flanges	$D = 16.86\text{in}$
$Z = 101\text{in}^3$	Plastic section modulus	$Z = 101\text{in}^3$

Girder Loads:

$$I = \begin{cases} \frac{50\text{ft}}{L + 125\text{ft}} & \text{if } \frac{50\text{ft}}{L + 125\text{ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases} \quad \text{Impact} \quad I = 0.3 \quad 3.8.2.1$$

Maximum Live Load Moments:

Lane Load $P_m=18\text{k}$ for moment, $P_s=26\text{k}$ for shear fig. 3.7.6.b
 Uniform Load of 0.64 k/ft over the whole span

Uniform load:	$M_{1\text{Lane}} = \frac{\omega \times L^2}{8}$	$M_{1\text{Lane}} = 50 \text{ ftk}$
	$V_{1\text{Lane}} = \frac{1}{2} \times \omega \times L$	$V_{1\text{Lane}} = 8 \text{ k}$

$$\begin{aligned} \text{Point Load: } M_{2\text{Lane}} &= \frac{P_m \times L}{4} & M_{2\text{Lane}} &= 112.5 \text{ ftk} \\ V_{2\text{Lane}} &= P_s & V_{2\text{Lane}} &= 26 \text{ k} \end{aligned}$$

All values are lane loads. To get wheel line loads => divide live loads by 2.

$$\begin{aligned} M_{LL} &= \frac{1}{2}(M_{1\text{Lane}} + M_{2\text{Lane}}) & M_{LL} &= 81.25 \text{ ftk} \\ M_{LL_I_Lane} &= M_{LL} \times (1 + I) \times DF & M_{LL_I_Lane} &= 63.215 \text{ ftk} \\ V_{LL} &= \frac{1}{2}(V_{1\text{Lane}} + V_{2\text{Lane}}) & V_{LL} &= 17 \text{ k} \\ V_{LL_I_Lane} &= V_{LL} \times (1 + I) \times DF & V_{LL_I_Lane} &= 13.227 \text{ k} \end{aligned}$$

HS-20 Max moment occur when rear axle is placed at midspan. Max shear occur for middle axle at one end

$$P = 16 \text{ k}$$

$$\begin{aligned} M_{LL} &= \frac{P \times L}{4} & M_{LL} &= 100 \text{ ftk} \\ M_{LL_I_HS20} &= M_{LL} \times (1 + I) \times DF & M_{LL_I_HS20} &= 77.803 \text{ ftk} \\ V_{LL} &= P + \frac{L - 14 \text{ ft}}{L} \times P & V_{LL} &= 23.04 \text{ k} \\ V_{LL_I_HS20} &= V_{LL} \times (1 + I) \times DF & V_{LL_I_HS20} &= 17.926 \text{ k} \end{aligned}$$

H-20 Max moment occur when rear axle is placed at midspan. Max shear occur for rear axle at one end.

$$P_1 = 16 \text{ k}$$

$$P_2 = 4 \text{ k}$$

$$\begin{aligned} M_{LL} &= \frac{P_1 \times L}{4} & M_{LL} &= 100 \text{ ftk} \\ M_{LL_I_H20} &= M_{LL} \times (1 + I) \times DF & M_{LL_I_H20} &= 77.803 \text{ ftk} \\ V_{LL} &= P_1 + \frac{L - 14 \text{ ft}}{L} \times P_2 & V_{LL} &= 17.76 \text{ k} \\ V_{LL_I_H20} &= V_{LL} \times (1 + I) \times DF & V_{LL_I_H20} &= 13.818 \text{ k} \end{aligned}$$

Type 3 Max moment occur when middle axle is 11.5 ft from one end. Max shear occur for rear axle at the end.

$$P_1 = 8.5 \text{ k}$$

$$P_2 = 8 \text{ k}$$

$$\begin{aligned} R_{\text{end}} &= \frac{L - 11.5 \text{ ft}}{L} \times P_1 + \frac{L - 11.5 \text{ ft} - 4 \text{ ft}}{L} \times P_2 & R_{\text{end}} &= 7.82 \text{ k} \\ M_{LL} &= R_{\text{end}} \times 11.5 \text{ ft} & M_{LL} &= 89.93 \text{ ftk} \\ M_{LL_I_Type3} &= M_{LL} \times (1 + I) \times DF & M_{LL_I_Type3} &= 69.968 \text{ ftk} \\ V_{LL} &= P_1 + \frac{L - 4 \text{ ft}}{L} \times P_1 + \frac{L - 4 \text{ ft} - 15 \text{ ft}}{L} \times P_2 & V_{LL} &= 17.56 \text{ k} \\ V_{LL_I_Type3} &= V_{LL} \times (1 + I) \times DF & V_{LL_I_Type3} &= 13.662 \text{ k} \end{aligned}$$

Dead Loads (steel, parapet, slab, curb):

Assume "heaviest" steel throughout section. Assume slab, channel equally distributed to all girders/stringers. Assume curb to be distributed to the exterior beams only.

Steel:	$w_b = w_{\text{steel}} \times A_b$	$w_b = 0.05 \frac{k}{ft}$
Slab:	$w_s = w_{\text{concrete}} \times t_s \times \left(\frac{4ft + 7in}{2} + \text{overhang} \right)$	$w_s = 0.401 \frac{k}{ft}$
Curb:	$w_c = w_{\text{concrete}} \times (10in \times 27in)$	$w_c = 0.281 \frac{k}{ft}$
Channel:	$w_{ch} = w_{\text{steel}} \times 6.03in^2 \times \frac{2}{5}$	$w_{ch} = 8.206 \times 10^{-3} \frac{k}{ft}$

Total Dead Load = sum w

$DL = w_b + w_s + w_c + w_{ch}$	$DL = 0.741 \frac{k}{ft}$
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Uniform Load:

$M_{DL} = \frac{DL \times L^2}{8}$	$M_{DL} = 57.862 \text{ ftk}$
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$V_{DL} = \frac{1}{2} \times DL \times L$	$V_{DL} = 9.258 k$
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Capacities:

$b = \frac{7.495in - 0.355in}{2}$	Width of projecting flange element
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$t_w = 0.355in$	Thickness of web
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$D = 16.86 in$	Clear distance between flanges
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Check compact:

$\frac{b}{t_w} \leq \frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$	$\frac{b}{t_w} = 10.056$	$\frac{2055}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 10.831$	OK!	(10-93)
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$\frac{D}{t_w} \leq \frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$	$\frac{D}{t_w} = 47.493$	$\frac{19230}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 101.351$	OK!	(10-93)
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Since not both of the two criteria above exceed 75% of limit => don't check (10-95)

$M_n = F_y \times Z$	(10-92)
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$Z = 101 in^3$	Plastic section modulus from Manual of Steel Construction.
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$M_n = F_y \times Z$	$M_n = 303 \text{ ftk}$
	$M_n = 3.636 \times 10^3 \text{ in} \times k$

Shear Capacity:

Check (10-116)

$\frac{D}{t_w} \leq \frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}}$
--

$$K = 5$$

$$D = 16.86 \text{ in}$$

$$t_w = 0.355 \text{ in}$$

$$\frac{D}{t_w} = 47.493$$

For unstiffened beams and girders

Clear distance between flanges

Web thickness

$$\frac{6000 \times \sqrt{K}}{\sqrt{\frac{F_y}{1 \text{ psi}}}} = 70.711 \quad \Rightarrow \quad C = 1.0 \quad (10-116)$$

$$V_p = 0.58 \times F_y \times D \times t_w$$

$$V_p = 124.973 \text{ k} \quad (10-115)$$

$$V_n = C \times V_p$$

$$V_n = 124.973 \text{ k} \quad (10-113)$$

Rating:

$$\text{Inventory:} \quad A_1 = 1.3 \quad A_{2i} = 2.17$$

$$\text{Operating:} \quad A_1 = 1.3 \quad A_{2o} = 1.3$$

$$\text{Lane} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}} \quad RF = 1.66$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}} \quad RF = 2.772$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}} \quad RF = 3.935$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}} \quad RF = 6.568$$

$$\text{HS-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}} \quad RF = 1.349$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}} \quad RF = 2.252$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}} \quad RF = 2.903$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}} \quad RF = 4.846$$

$$\text{H-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}} \quad RF = 1.349$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}} \quad RF = 2.252$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}} \quad RF = 3.767$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}} \quad RF = 6.287$$

Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL-I_Type3}}$	RF = 1.5
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL-I_Type3}}$	RF = 2.504
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL-I_Type3}}$	RF = 3.809
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL-I_Type3}}$	RF = 6.359

D.6. RATING FOR BRIDGE #6

Units:

$$k = 1000\text{lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2} \quad \text{ink} = \text{in} \times k$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of concrete}$$

$$w_{\text{fill}} = 125 \frac{\text{lb}}{\text{ft}^3} \quad \text{Weight of fill on top of slab}$$

$$f_c = 3\text{ksi} \quad \text{Concrete strength}$$

$$F_y = 40\text{ksi} \quad \text{Steel strength}$$

Input:

$$t_s = 15.6\text{in} \quad \text{Thickness of concrete slab} \quad t_s = 15.6\text{in}$$

$$t_{\text{fill}} = 2.38\text{ft} \quad \text{Thickness of fill + AC} \quad t_{\text{fill}} = 2.38\text{ft}$$

$$b = 1\text{ft} \quad \text{All calculations are one-foot strip}$$

$$\phi_m = 0.9 \quad \text{Strength reduction factor for Flexure} \quad 8.16.1.2.2$$

$$\phi_s = 0.85 \quad \text{Strength reduction factor for Shear}$$

Span Length:

$$L_1 = 20\text{ft} \quad \text{Distance cc supports} \quad L_1 = 20\text{ft}$$

$$L_2 = 18\text{ft} + t_s \quad \text{Clear distance plus } t_s \quad L_2 = 19.3\text{ft}$$

$$L = \min \left(\left(L_1 \right) \right) \quad \text{Span Length} \quad L = 19.3\text{ft} \quad 3.24.1.1$$

$$L = 20\text{ft} \quad \text{Use Design span} \quad L = 20\text{ft}$$

Impact:

$$I = 0.1 \quad \text{Impact. 2.38 ft of fill.} \quad I = 0.1 \quad 3.8.2.3$$

Steel Reinforcing per one-foot strip:

$$F_s = 4736 \text{ lb}$$

$$L_s = 22 \text{ ft} + 2 \text{ in}$$

$$b_s = 39 \text{ ft} + 8 \text{ in}$$

$$A_s = \frac{F_s}{w_{\text{steel}}} \times \frac{1}{L_s \times b_s} \times 1 \text{ ft}$$

$$d = 13 \text{ in}$$

Total weight of reinf in slab

Total length of steel reinforcement

Width of slab

Steel area per one-foot strip

Dist from top of slab to reinf

$$F_s = 4.736 \text{ k}$$

$$L_s = 22.167 \text{ ft}$$

$$b_s = 39.667 \text{ ft}$$

$$A_s = 1.583 \text{ in}^2$$

$$d = 13 \text{ in}$$

Dead Load Moment per one-foot strip

$$DL_s = w_{\text{steel}} \times A_s$$

$$DL_c = w_{\text{concrete}} \times t_s \times b$$

$$DL_{\text{fill}} = w_{\text{fill}} \times t_{\text{fill}} \times b$$

$$DL = DL_s + DL_c + DL_{\text{fill}}$$

$$M_{DL} = \frac{DL \times L^2}{8}$$

Reinforcement

Concrete

Fill

Total dead load

Dead Load Moment per one-foot strip

$$DL_s = 5.386 \frac{\text{lb}}{\text{ft}}$$

$$DL_c = 195 \frac{\text{lb}}{\text{ft}}$$

$$DL_{\text{fill}} = 297.5 \frac{\text{lb}}{\text{ft}}$$

$$DL = 497.886 \frac{\text{lb}}{\text{ft}}$$

$$M_{DL} = 24.894 \text{ ftk}$$

Dead Load Shear per one-foot strip:

$$V_{DL} = \frac{1}{2} \times DL \times L$$

$$V_{DL} = 4.979 \text{ k}$$

Moment Capacity per one-foot strip:

$$a = \frac{A_s \times F_y}{0.85 \times f_c \times b}$$

$$M_n = \phi_m \times A_s \times F_y \times \left(d - \frac{a}{2} \right)$$

Moment Capacity per foot

$$a = 2.07 \text{ in}$$

$$M_n = 56.832 \text{ ftk}$$

Shear Capacity per one-foot strip:

$$F_v = 786 \text{ lb}$$

$$A_v = \frac{F_v}{w_{\text{steel}}} \times \frac{1}{L_s \times b_s} \times 1 \text{ ft}$$

$$s = 1 \text{ ft}$$

$$V_c = 2 \times \sqrt{\frac{f_c}{1 \text{ psi}}} \times 1 \text{ psi} \times b \times d$$

$$V_s = \frac{A_v \times F_y \times d}{s}$$

$$V_n = \phi_s \times (V_c + V_s)$$

Weight of reinforcement perpendicular to traffic

Steel area per one-foot strip, perpendicular to traffic

One-foot strip

$$F_v = 0.786 \text{ k}$$

$$A_v = 0.263 \text{ in}^2$$

$$V_c = 17.089 \text{ k}$$

$$V_s = 11.386 \text{ k}$$

$$V_n = 24.204 \text{ k}$$

8.16.6.2.1

Loads For Lane Loading:

$$P_s = 26k$$

Point Load for Shear for Lane Loading

fig. 3.7.6.b

$$P_m = 18k$$

Point Load for Moment for Lane Loading

$$\omega = 0.64 \frac{k}{ft}$$

Uniform Load for Lane Loading

Distribution Width:

Main reinforcement is parallel to traffic

$$E = \begin{cases} 4 + 0.06 \times \left(\frac{L}{1ft} \right) & \text{if } 4 + 0.06 \times \left(\frac{L}{1ft} \right) \leq 7 \\ 7 & \text{otherwise} \end{cases}$$

$$E = 5.2$$

3.24.3.2

Live Load Moment for L = 20 ft:

$$\text{Lane Load } M_{LL} = \frac{P_m \times L}{4} + \frac{\omega \times L^2}{8}$$

Moment per 10-ft lane

$$M_{LL} = 122 \text{ ftk}$$

Fig.3.7.6.b

3.7.1.2

$$M_{LL_I_Lane} = \frac{M_{LL} \times (1 + I)}{2 \times E}$$

$$M_{LL_I_Lane} = 12.904 \text{ ftk}$$

3.24.3.2

$$\text{HS-20 } M_{truck} = 160 \text{ ftk}$$

Moment per truck

$$M_{truck} = 160 \text{ ftk}$$

AASHTO p.632

$$M_{LL} = \frac{1}{2} \times M_{truck}$$

Moment per wheel line

$$M_{LL} = 80 \text{ ftk}$$

$$M_{LL_I_HS20} = \frac{M_{LL} \times (1 + I)}{E}$$

$$M_{LL_I_HS20} = 16.923 \text{ ftk}$$

p.631

$$\text{H-20 } M_{truck} = 160 \text{ ftk}$$

Moment per truck

$$M_{truck} = 160 \text{ ftk}$$

$$M_{LL} = \frac{1}{2} \times M_{truck}$$

Moment per wheel line

$$M_{LL} = 80 \text{ ftk}$$

$$M_{LL_I_H20} = \frac{M_{LL} \times (1 + I)}{E}$$

$$M_{LL_I_H20} = 16.923 \text{ ftk}$$

$$\text{Type-3 } M_{truck} = 137.7 \text{ ftk}$$

Moment per truck

$$M_{truck} = 137.7 \text{ ftk}$$

Excel

$$M_{LL} = \frac{1}{2} \times M_{truck}$$

Moment per wheel line

$$M_{LL} = 68.85 \text{ ftk}$$

$$M_{LL_I_Type3} = \frac{M_{LL} \times (1 + I)}{E}$$

$$M_{LL_I_Type3} = 14.564 \text{ ftk}$$

Live Load Shear for L = 20 ft:

$$\text{Lane Load } V_{LL} = P_s + \frac{1}{2} \times \omega \times L$$

Shear per 10-ft lane

$$V_{LL} = 32.4 \text{ k}$$

Fig.3.7.6.b

3.7.1.2

$$V_{LL_I_Lane} = \frac{V_{LL} \times (1 + I)}{2 \times E}$$

$$V_{LL_I_Lane} = 3.427 \text{ k}$$

3.24.3.2

$$\text{HS-20 } V_{truck} = 32k + 32k \times \frac{20ft - 14ft}{20ft}$$

$$V_{truck} = 41.6 \text{ k}$$

	$V_{LL} = \frac{1}{2} \times V_{truck}$	Shear per wheel line	$V_{LL} = 20.8 \text{ k}$
	$V_{LL_I_HS20} = \frac{V_{LL} \times (1 + I)}{E}$		$V_{LL_I_HS20} = 4.4 \text{ k}$
H-20	$V_{truck} = 32\text{k} + 8\text{k} \times \frac{20\text{ft} - 14\text{ft}}{20\text{ft}}$		$V_{truck} = 34.4 \text{ k}$
	$V_{LL} = \frac{1}{2} \times V_{truck}$	Shear per wheel line	$V_{LL} = 17.2 \text{ k}$
	$V_{LL_I_H20} = \frac{V_{LL} \times (1 + I)}{E}$		$V_{LL_I_H20} = 3.638 \text{ k}$
Type-3	$V_{truck} = 17\text{k} + 17\text{k} \times \frac{20\text{ft} - 4\text{ft}}{20\text{ft}} + 16\text{k} \times \frac{20\text{ft} - 19\text{ft}}{20\text{ft}}$		$V_{truck} = 31.4 \text{ k}$
	$V_{LL} = \frac{1}{2} \times V_{truck}$	Shear per wheel line	$V_{LL} = 15.7 \text{ k}$
	$V_{LL_I_Type3} = \frac{V_{LL} \times (1 + I)}{E}$		$V_{LL_I_Type3} = 3.321 \text{ k}$

Rating:

Inventory:	$A_1 = 1.3$	$A_{2i} = 2.17$		
Operating:	$A_1 = 1.3$	$A_{2o} = 1.3$		
Lane Load	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	$RF = 0.874$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	$RF = 1.459$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	$RF = 2.384$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	$RF = 3.98$
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	$RF = 0.666$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	$RF = 1.112$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	$RF = 1.857$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	$RF = 3.1$
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	$RF = 0.666$

Type-3	Shear:	Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_H20}}$	RF = 1.112
		Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.246
	Flexure:	Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_H20}}$	RF = 3.749
		Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 0.774
	Shear:	Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{20} \times M_{LL_I_Type3}}$	RF = 1.292
		Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.46
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{20} \times V_{LL_I_Type3}}$	RF = 4.107
		Inventory:		

LOADS EXTRACTED FROM THE BDI-SOFTWARE PER ONE-INCH STRIP

HS-20	Flexure	Inventory	Dead load per inch-strip	$M_{DL_HS20} = 15.76 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 9.789 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 10.768 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_HS20} = 0.4579k$
			Live load per inch-strip	$V_{LL} = 0.3321k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 0.365k$
H-20	Flexure	Inventory	Dead load per inch-strip	$M_{DL_H20} = 15.76 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 9.789 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 10.768 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_H20} = 0.4579k$
			Live load per inch-strip	$V_{LL} = 0.3002k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 0.33k$
Type-3	Flexure	Inventory	Dead load per inch-strip	$M_{DL_Type3} = 15.76 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 7.23 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 7.953 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_Type3} = 0.4579k$
			Live load per inch-strip	$V_{LL} = 0.251k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 0.276k$

Capacities converted from one-foot strip to one-inch strip

$$\text{Moment capacity per one-inch strip} \quad M_n = \frac{M_n}{12} \quad M_n = 56.832 \text{ in} \times k$$

$$\text{Shear Capacity per one-inch strip} \quad V_n = \frac{V_n}{12} \quad V_n = 2.017 k$$

BDI Ratings:

$$\text{HS-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}} \quad RF = 1.555$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}} \quad RF = 2.596$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}} \quad RF = 1.793$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}} \quad RF = 2.994$$

$$\text{H-20} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}} \quad RF = 1.555$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}} \quad RF = 2.596$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}} \quad RF = 1.984$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}} \quad RF = 3.312$$

$$\text{Type-3} \quad \text{Flexure:} \quad \text{Inventory:} \quad RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}} \quad RF = 2.106$$

$$\text{Operating:} \quad RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}} \quad RF = 3.515$$

$$\text{Shear:} \quad \text{Inventory:} \quad RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}} \quad RF = 2.373$$

$$\text{Operating:} \quad RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}} \quad RF = 3.961$$

D.7. RATING FOR BRIDGE #7Units:

$$k = 1000 \text{ lb} \quad \text{ksi} = \frac{k}{\text{in}^2} \quad \text{ftk} = k \times \text{ft} \quad \text{psi} = 1 \frac{\text{lb}}{\text{in}^2} \quad \text{ink} = \text{in} \times k$$

Material properties:

$$w_{\text{steel}} = 0.2835 \frac{\text{lb}}{\text{in}^3} \quad \text{Weight of steel}$$

$$w_{\text{concrete}} = 150 \frac{\text{lb}}{\text{ft}^3}$$

$$f_c = 3 \text{ ksi}$$

$$F_y = 30 \text{ ksi}$$

Input:

$$t_s = 22 \text{ in}$$

$$b = 1 \text{ ft}$$

$$\phi_m = 0.9$$

$$\phi_s = 0.85$$

Span Length:

$$L_1 = (23 \text{ ft} + 8.5 \text{ in}) + (1 \text{ ft} + 3 \text{ in})$$

$$L_2 = (23 \text{ ft} + 8.5 \text{ in}) + t_s$$

$$L = \min \left(\begin{pmatrix} L_1 \\ L_2 \end{pmatrix} \right)$$

$$L = 25 \text{ ft}$$

Impact:

$$I = \begin{cases} \frac{50 \text{ ft}}{L + 125 \text{ ft}} & \text{if } \frac{50 \text{ ft}}{L + 125 \text{ ft}} \leq 0.3 \\ 0.3 & \text{otherwise} \end{cases}$$

Steel Reinforcing per one-foot strip:

$$A_s = 1.864 \text{ in}^2$$

$$d = 20.5 \text{ in}$$

Dead Load Moment per one-foot strip

$$DL_s = w_{\text{steel}} \times A_s$$

$$DL_c = w_{\text{concrete}} \times t_s \times b$$

$$DL_{si} = 126.8 \frac{\text{lb}}{\text{ft}}$$

$$DL = DL_s + DL_c + DL_{si}$$

$$M_{DL} = \frac{DL \times L^2}{8}$$

Dead Load Shear per one-foot strip:

$$V_{DL} = \frac{1}{2} \times DL \times L$$

Weight of concrete

Concrete strength

Steel strength

Thickness of concrete slab

$$t_s = 22 \text{ in}$$

All calculations are one-foot strip

Strength reduction factor for Flexure

8.16.1.2.2

Strength reduction factor for Shear

Distance cc supports

$$L_1 = 24.958 \text{ ft}$$

Clear distance plus t_s

$$L_2 = 25.542 \text{ ft}$$

Span Length

$$L = 24.958 \text{ ft}$$

3.24.1.1

Use Design span

$$L = 25 \text{ ft}$$

Impact

$$I = 0.3$$

3.8.2.1

From Iowa DOT

$$A_s = 1.864 \text{ in}^2$$

Dist from top of slab to reinf

$$d = 20.5 \text{ in}$$

Reinforcement

$$DL_s = 6.341 \frac{\text{lb}}{\text{ft}}$$

Concrete

$$DL_c = 275 \frac{\text{lb}}{\text{ft}}$$

Superimposed dead load
(Steel rail and additional
slab weight)

$$DL_{si} = 126.8 \frac{\text{lb}}{\text{ft}}$$

Total dead load

$$DL = 408.141 \frac{\text{lb}}{\text{ft}}$$

Dead Load Moment per
one-foot strip

$$M_{DL} = 31.886 \text{ ftk}$$

$$V_{DL} = 5.102 \text{ k}$$

Moment Capacity per one-foot strip:

$$a = \frac{A_s \times F_y}{0.85 \times f_c \times b}$$

$$a = 1.827 \text{ in}$$

$$M_n = \phi_m \times A_s \times F_y \times \left(d - \frac{a}{2} \right)$$

Moment Capacity per foot

$$M_n = 82.145 \text{ ftk}$$

Shear Capacity per one-foot strip:

$$D = 0.5 \text{ in}$$

Diameter of reinforcement perpendicular to traffic

$$D = 0.5 \text{ in}$$

$$A_v = \frac{\pi \times D^2}{4}$$

Area of reinforcement perpendicular to traffic

$$A_v = 0.196 \text{ in}^2$$

$$s = 1 \text{ ft}$$

$$V_c = 2 \times \sqrt{\frac{f_c}{1 \text{ psi}}} \times 1 \text{ psi} \times b \times d$$

$$V_c = 26.948 \text{ k}$$

8.16.6.2.1

$$V_s = \frac{A_v \times F_y \times d}{s}$$

$$V_s = 10.063 \text{ k}$$

$$V_n = \phi_s \times (V_c + V_s)$$

$$V_n = 31.459 \text{ k}$$

Loads For Lane Loading:

$$P_s = 26 \text{ k}$$

Point Load for Shear for Lane Loading

fig. 3.7.6.b

$$P_m = 18 \text{ k}$$

Point Load for Moment for Lane Loading

$$\omega = 0.64 \frac{\text{k}}{\text{ft}}$$

Uniform Load for Lane Loading

Distribution Width:

Main reinforcement is parallel to traffic

$$E = \begin{cases} 4 + 0.06 \times \left(\frac{L}{1 \text{ ft}} \right) & \text{if } 4 + 0.06 \times \left(\frac{L}{1 \text{ ft}} \right) \leq 7 \\ 7 & \text{otherwise} \end{cases}$$

$$E = 5.5$$

3.24.3.2

Live Load Moment for L = 25 ft:

$$\text{Lane Load } M_{LL} = \frac{P_m \times L}{4} + \frac{\omega \times L^2}{8}$$

Moment per 10-foot lane

$$M_{LL} = 162.5 \text{ ftk}$$

Fig.3.7.6.b

3.7.1.2

$$M_{LL_I_Lane} = \frac{M_{LL} \times (1 + I)}{2 \times E}$$

$$M_{LL_I_Lane} = 19.205 \text{ ftk}$$

3.24.3.2

$$\text{HS-20 } M_{\text{truck}} = 207.4 \text{ ftk}$$

Moment per truck

$$M_{\text{truck}} = 207.4 \text{ ftk}$$

AASHTO p.632

$$M_{LL} = \frac{1}{2} \times M_{\text{truck}}$$

Moment per wheel line

$$M_{LL} = 103.7 \text{ ftk}$$

$$M_{LL_I_HS20} = \frac{M_{LL} \times (1 + I)}{E}$$

$$M_{LL_I_HS20} = 24.511 \text{ ftk}$$

p.631

H-20	$M_{\text{truck}} = 200 \text{ftk}$	Moment per truck	$M_{\text{truck}} = 200 \text{ftk}$	
	$M_{\text{LL}} = \frac{1}{2} \times M_{\text{truck}}$	Moment per wheel line	$M_{\text{LL}} = 100 \text{ftk}$	
	$M_{\text{LL}_I\text{H20}} = \frac{M_{\text{LL}} \times (1 + I)}{E}$		$M_{\text{LL}_I\text{H20}} = 23.636 \text{ftk}$	
Type-3	$M_{\text{truck}} = 179.9 \text{ftk}$	Moment per truck	$M_{\text{truck}} = 179.9 \text{ftk}$	Excel
	$M_{\text{LL}} = \frac{1}{2} \times M_{\text{truck}}$	Moment per wheel line	$M_{\text{LL}} = 89.95 \text{ftk}$	
	$M_{\text{LL}_I\text{Type3}} = \frac{M_{\text{LL}} \times (1 + I)}{E}$		$M_{\text{LL}_I\text{Type3}} = 21.261 \text{ftk}$	
<u>Live Load Shear for L = 25 ft:</u>				
Lane Load	$V_{\text{LL}} = P_s + \frac{1}{2} \times \omega \times L$	Shear per lane	$V_{\text{LL}} = 34 \text{k}$	
	$V_{\text{LL}_I\text{Lane}} = \frac{V_{\text{LL}} \times (1 + I)}{2 \times E}$		$V_{\text{LL}_I\text{Lane}} = 4.018 \text{k}$	
HS-20	$V_{\text{truck}} = 32\text{k} + 32\text{k} \times \frac{25\text{ft} - 14\text{ft}}{25\text{ft}}$		$V_{\text{truck}} = 46.08 \text{k}$	
	$V_{\text{LL}} = \frac{1}{2} \times V_{\text{truck}}$	Shear per wheel line	$V_{\text{LL}} = 23.04 \text{k}$	
	$V_{\text{LL}_I\text{HS20}} = \frac{V_{\text{LL}} \times (1 + I)}{E}$		$V_{\text{LL}_I\text{HS20}} = 5.446 \text{k}$	
H-20	$V_{\text{truck}} = 32\text{k} + 8\text{k} \times \frac{25\text{ft} - 14\text{ft}}{25\text{ft}}$		$V_{\text{truck}} = 35.52 \text{k}$	
	$V_{\text{LL}} = \frac{1}{2} \times V_{\text{truck}}$	Shear per wheel line	$V_{\text{LL}} = 17.76 \text{k}$	
	$V_{\text{LL}_I\text{H20}} = \frac{V_{\text{LL}} \times (1 + I)}{E}$		$V_{\text{LL}_I\text{H20}} = 4.198 \text{k}$	
Type-3	$V_{\text{truck}} = 17\text{k} + 17\text{k} \times \frac{25\text{ft} - 4\text{ft}}{25\text{ft}} + 16\text{k} \times \frac{25\text{ft} - 19\text{ft}}{25\text{ft}}$		$V_{\text{truck}} = 35.12 \text{k}$	
	$V_{\text{LL}} = \frac{1}{2} \times V_{\text{truck}}$	Shear per wheel line	$V_{\text{LL}} = 17.56 \text{k}$	
	$V_{\text{LL}_I\text{Type3}} = \frac{V_{\text{LL}} \times (1 + I)}{E}$		$V_{\text{LL}_I\text{Type3}} = 4.151 \text{k}$	

Rating:Inventory: $A_1 = 1.3$ $A_{2i} = 2.17$ Operating: $A_1 = 1.3$ $A_{2o} = 1.3$

Lane Load:	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Lane}}$	RF = 0.976
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Lane}}$	RF = 1.63
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Lane}}$	RF = 2.847
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Lane}}$	RF = 4.753
HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_HS20}}$	RF = 0.765
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_HS20}}$	RF = 1.277
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_HS20}}$	RF = 2.101
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_HS20}}$	RF = 3.507
H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_H20}}$	RF = 0.793
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_H20}}$	RF = 1.324
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.725
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_H20}}$	RF = 4.549
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 0.882
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 1.472
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.757
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 4.601

LOADS EXTRACTED FROM THE BDI-SOFTWARE PER ONE-INCH STRIP

HS-20	Flexure	Inventory	Dead load per inch-strip	$M_{DL_HS20} = 22.65 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 11.90 \text{ in} \times k$
			$M_{LL_I_HS20} = M_{LL} \times (1 + I)$	$M_{LL_I_HS20} = 15.47 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_HS20} = 0.4290k$
			Live load per inch-strip	$V_{LL} = 0.3755k$
			$V_{LL_I_HS20} = V_{LL} \times (1 + I)$	$V_{LL_I_HS20} = 0.488k$
H-20	Flexure	Inventory	Dead load per inch-strip	$M_{DL_H20} = 23.25 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 11.47 \text{ in} \times k$
			$M_{LL_I_H20} = M_{LL} \times (1 + I)$	$M_{LL_I_H20} = 14.911 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_H20} = 0.4266k$
			Live load per inch-strip	$V_{LL} = 0.3179k$
			$V_{LL_I_H20} = V_{LL} \times (1 + I)$	$V_{LL_I_H20} = 0.413k$
Type-3	Flexure	Inventory	Dead load per inch-strip	$M_{DL_Type3} = 23.25 \text{ in} \times k$
			Live load per inch-strip	$M_{LL} = 9.499 \text{ in} \times k$
			$M_{LL_I_Type3} = M_{LL} \times (1 + I)$	$M_{LL_I_Type3} = 12.349 \text{ in} \times k$
	Shear	Inventory	Dead load per inch-strip	$V_{DL_Type3} = 0.4266k$
			Live load per inch-strip	$V_{LL} = 0.2656k$
			$V_{LL_I_Type3} = V_{LL} \times (1 + I)$	$V_{LL_I_Type3} = 0.345k$

Capacities converted from one-foot strip to one-inch strip

Moment capacity per one-inch strip	$M_n = \frac{M_n}{12}$	$M_n = 82.145 \text{ in} \times k$
Shear Capacity per one-inch strip	$V_n = \frac{V_n}{12}$	$V_n = 2.622k$

BDI Ratings:

HS-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2i} \times M_{LL_I_HS20}}$	$RF = 1.57$
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_HS20}}{A_{2o} \times M_{LL_I_HS20}}$	$RF = 2.62$
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2i} \times V_{LL_I_HS20}}$	$RF = 1.948$
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_HS20}}{A_{2o} \times V_{LL_I_HS20}}$	$RF = 3.252$

H-20	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2i} \times M_{LL_I_H20}}$	RF = 1.605
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_H20}}{A_{2o} \times M_{LL_I_H20}}$	RF = 2.678
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2i} \times V_{LL_I_H20}}$	RF = 2.305
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_H20}}{A_{2o} \times V_{LL_I_H20}}$	RF = 3.847
Type-3	Flexure:	Inventory:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2i} \times M_{LL_I_Type3}}$	RF = 1.938
		Operating:	$RF = \frac{M_n - A_1 \times M_{DL_Type3}}{A_{2o} \times M_{LL_I_Type3}}$	RF = 3.234
	Shear:	Inventory:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2i} \times V_{LL_I_Type3}}$	RF = 2.759
		Operating:	$RF = \frac{V_n - A_1 \times V_{DL_Type3}}{A_{2o} \times V_{LL_I_Type3}}$	RF = 4.605